# Vector seasonality, host infection dynamics and fitness of pathogens transmitted by the tick *Ixodes scapularis*

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#### $\rm S\,U\,M\,M\,A\,R\,Y$

Fitness of tick-borne pathogens may be determined by the degree to which their infection dynamics in vertebrate hosts permits transmission cycles if infective and uninfected tick stages are active at different times of the year. To investigate this hypothesis we developed a simulation model that integrates the transmission pattern imposed by seasonally asynchronous nymphal and larval *Ixodes scapularis* ticks in northeastern North America, with a model of infection in white-footed mice (*Peromyscus leucopus*) reservoir hosts, using the bacteria *Borrelia burgdorferi* and *Anaplasma phagocytophilum* as examples. In simulations, survival of microparasites, their sensitivity to reduced rodent and tick abundance, and to 'dilution' by a reservoir-incompetent host depended on traits that allowed (i) highly efficient transmission from acutely-infected hosts, (ii) long-lived acute or 'carrier' host infections, and/or (iii) transmission amongst co-feeding ticks. Minimum values for transmission efficiency to ticks, and duration of host infectivity, necessary for microparasite persistence, were always higher when nymphal and larval ticks were seasonally asynchronous than when these instars were synchronous. Thus, traits influencing duration of host infectivity, transmission efficiency to ticks and co-feeding transmission are likely to be dominant determinants of fitness in *I. scapularis*-borne microparasites in northeastern North America due to abiotic forcings influencing *I. scapularis* seasonality.

Key words: Ixodes scapularis, Peromyscus leucopus, white-footed mouse, model, fitness, Borrelia burgdorferi, Anaplasma phagocytophilum.

# INTRODUCTION

Ixodes scapularis is the tick vector of a number of tick borne zoonoses, including Lyme borreliosis, one of the most frequent vector-borne zoonoses in temperate zones (Thompson *et al.* 2001), which is caused by the bacterium *Borrelia burgdorferi* in northeastern North America. It is believed that transmission cycles of *B. burgdorferi* are very efficient in northeastern North America because the seasonal activity of nymphal and larval *Ixodes scapularis* ticks is asynchronous (Wilson and Spielman, 1985). Typically, infected nymphs become active in spring and early summer transmitting the bacteria to rodents (particularly white footed mice: *Peromyscus leucopus*).

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Non-infected larvae that are active in mid to late summer then acquire the infection from persistently infected rodents. Larvae maintain infection through the molt, giving rise to a new population of infected host-seeking nymphs in the following spring (Yuval and Spielman, 1990). The efficiency of this cycle leads to a high prevalence of *B. burgdorferi* infection in questing nymphal ticks, and a high public health risk in the region (Thompson *et al.* 2001).

In addition to *B. burgdorferi*, *I. scapularis* ticks and *P. leucopus* rodents maintain the bacterium *Anaplasma phagocytophilum* and the protozoan *Babesia microti*, which cause human granulocytic anaplasmosis and human babesiosis respectively (Thompson *et al.* 2001). The transmission efficiency of most strains of *B. burgdorferi* from acutely infected rodent hosts to ticks is usually very high (>50%: Donahue *et al.* 1987; Derdáková *et al.* 2004), compared with *A. phagocytophilum* and *B. microti* (Mather *et al.* 1990; Massung *et al.* 2004). Typically, *B. burgdorferi* is transmitted with high efficiency from *P. leucopus* rodents almost life-long (Donahue

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et al. 1987), but some strains and A. phagocytophilum have short infective periods in rodent hosts (Lindsay et al. 1997; Derdáková et al. 2004; Massung et al. 2004). Variation in longevity and transmissibility of host infections with these pathogens is likely to affect the public health risk via effects on infection prevalence in questing nymphs (Porco, 1999).

For the pathogens to survive in an I. scapularisrodent cycle, the duration of rodent infectivity for ticks must span any gap between the seasons of nymphal and larval activity (Randolph, 2001). The duration of infectivity is a crucial measure of fitness in different host species for vector-borne pathogens and particularly for B. burgdorferi in northeastern USA (Brisson and Dykhuizen, 2004; Tsao et al. 2004; Hanincová et al. 2006) and it has been suggested that B. burgdorferi strains that are short-lived in rodents are better adapted to alternative reservoir hosts (Derdáková et al. 2004). However, for I. scapularis-borne zoonoses investigated to date, recovery of rodents from acute, highly transmissible infections (if they actually do recover) is not complete, and the rodents remain persistently infective 'carriers' that transmit infection to ticks with low efficiency (Derdáková et al. 2004; Levin and Ross, 2004). The potential capacity for B. burgdorferi and A. phagocytophilum to be transmitted between ticks co-feeding on the same host irrespective of systemic host infection (co-feeding transmission: Randolph et al. 1996; Levin and Fish, 2000) adds further complexity to the transmission dynamics. Furthermore, relative rates of rodent birth and death rates between nymphal and larval appearance each year very likely affect transmission cycles (Schauber and Ostfeld, 2002).

Together, these observations suggest that (i) the efficiency with which ticks acquire infection from infected hosts, (ii) the duration of host infectivity relative to the timing of tick activity and (iii) the capacity for co-feeding transmission may be particularly crucial as fitness determinants for pathogens transmitted by I. scapularis and other ticks where different instars are seasonally asynchronous in comparison to other vector-borne pathogens. If so, then the evolutionary 'strain space' (Gog and Grenfell, 2002) of I. scapularis-borne microparasite populations may be shaped by abiotic forcings via their influence on tick phenology. Because I. scapularis phenology is mostly temperature-related (Ogden et al. 2004) both the quantity (numbers of infected ticks per unit area, per unit time) and quality (pathogen species and genotypes) of the public health risk posed by *I. scapularis* ticks could be predictable. Here we investigate these hypotheses using a simulation model that combines seasonal life-history events of I. scapularis ticks, P. leucopus rodent hosts, and cycles of pathogen transmission between these two populations.

## MATERIALS AND METHODS

#### Model construction

The model was constructed in STELLA 7.0.3 for Windows software (High Performance Systems Inc. NH). A diagram of the conceptual model is presented as Fig. 1. The model comprised 2 components: (i) a simulation model of I. scapularis populations that provided values for the daily number of infected and uninfected ticks attaching to, and detaching from, hosts in a seasonal cycle representative of conditions in northeastern North America, and (ii) an SIR model of a host for larval and nymphal I. scapularis, and tick-borne microparasites, based on published values for seasonal population processes of *P. leucopus* in northeastern North America. The model was calibrated with data from the field and laboratory so that the phenologies of tick attachment rates to rodents, and annual cycles of rodent abundance, approximated to those seen in the field each year. By using laboratory data on P. leucopus infectivity for ticks with different microparasites, we could then investigate how seasonal asynchrony of immature I. scapularis may affect microparasite survival, and thus fitness, in nature.

Ixodes scapularis population model. Rates of interstadial development of I. scapularis are mostly controlled by ambient temperature in northeastern North America, although nymph-to-adult development is likely also controlled by temperatureindependent diapause (Ogden et al. 2004). The model uses site-specific temperature data (while accounting for diapause) to drive simulations of abundance and seasonality of I. scapularis populations at specific geographical locations (for details see Ogden et al. 2005). For this study, the model was modified from that in Ogden et al. (2005) in 2 ways: (i) immature ticks could feed on reservoirincompetent deer as well as reservoir-competent rodents, and (ii) larvae and nymphs could feed on infective or uninfected rodents. The proportion of feeding larvae acquiring infection from the rodent population at any one time was calculated from the proportions of larvae attaching to acutely-infected and carrier mice, and the transmission coefficients from these rodents.

Nearly all simulations were run using tick development times calculated from 1971–2000 temperature normals (Ogden *et al.* 2005) from the Chatham, Ontario meteorological station ( $42^{\circ}23'N$ ,  $82^{\circ}12'W$ ), which is close to an established population of *I. scapularis* (Ogden *et al.* 2005). These data simulate the asynchronous pattern of seasonal activity of immature *I. scapularis* (Ogden *et al.* 2006) typical for northeastern North America (Wilson and Spielman, 1985). For some comparisons, the model was calibrated to simulate hypothetical, more synchronous larval and nymphal activity periods. In this case, tick



Fig. 1. A diagram of the combined *Ixodes scapularis* and SIR *Peromyscus leucopus* rodent models. The bold dotted lines indicate infection transmission between tick and rodent populations. For simplicity, not all flows to indicate mortality, nor linkage of *P. leucopus* abundance to host-finding success of immature ticks, are shown.

mortality rates were adjusted so that peak and total numbers of larvae and nymphs feeding on rodents were lower than when the ticks were asynchronous. This was necessary to be sure that any survival advantage due to synchronous tick activity was not attributable simply to increases in tick abundance overall, which occur due to faster development of ticks in the model (Ogden *et al.* 2006), and would increase tick infestation levels of rodents and affect transmission cycles (see results of sensitivity analyses).

Model parameters and their estimates are presented in Table 1 and model equations are presented in Appendix 1. In all simulations the model was seeded with 1000 questing adults and 100 infected questing nymphs to establish ticks and infection in the model in the first year. The model then took a number of years of tick and pathogen reproduction (with ticks regulated by density-dependent effects) to come to a stable cyclical equilibrium.

Peromyscus leucopus *population model*. Rodent numbers simulated by the rodent population model replaced the constant rodent density in the original *I. scapularis* model (Ogden *et al.* 2005). Male and female rodents in the model each comprised 3 states: (i) juveniles, considered here to equate with

'non-trappable' juveniles still in the nest in field studies, (ii) trappable juveniles/subadults (TJSAs), and (iii) adults. *Peromyscus leucopus* can remain nontrappable juveniles up to 30 days of age, they can become subadults at 42 days, and adults at 56 days (Rintamaa *et al.* 1976; Schug *et al.* 1991). Residence time as a non-trappable juvenile was fixed at 30 days, while TJSAs became adults at a *per capita* daily rate of 1/25 (i.e. a TJSA became an adult after a mean of 25 days). The basic daily *per capita* mortality rate of all TJSAs and adult rodents was 0.012 (Schug *et al.* 1991). Mortality of 'non-trappable' juveniles in the model was accounted for in the litter size of 'litterbearing females' (see below).

The daily *per capita* rate at which 'adult females' became 'pregnant females' was termed the 'breeding proportion'. This rate reflected the winter decline in breeding in *P. leucopus* (Wolff, 1985), being zero on 31 December, rising to unity from 1 April to 30 September, after which the proportion declined again. Rises and falls in the 'breeding proportion' were sigmoid. The 'pregnant females' remained in this state for a mean 28 days (Lewellen and Vessey, 1998) at which point they gave birth (as 'litter-bearing females'). 'Litter-bearing females' remained in this state for 1 day ensuring that they did not give rise to more than 1 litter before returning to the

(The right hand column indicates the source of the value: M, model derived; L, laboratory study; F, field study; A, assumed in the model; A/F, assumed based on field observations. The parameter values and their sources are explained in detail in Ogden *et al.* (2005).)

ELA	Number of egg-laying females (initial value 0)	М
E	Number of eggs (initial value 0)	Μ
HL	Number of hardening larvae (initial value 0)	M
QL FI	Number of questing larvae (initial value $0$ )	M
FL FI	Number of reading larvae (initial value 0)	M
EL Superscripted in	Indicate whether feeding or engorged larvae are feeding or have fed, on	M
<i>nr</i> and <i>d</i>	rodents (acquiring infection or not respectively) or on deer	111
ON	Number of uninfected questing nymphs (initial value 0)	М
$\tilde{O}N^i$	Number of infected questing nymphs (initial value 100)	M
$\tilde{F}N^r$	Number of nymphs feeding on rodents (initial value 0)	М
$FN^d$	Number of nymphs feeding on deer (initial value 0)	М
EN	Number of engorged nymphs (initial value 0)	Μ
QA	Number of questing adults (initial value 1000)	Μ
FA	Number of feeding adult females (initial value 0)	М
EA	Number of engorged adult females (initial value 0)	$\mathbf{M}$
$ELA_{t-y}$	Number of egg-laying adult females at time $t-y$ (initial value 0)	M
$E_{t-q}$	Number of eggs at time $t-q$ (initial value 0)	M
$HL_{t-z}$	Number of hardening larvae at time $t - z$ (initial value 0) <sup>†</sup>	M
$FL_{t-r}$	Number of recorded larges at time $t - r$ (initial value 0)	M
$EL_{t-s}$	Number of feeding pymphs at time $t - u$ (initial value 0)	M
$FN_{t-u}$	Number of engagged numbes at time $t - r$ (initial value 0)	M
$EN_{t-v}$ EA.	Number of feeding adults at time $t = w$ (initial value 0)	M
$EA_{t}$	Number of engaged adults at time $t - x$ (initial value 0) <sup>†</sup>	M
v = -i = x	Time delay for 'oviposition' (1 day)	M
<i>q</i>	Time delay for the pre-eclosion period of eggs (see Ogden et al. 2005)	L
z	Time delay for hardening of larvae (21 days)	F
r	Time delay for the feeding period of larvae (3 days)	L
\$	Time delay for engorged larva to nymph development (see Ogden et al. 2005)	L
u	Time delay for the feeding period of nymphs (5 days)	L
υ	Time delay for engorged nymph to adult development (see Ogden <i>et al.</i> 2005)	L
τυ	Time delay for the feeding period of adult females (10 days)	L
x	Time delay for the pre-oviposition period (see Ogden <i>et al.</i> 2005)	
$\mu_e$	Daily, per capita mortality rate of eggs (0.002)	F
$\mu_{hl}$	Daily, <i>per capita</i> mortality rate of nurdening larvae (0.006)	г F
$\mu_{ql}$	Daily, <i>per capita</i> mortality rate of questing nymphs (0:006)	F
$\mu_{qn}$ $\mu_{aa}$	Daily, <i>per capita</i> mortality rate of questing adults (0.006)	F
$\mu_{el}$	Daily, <i>per capita</i> mortality rate of engorged larvae (0.003)	F
$\mu_{en}$	Daily, <i>per capita</i> mortality rate of engorged nymphs (0.002)	F
$\mu_{en}$	Daily, per capita mortality rate of engorged adults (0.0001)	F
$\mu_{fl}$	Density-dependent, <i>per capita</i> mortality of feeding larvae on rodents $(0.65 + [0.0491, p(\xi1.01 + (EI^{ir} + EI^{ir})]/R)])$	L
$\mu_{fld}$	Density-dependent, <i>per capita</i> mortality of feeding larvae on deer	А
-	$(0.65 + [0.049 \text{Ln}(\{1.01 + (FL^d + FN^d + FA)\}/D)])$	
$\mu_{fn}$	Density-dependent, per capita mortality of nymphs feeding on rodents	L
	$(0.55 + [0.049 \text{Ln}(\{1.01 + (FN^{nr} + FN^{nr})\}/R)])$	
$\mu_{fnd}$	Density-dependent, <i>per capita</i> mortality of nymphs feeding on deer	А
	$(0.55 + [0.049 \text{Ln}(\{1.01 + (FL^a + FN^a + FA)\}/D)])$	Б
$\mu_{fa}$	Density-dependent, <i>per capita</i> mortality of feeding adults $(0.5 + [0.040] + (4.04 + E.4) (D))$	F
D	$(0.5 + [0.049 \text{Ln}(\{1.01 + PA\}/D)])$ Total number of transpla redents (initially 120)	м
D	Number of deer (20)	Δ
D ሰ	Per capita egg production by egg-laying females (3000)	L
$f^{FA}$	Density-dependent reduction in fecundity of egg-laying females	F
5	$(1 - [0.01 + (0.04 \times Ln \{1.01 + FA/D\})])$	-
$ heta^i$	Temperature-variable factor for questing activity of immature ticks	L
	(see Ogden <i>et al.</i> 2005)	
$ heta^a$	Temperature-variable factor for questing activity of adult ticks	L
	(see Ogden et al. 2005)	
$\lambda_{qlir}$	Daily probability that questing larvae attach to an infective rodent and	A/F
	acquire infection $(0.0013(R)^{0.515})(((R_{ai} \times TE_a)/R)) + ((R_{ci} \times TE_c)/R))[+\kappa]^*)$	
$\lambda_{qlnr}$	Daily probability that questing larvae attach to a non-infective rodent or an	A/F
	infected rodent from which they don't acquire infection	
	$(0.0013(R)^{0.010})(1 - (((R_{ai} \times TE_a)/R)) + ((R_{ci} \times TE_c)/R))[+ \kappa]^*))$	

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$\lambda_{qnr}$	Daily probability that questing nymphs attach to a rodent $(0.002(R)^{0.515})$	A/F
$\lambda_{qld}$	Daily probability that questing larvae attach to a deer $(0.0013(D)^{0.515})$	A/F
$\lambda_{and}$	Daily probability that questing nymphs attach to a deer $(0.002(D)^{0.515})$	A/F
$\lambda_{aa}$	Daily host finding probability for questing adults $(0.086(D)^{0.515})$	A/F
$TE_a$	Pathogen transmission efficiency to larvae from acutely-infected rodents	L
$TE_c$	Pathogen transmission efficiency to larvae from 'carrier' rodents	L

\*  $\kappa$  the 'co-feeding proportion' was only included for certain simulations (see Materials and Methods section). † When these variables appear on the right hand side of equations they represent survivors of those individuals that entered that state at time t-x.

'adult female' state. Females returned to the adult female state immediately after giving birth: there is little evidence of lactational anoestrus in *P. leucopus* (Lewellen and Vessey, 1998).

For simplicity, in most simulations it was assumed that there was no midsummer hiatus in breeding (Rintamaa et al. 1976), i.e. the model represented more northern populations of P. leucopus (Millar and Gyug, 1981). An index of habitat carrying capacity (K) simulated reduced 'food supply' through autumn to early spring (1 September through to 1 April), i.e. the simulations assumed no 'mast years' occurred, which could increase rather than decrease winter/ spring survival (Jones et al. 1998). K could alter a number of the model variables simultaneously. The 'breeding proportion' and the numbers of rodents per litter declined with reduced K (Rintamaa et al. 1976; Nadeau et al. 1981; Wolff, 1985; Schug et al. 1991), while the daily *per capita* mortality rate of all rodents increased inversely with K (Linzey and Kesner, 1991; Schug et al. 1991) (Table 2).

The *P. leucopus* population in the model was regulated by density-dependent effects on reproduction (as suggested by analysis of field data: Lewellen and Vessey, 1998), by reducing the 'breeding proportion', and the numbers of rodents born and surviving to be trappable (see Table 2).

Empirical validation and sensitivity analyses were re-run using 2 variants of the model. In the first variant, we included a midsummer hiatus in P. leucopus breeding: a physiological cessation of male and female reproductive activity due to unknown cues (Terman and Terman, 1999). Where this occurs in northeastern USA, it typically does so in July and early August (Rintamaa et al. 1976), and to model its potential effects, the 'breeding proportion' in the model was reduced to zero from mid-July to mid-August. To compensate for an overall reduced abundance of rodents (which could affect both tick and microparasite abundance and invalidate comparisons amongst model variants), the basic mortality rate was reduced from 0.012 to 0.0115. In the second variant, a more complex seasonal pattern of rodent mortality as suggested by Schug et al. (1991) was introduced. In this version, adult rodent mortality in winter was unaffected by K but adult female mortality increased in spring and summer associated with intraspecific competition associated with breeding. To achieve this, adult female mortality was increased by one four hundredth of the breeding proportion, and this also necessitated a slight decrease in the basic rate of mortality to obtain rodent numbers that were comparable amongst model variants.

Model parameters and their estimates are presented in Table 2 and model equations are presented in Appendix 2. All versions of the model were initially seeded with 60 non-pregnant adult females and 60 adult males. Ten of each of these were in the acuteinfected class to seed infection in the model (see below). Although the model does not explicitly have a spatial dimension, the rodent numbers were scaled to those typically captured in 10-20 ha grids in the northern part of the rodent's range (Harland et al. 1979; Nadeau et al. 1981), and deer densities were scaled high (equivalent to 1-2 per ha in comparison to rodent numbers, where 1-2 per hectare is considered a high natural density for whitetailed deer: Kilpatrick et al. 2001) to account for the absence of other hosts for adult and immature ticks.

Modelling infection in rodent and tick populations. All states in the rodent population could acquire infection except juveniles and 'litter-bearing' females. Non-trappable juveniles confined to the nest are unlikely to acquire ticks (Hofmeister et al. 1999), and litter-bearing females were in that state for 1 day only. Tick-to-rodent transmission efficiency was set at 100%. The per capita daily rate at which naïve mice became 'acutely-infected' mice was then the number of infected questing nymphs that attached to a rodent on that day. The daily per capita rate at which 'acutely-infected' mice recovered was 1.3/Infection Duration, where duration of acute infections in rodents was approximated from laboratory studies (Table 3). This relationship was designed to capture some of the variation in transmission efficiency during the acute infection period (Derdáková et al. 2004; Levin and Ross, 2004). Our examples are simplifications, and do not cover the full gamut of possible values for duration of host infection and transmission efficiency, and variations in transmission efficiency

(The	right	hand	column	indicates	the sou	rce of	the	value:	М,	model	derived;	L,	laboratory	study;	F,	field	study;
A, as	sumed	in the	e model;	A/F, assu	med bas	ed on	field	observ	ration	ns; A/L	, assume	d ba	ised on labo	oratory	obse	ervati	ons.)

RTotal number of trappable rodents (initial value 120) $R_{ai}$ Total number of acutely-infected rodents (initial values 0) $R_{ci}$ Total number of rodents with carrier infections (initial value 0) $AM$ The number of uninfected adult males (initial value 50) $SAM$ The number of non-trappable juvenile/sub-adult males (initial value 0) $JM$ The number of uninfected trappable juvenile/sub-adult females (initial value 0) $JK$ The number of uninfected trappable juvenile/sub-adult females (initial value 0) $JF$ The number of uninfected pregnant females (initial value 0) $JF$ The number of uninfected pregnant females (initial value 0) $JF$ The number of uninfected value pregnant females (initial value 0) $JF$ The number of uninfected pregnant females (initial value 0) $JF$ The number of uninfected inter-bearing' females (initial value 0) $Superscript i$ Indicates rodents with carrier infectionsSuperscript cIndicates rodents with carrier infectionsSubscriptThe number of rodents in that state at 1 or 30 days before the present day $t-1$ or $t-30$ $\beta$ Per capita daily rate trappable juvenile/sub-adults become adults (1/25) $\varpi$ Per capita daily rate trappable juvenile/sub-adults become adults (1/25) $\varpi$ Per capita daily rate at which pregnant females became 'litter-bearing' females (1/20) $\xi$ Density-dependent effect on breeding and birth rates (1 $-(0.09 \times Ln(1.01 + R))$ ) $\chi$ Density-dependent effect on breeding and birth rates (1 $-(0.09 \times Ln(1.01 + R))$ ) $\chi$ Per capita daily rate at which a			
$R_{ai}$ Total number of acutely-infected rodents (initial values 0) $R_{ci}$ Total number of rodents with carrier infections (initial value 0) $AM$ The number of uninfected adult males (initial value 50) $SAM$ The number of non-trappable juvenile/sub-adult males (initial value 0) $JM$ The number of uninfected trappable juvenile/sub-adult males (initial value 0) $JM$ The number of non-trappable juvenile/sub-adult females (initial value 0) $JF$ The number of uninfected trappable juvenile/sub-adult females (initial value 0) $JF$ The number of uninfected pregnant females (initial value 0)† $PF$ The number of uninfected 'litter-bearing' females (initial value 0)† $Superscript i$ Indicates rodents that are acutely infected (starting value 0 except 10 infected adults of each sex)Superscript cIndicates rodents with carrier infectionsSubscriptThe number of rodents in that state at 1 or 30 days before the present day $t-1$ or $t-30$ $\beta$ Per capita daily rate trappable juvenile/sub-adults become adults (1/25) $\varpi$ Per capita daily rate trappable juvenile/sub-adults become adults (1/20) $\chi$ Density-dependent effect on breeding and birth rates (1-(0:09 × Ln(1:01 + R))) $l-K$ Winter effect on 'carrying capacity' ( $K=1$ from 1st April to 1st September, $0:092$ at other times) $\gamma$ Per capita daily rate at which acutely-infected rodents become persistently-infected rodent (1:3/Infection Duration) $\mu_r$ Daily, per capita mortality rate of all trappable rodents (0:012). For all states, the dail		Total number of trappable rodents (initial value 120)	М
$R_{ci}$ Total number of rodents with carrier infections (initial value 0) $AM$ The number of uninfected adult males (initial value 50) $SAM$ The number of uninfected trappable juvenile/sub-adult males (initial value 0) $JM$ The number of uninfected trappable juvenile/sub-adult males (initial value 0) $JM$ The number of uninfected trappable juvenile/sub-adult females (initial value 0) $SAF$ The number of non-trappable juvenile/sub-adult females (initial value 0) $JF$ The number of non-trappable juvenile/sub-adult females (initial value 0) $JF$ The number of uninfected pregnant females (initial value 0) $Superscript i$ Indicates rodents that are acutely infected (starting value 0 except 10 infected adults of each sex)Superscript cIndicates rodents with carrier infectionsSubscriptThe breeding proportion: the <i>per capita</i> daily rate at which adult females became pregnant females, which reduced by $40 \times (1-K)$ , in autumn and was zero in winter.gPer capita daily rate trappable juvenile/sub-adults become adults (1/25) $\varpi$ Per capita daily rate trappable juveniles/sub-adults become adults (1/25) $\varphi$ Per capita daily rate trappable juveniles/sub-adults become presistently. $\chi$ Density-dependent effect on breeding and birth rates $(1-(0.09 \times Ln(1.01+R))$ ) $I-K$ Winter effect on 'carrying capacity' ( $K=1$ from 1st April to 1st September, 0.0992 at other times) $\gamma$ Per capita daily rate at which acutely-infected rodents become persistently-infected rodents (1.3/Infection Duration) $\mu_r$ Daily, per capita mortality rate of all trappable rodents (0.012). Fo	ai	Total number of acutely-infected rodents (initial values 0)	Μ
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per capita mortality rate increased in winter by $(1-K)/2$	r	Daily, <i>per capita</i> mortality rate of all trappable rodents (0.012). For all states, the daily per capita mortality rate increased in winter by $(1 - K)/2$	F
$\lambda i$ Daily <i>per capita</i> rate at which rodents acquired an infected nymphal tick ( $\lambda_{qn} \mathbf{r} \times QN^i$ )		Daily <i>per capita</i> rate at which rodents acquired an infected nymphal tick $(\lambda_{qn}\mathbf{r} \times QN^i)$	М

<sup>†</sup> When these variables appear on the right hand side of equations they represent survivors of those individuals that entered that state at time t-x.

over time post-infection that may occur in nature (Burgdorfer and Schwan, 1991; Derdáková et al. 2004). All recovered mice became 'carrier' mice although 'carrier' mice could also be completely 'recovered/immune' mice by setting the transmission efficiency from these mice (see below) to zero. To simulate life-long 'acute' infections in some Borrelia burgdorferi strains, infection duration was raised higher than the maximum rodent life-expectancy (>1000 days). There was no additional rodent mortality associated with infection in the model (Hofmeister et al. 1999; Bunikis et al. 2004) except in some sensitivity analyses. Four different 'pathogens' were simulated: A. phagocytophilum and B. burgdorferi strains BL206 and B348 from northeastern USA, and LI-231 from Ontario, Canada. Simulations of the latter were used in empirical validation only. BL206 is transmitted from P. leucopus to ticks life-long with high efficiency (Donahue et al. 1987; Derdáková et al. 2004), while strains B348 and LI-231 are efficiently transmitted for a short period, although recovered rodents may remain 'carriers' (Lindsay et al. 1997; Derdáková et al. 2004) (Table 3). For A. phagocytophilum and B. burgdorferi B348 and LI-231, the decline in transmission

efficiency from acute to carrier was exponential (Table 2). Recovered rodents or 'carriers' of *A. phagocytophilum* and *B. burgdorferi* B348 and LI-231 could not revert to the acute-infected status by re-infection (Stafford *et al.* 1999; Derdáková *et al.* 2004). The proportion of larvae acquiring infection from the rodent population at any one time was calculated as:

$$\begin{pmatrix} \frac{\text{TE acute} - \text{infected rodents} \times R_{ai}}{R} \\ + \left( \frac{\text{TE carrier rodents} \times R_{ci}}{R} \right)$$

where TE is the efficiency of transmission from host-to-larva,  $R_{ai}$  and  $R_{ci}$  are the numbers of acutely infected and carrier rodents and R is the total number of trappable and infectable rodents.

To investigate how co-feeding transmission may contribute to transmission cycles, in some simulations we included a 'co-feeding proportion' in the calculation of the proportion of larvae acquiring infection from the rodent population at any one time. The cofeeding proportion' ( $\kappa$  in Table 1) was calculated as 0.67\*Ln(T+1.001) (where T is the instantaneous Table 3. Infection and transmission characteristics of the tick-borne pathogens used in model simulations, and the studies from which these values were approximated

(\* Transmission cycles died out in simulations using these values and only values obtained by Levin and Ross (2004) are considered in the results.)

Pathogen		Transmission efficien		
	Duration of acute host infection (days)	Acute-infected rodents	'Carrier' rodents	Reference
A. phagocytophilum	14	40%	2.5%	Levin and Ross (2004)
A. phagocytophilum	14	25%	2.5%	Massung et al. $(2004)^*$
B. burgdorferi B348	14	75%	2.5%	Derdáková et al. (2004)
B. burgdorferi LI-231	14	60%	2%	Lindsay et al. (1997)
B. burgdorferi BL206	Life-long	60%	NA	Donahue <i>et al.</i> 1987), Derdáková <i>et al.</i> (2004)



Fig. 2. Monthly variations in the numbers of 'trappable' *Peromyscus leucopus* at model equilibrium (A), compared against field observations in northeastern USA (Nadeau *et al.* 1981) (B). Field observations are mean monthly values (+/- maximum and minimum over 5 years) of the minimum numbers of *P. leucopus* known alive (MNKA). Also shown are simulated monthly variations in *P. leucopus* numbers when the model included a mid-summer hiatus in rodent breeding (C) and when adult rodent mortality was set higher in spring and summer than in winter (D).

number of infective nymphs attached per rodent) thus an additional rodent-to-larva transmission coefficient was accorded to all acutely infected and 'carrier' rodents that was 'tick infestation intensity dependent' rising from 6% when rodents carried 1 nymph, to a potential maximum of 84% were rodents to carry 5 nymphs, of which 2 may be infected in the most efficient of simulated transmission cycles. This relationship was used in order to give values of transmission efficiency observed in field and laboratory studies and attributed to co-feeding transmission (Gern and Rais, 1996; Ogden *et al.* 1997, 2003; Richter *et al.* 2002; Derdáková *et al.* 2004). In 3 of these studies there was evidence for density dependence in transmission: uninfected larvae were more likely to co-feed with an infective nymph (or uninfected nymph with infected adult) the higher was the number of infected ticks feeding on the host (Ogden *et al.* 1997; Richter *et al.* 2002; Ogden *et al.* 2003). The total combined proportion of feeding larvae acquiring infection from rodents via systemic infections and co-feeding transmission was constrained to a maximum 0.99 by the IF, AND, ELSE logic of STELLA.

In all simulations, the model was seeded with infected nymphs (see description of I. scapularis population model), and with 10 infected adult female and 10 infected adult male mice (see description of P. leucopus model), and the simulation length was 40 years.

#### Empirical validation

A number of values at model equilibrium were compared against field observations: (i) seasonal variations in numbers of 'trappable' rodents, (ii) seasonal variations in immature tick infestations of rodents, (iii) questing nymph infection prevalence, and (iv) seasonal variation in rodent infection prevalence. For the latter, simulations of *B. burgdorferi* strain BL206 were compared with observations from 2 field studies in Connecticut, USA (Anderson et al. 1987; Bunikis et al. 2004). In the study of Bunikis et al. (2004) the dominant genotypes were those related to B. burgdorferi BL206 (Tsao et al. 2004). A period between infection and seroconversion of 2.5 weeks was accounted for where infections were detected serologically (Schwan et al. 1989). Simulations of B. burgdorferi strain LI-231 were compared with observations at the site (Long Point, Ontario) where the isolate in transmission studies was obtained (Lindsay et al. 1997). All of the simulations were run with and without the 'co-feeding proportion'.

# Local sensitivity analyses

A comparative index (Keeling and Gilligan, 2000) was used to test the sensitivity of the 3 model domains (rodent population, tick population and pathogen transmission) to individual model variables:

$$S = \frac{Log_{10} \frac{T_i}{T_o}}{Log_{10} \frac{V_i}{V_o}}$$

where  $T_o$  is the outcome parameter at equilibrium using starting values for all variables (see Table 1), and  $T_i$  is the outcome parameter, at equilibrium, when the variable under investigation V is increased by a small amount (5%), from its starting value  $V_o$ , to  $V_i$ .

Five outcome parameters were measured: (i) annual peak rodent numbers, (ii) annual peak questing nymph numbers, (iii) annual mean infection prevalence in questing nymphs, (iv) annual mean infection prevalence in rodents, and (v) 'risk' of human infection (being the product of peak questing nymph numbers and infection prevalence). We tested the sensitivity of these outcomes to 5% changes in rodent population parameters (density-dependent effects, mortality and reproduction rates and fecundity), tick population parameters (mortality and host finding rates) and deer numbers. For brevity, sensitivity analyses were not performed for *B. burg-dorferi* strain LI-231, and the 'co-feeding proportion' was not included.

# Global sensitivity analyses

We assessed the global sensitivity of simulated microparasite transmission cycles to the degree of seasonal synchrony of immature ticks and to the inclusion of



Fig. 3. The seasonal variation in monthly nymphal and larval *Ixodes scapularis* infestations of mice at model equilibrium expressed as a proportion of the total annual numbers infesting the mice. In (A) the model simulated the classical immature tick seasonality in northeastern North America. The model in (B), calibrated to produce a hypothetical synchronous pattern of immature tick activity, was used in comparisons.

co-feeding transmission. Simulations were run with and without the co-feeding proportion, and when the simulated seasonal activities of larval and nymphal I. scapularis were synchronous or asynchronous (see Fig. 3). Four analyses were performed. First, we estimated the minimum values for the duration of acute infection, below which deterministic die-out of microparasites occurred, for microparasites transmitted with 40%, 60% or 75% efficiency from acuteinfected hosts to ticks. These values were obtained when transmission efficiency from 'carrier' animals was 2.5% or 0% (i.e. infected animals recovered completely after the acute phase of infection). Second, we estimated the minimum transmission efficiency from acutely infected animals, below which deterministic die-out of the microparasites occurred, when the duration of the acute phase was set at 14 days, and the transmission efficiency from 'carrier' animals was either 2.5% or 0%. Third, we estimated the increase in mortality of acutely infected rodents needed to cause deterministic die-out of B. burgdorferi B348. Fourth, the degree of (i) increase in mortality rates of non-feeding ticks of all stages, (ii) increase in the basic rodent mortality rate, and (iii) decrease in transmission efficiency from 'carrier' animals to larvae (for A. phagocytophilum and B. burgdorferi B348) required for deterministic die out of infection were recorded for each pathogen.

# Interplay of rodent and deer host densities

We investigated the susceptibility of each pathogen to the 'dilution effect' of increasing densities of



Fig. 4. Mean monthly prevalence of infection in questing nymphs for each pathogen at model equilibrium, obtained with and without co-feeding transmission.

reservoir-incompetent deer relative to reservoircompetent rodents by plotting how threshold densities of rodents for pathogen survival varied with different deer densities ('joint threshold curves'; Norman et al. 1999). Equilibrium rodent numbers were reduced stepwise by increasing the basic rodent mortality rate, and at each step multiple simulations were run with deer numbers varying from zero to 1000. At each step, the annual maximum number of rodents was recorded as were the deer numbers at which deterministic die-out of the ticks and/or the pathogen occurred. Threshold deer numbers were then plotted against the corresponding number of rodents. The process was repeated to produce a joint threshold curve for each B. burgdorferi strains BL206 and B348, and A. phagocytophilum. A joint threshold curve was also created for a hypothetical pathogen, which had the transmission characteristics of B. burgdorferi B348 but a longer 28-day duration of acute infection. The curve for A. phagocytophilum was repeated using more synchronous seasonal larval and nymphal I. scapularis activity.

# RESULTS

Simulated tick and rodent populations reached a stable cyclical equilibrium within 10 years. Transmission cycles of tick-borne pathogens reached stable cyclical equilibria within 15 years. In the absence of simulated co-feeding transmission, *A. phagocytophilum* infection died out when the transmission coefficient from acutely infected rodents to larvae was set at 25%, so results of simulations using the higher transmission efficiency value of 40% are presented. The model reached the same equilibria irrespective of the way in which it was initially seeded with ticks, rodents and infection, providing the seeding methods permitted survival for the first years.

### Empirical validation

The *P. leucopus* population model obtained a stable, cyclical equilibrium with the seasonal variations in juvenile/subadult, adult and total rodent numbers observed in the field in northeastern North America (Harland *et al.* 1979; Nadeau *et al.* 1981; Yunger, 2002; Fig. 2). A similar pattern was observed under 2 different scenarios of seasonal rodent mortality and reproduction (Fig. 2).

The peak mean monthly nymph infestation of rodents in simulations was 5 nymphs per rodent (in June, Fig. 3A), comparable with the 2–8 nymphs per *P. leucopus* observed in the field (Wilson and Spielman 1985; Lindsay *et al.* 1999; Schmidt *et al.* 1999; LoGiudice *et al.* 2003). Peak mean monthly larval infestations were 61 per rodent in August (Fig. 3A). Peak infestations of 30–40 per rodent are normal in the field (Wilson and Spielman 1985; Lindsay *et al.* 1999; Schmidt *et al.* 1985; Lindsay *et al.* 1999; Schmidt *et al.* 1985; Lindsay *et al.* 1999; Schmidt *et al.* 1999), but can reach >100 (Levin *et al.* 1999; LoGiudice *et al.* 2003).

When transmission cycles of 4 tick-borne pathogen species or strains with different characteristics of transmission from the host (Table 3) were simulated, infection prevalence in questing nymphs was stable through the year (Fig. 4) and comparable with field studies (Table 4).

In simulations of *B. burgdorferi* strain BL206, seasonal prevalence of infection in rodents was similar to that observed in longitudinal studies in Connecticut (Anderson *et al.* 1987; Bunikis *et al.* 2004; Fig. 5), and cross-sectional studies elsewhere in northeastern USA (Levine *et al.* 1985; Mather *et al.* 1989). In simulations of *B. burgdorferi* strain LI-231 and *A. phagocytophilum*, the prevalence of infective rodents was much lower, and the seasonal prevalence of *B. burgdorferi* LI-231 infection in rodents was similar to that observed in the field (Lindsay *et al.* 1997) (Fig. 5). These seasonal patterns were consistent under 2 different scenarios

Table 4. The mean annual prevalence of infection in questing nymphal ticks at model equilibrium alongside comparable estimates obtained in field studies

		Simulated NIP			Observed NIP			
Pathogen/strain in simulations	TE	No co- feeding	With co- feeding	Prevalence	State/Province	Strain	Reference	
A. phagocytophilum	25 40	0 2·0%	6·0% 9·0%	1.5% 1.9% 8.5–16.4% 10.2%	Connecticut New York New York Wisconsin	Unknown Unknown Unknown Unknown	Levin <i>et al.</i> (1999) Adelson <i>et al.</i> (2004) Daniels <i>et al.</i> (1998) Pancholi <i>et al.</i> (1995)	
B. burgdorferi LI-231 B. burgdorferi B348	60 75	4·1% 5·8%	12·5% 15·8%	17·0% 17·0%	Ontario Ontario	LI-231 LI-231	Lindsay <i>et al</i> . (1997) Lindsay <i>et al</i> . (1997)	
B. burgdorferi BL206	60	25.7%	44.7%	18.6-38.6% 31.7-32.9% 32.5-38.6% up to 75%	New York Connecticut Connecticut New York	Unknown Unknown Mixed* Unknown	Daniels <i>et al.</i> (1998) Levin <i>et al.</i> (1999) Tsao <i>et al.</i> (2004) LoGiudice <i>et al.</i> (2003)	

(NIP, nymphal infection prevalence; TE, host-to-tick transmission efficiency from acutely-infected hosts (%).)

\* Included genotypes related to B. burgdorferi strains BL206 (which predominated) and B348.

of seasonal rodent mortality and reproduction (Fig. 5). Incorporating co-feeding transmission did not alter the seasonal patterns but increased the prevalence of rodents infective for *B. burgdorferi* BL206 by 5% throughout the year, and almost doubled peak prevalence of infection with *A. phagocytophilum* and *B. burgdorferi* LI-231.

# Local sensitivity analyses

Rodent numbers were sensitive to rodent mortality and reproduction rates. Questing nymph abundance was sensitive to off-host tick mortality, host finding rates, deer abundance, and variables that altered rodent abundance (Fig. 6).

Infection prevalence in questing nymph and rodents, and 'risk' (the product of peak questing nymph numbers and mean infection prevalence and an index of the risk of human infection) were each sensitive to rates of tick and rodent mortality, and of rodent reproduction. The direction of changes in questing nymph and rodent infection prevalence, and 'risk' were consistent amongst the tick-borne pathogens, except that small increases in deer numbers increased A. phagocytophilum prevalence in ticks and rodents (i.e. 'rescued' the transmission cycles), but reduced B. burgdorferi prevalence in questing nymphal ticks (Fig. 6). Except for infected rodent mortality rates, to which B. burgdorferi BL206 was the most sensitive, prevalence and 'risk' values for A. phagocytophilum were an order of magnitude more sensitive to all variables than those for the B. burgdorferi strains, and B348 was the more sensitive of the 2 B. burgdorferi strains. The pattern of model sensitivity was similar under 2 different scenarios of seasonal rodent mortality and reproduction, although increased summer mortality of adult rodents reduced the overall sensitivity of infection parameters to changes in rodent and tick abundance (Fig. 6).

#### Global sensitivity analyses

The duration of acute infection in the host required to prevent deterministic die out was always higher (by between 23 and 50%) when seasonal activity of immature *I. scapularis* was asynchronous rather than synchronous (Fig. 3B, Table 5). When the duration of acute infection was set at 14 days and transmission efficiency from carrier rodents to ticks was 2.5%, the minimum transmission efficiency to ticks from acuteinfected hosts was 22% when immature ticks were synchronous and 29% when they were asynchronous. When the transmission efficiency from carrier rodents to ticks was set at 0%, the minimum transmission efficiency to ticks from acute-infected hosts was 32% when immature ticks were synchronous and 45% when they were asynchronous.

When immature tick activity was synchronous, *B. burgdorferi* B348 died out if the mortality rate of acute-infected rodents was increased 15-fold, but when the ticks were asynchronous this microparasite died out if acute-infected rodent mortality was increased 9-fold.

When co-feeding transmission was included in the models, transmission cycles could be maintained in the absence of systemic host infections (i.e. when host-to-tick transmission efficiency from acuteinfected and carrier animals was set to zero) provided that tick abundance did not fall below the levels obtained by increasing tick mortality as described in Table 6.

*B. burgdorferi* BL206 was the most resistant, and *A. phagocytophilum* the least resistant to deterministic die out due to increases in tick and rodent mortality rates (Table 6). These differences were less



Fig. 5. The monthly variations in rodent infection prevalence with Borrelia burgdorferi BL206 (solid line with filled triangles), B. burgdorferi LI-231 (broken line with filled squares), and A. phagocytophilum (broken line with filled circles), predicted by the model at equilibrium without effects of co-feeding transmission. Also shown are field observations of B. burgdorferi infection prevalence in Peromyscus leucopus in studies in Connecticut, USA (open circles [mean values across 2 years and sites: Anderson et al. 1987] and crosses [mean values across 2 years: Bunikis et al. 2004]) and Ontario, Canada (open squares [Lindsay et al. 1997]). Vertical bars indicate the range of values obtained at different observations (for the field studies in Connecticut), or 95% confidence intervals (for the field study in Ontario). P. leucopus mortality and reproduction parameters were at their most simple in (A). In (B) the model included a mid-summer hiatus in rodent breeding, and in (C) adult rodent mortality was higher in spring and summer than in winter.

marked when the seasonal activity periods for larval and nymphal *I. scapularis* were more synchronous (Table 6). Co-feeding transmission increased resistance to die-out, particularly for *A. phagocytophilum*  and *B. burgdorferi* B348. In all cases microparasite die-out preceded die-out of ticks and rodents. *A. phagocytophilum* died out unless recovered rodents became 'carriers' and at least  $1\cdot15\%$  of larvae acquired infection when feeding on these rodents, but 'carriers' were unnecessary if co-feeding transmission was included. Carriers were also unnecessary to maintain *B. burgdorferi* B348, but their absence reduced mean annual questing nymph and rodent infection prevalence by 20% and 14%, respectively. When immature tick seasonal activity was set to be synchronous, transmission from carriers was not necessary to maintain *A. phagocytophilum* or *B. burgdorferi* strain B348, and had little effect on infection prevalence in ticks and rodents.

#### Interplay of rodent and deer host densities

When rodent numbers were low, increasing numbers of reservoir-incompetent deer could permit maintenance of transmission cycles by increasing tick abundance (transmission cycle 'rescue': Norman et al. 1999, Fig. 7). As rodent numbers declined below a certain threshold the numbers of deer required to 'rescue' the transmission cycles increased exponentially. This threshold was inversely related to the transmission efficiency from acutely-infected hosts to larvae, i.e. the 'elbow' of the joint threshold curves in Fig. 7 moved to the left as transmission efficiency increased. For A. phagocytophilum and B. burgdorferi B348, high as well as low deer numbers could cause pathogens to die out, i.e. at high deer densities a 'dilution effect' occurred for these pathogens (as in Norman et al. 1999, Fig. 7). The numbers of deer needed to obtain a 'dilution effect' was lower for A. phagocytophilum than for B. burgdorferi B348, but numbers of deer sufficient to dilute transmission cycles of B. burgdorferi BL206 (>2000) were not reached in the simulations. A hypothetical pathogen, with transmission characteristics of B. burgdorferi B348 but a longer duration of acute infection, also did not suffer a 'dilution effect' with the range of deer numbers tested. Therefore, susceptibility to the 'dilution effect' varied with both the duration of acute infection, and acute phase host-to-tick transmission efficiency (Fig. 7). When seasonal nymphal and larval activity was more synchronous, higher deer numbers were needed to obtain a dilution effect for A. phagocytophilum (Fig. 7).

#### DISCUSSION

We have developed a model that simulates a seasonal pattern of rodent demography, tick vector abundance and attachment rates, and infection prevalence in rodents and questing ticks, which approximate the situation in northeastern North America. We used this system to compare the consequences of reductions in host and tick abundance on, and



Fig. 6. The sensitivity of model equilibrium parameter values for (left to right) (i) annual maximum rodent and tick numbers, (ii) mean annual infection prevalence in questing nymphal ticks, (iii) mean annual infection prevalence in rodents, and (iv) infection 'risk' (the product of mean annual prevalence in questing nymphal ticks, and maximum numbers of questing nymphs), to 5% increases in the variables on the left hand side of the figure. DD rodents: density dependent regulation of rodent breeding. *Peromyscus leucopus* mortality and reproduction parameters were at their most simple in (A). In (B) the model included a mid-summer hiatus in rodent breeding, and in (C) adult rodent mortality was higher in spring and summer than in winter.

limits of host-to-tick transmission characteristics for, the survival of different strains and species of *I. scapularis*-borne bacteria. We have then compared results obtained when larval and nymphal ticks were asynchronous and synchronous. Sensitivity analyses demonstrated the interrelatedness of rodent, tick and microparasite abundance in terms of both the ecology of the system, and the public health risk that may arise. This underlines the need to model how variations in the host community Table 5. The minimum duration of acute infection in hosts (in days), below which deterministic die out occurred, for a range of values for transmission efficiency to ticks from acute-infected and carrier hosts

(These values are	compared for s	simulations run	using sync	hronous an	id asynchronous	s patterns of sea	asonal activity	of larval
and nymphal Ixoa	les scapularis.)							

Transmission efficiency (%) from:		Minimum duration of acute infection needed for microparasite persistence					
Acute-infected hosts	Carrier hosts	Synchronous nymphs and larvae	Asynchronous nymphs and larvae	Increase due to asynchrony (%)			
40	2.5	7	10	43			
40	0	12	17	42			
60	2.5	4	6	50			
60	0	7	10	43			
75	2.5	4	5	25			
75	0	6.5	8	23			

Table 6. A comparison of the percentage increase in mortality rates of non-feeding ticks, and the basic mortality rate of rodents, required to cause deterministic die out of the different pathogens, and *Ixodes scapularis* and *Peromyscus leucopus* populations

(Figures in parentheses are values obtained using a model with coincident seasonal activity of nymphal and larval *I. scapularis.*)

	Increase in non-fe	eding tick mortality	Increase in the basic mortality rate of rodents			
	No co-feeding	With co-feeding	No co-feeding	With co-feeding		
A. phagocytophilum	5% (14%)	26%	8% (12%)	19%		
B. burgdorferi B348	14% (25%)	26%	16% (21%)	25%		
B. burgdorferi BL206	34% (41%)	39%	33% (33%)	37 %		
I. scapularis	45% (66%)	45%	NA	NA		
P. leucopus	NA	NA	42% (42%)	42 %		

simultaneously affect microparasite survival directly by varying densities of competent reservoir species, and indirectly by affecting tick vector abundance (Begon, 2006). These also suggest that parameterization of rodent model parameters are important to model outcomes and require further study.

Quantitative limits for characteristics of host infection and host-to-tick infectivity and transmission were obtained from the model under conditions of seasonally asynchronous activity of immature I. scapularis. In the absence of co-feeding transmission, a number of combinations of levels of transmission efficiency from acute-infected and carrier animals, and persistence of acute infection, could permit maintenance of microparasites in the model system. Higher transmission efficiency from acutely infected rodents to ticks and longer duration of acute host infections increased resistance to deterministic dieout due to reduced tick and rodent abundance and, possibly, to the 'dilution effect'. Here, the dilution effect was explored using a theoretical two-host system to compare our model with that of Norman et al. (1999), and produced qualitatively similar results. However, a 'dilution effect' occurred only when numbers of deer were unrealistically high, even though deer are completely reservoir incompetent (in the model and in nature for B. burgdorferi). Further

studies are required, therefore, to more fully and practically investigate under what circumstances, and for what pathogens, the 'dilution effect' may occur using more complex models containing hosts that are considered important dilution hosts in nature (LoGiudice et al. 2003). When immature I. scapularis were seasonally asynchronous rather than synchronous, infections had to persist longer and/or be transmitted with higher efficiency to survive, transmission cycles were much more sensitive to microparasite-induced mortality of rodents, and to the 'dilution effect' caused by a non-reservoir tick host (as defined in Norman et al. 1999), and differences in susceptibility to die-out amongst the pathogens were much more marked. As long as co-feeding transmission is efficient, it may buffer any limitations duration and transmission of systemic host infections may have on microparasite survival, even where ticks are not completely synchronous. However, co-feeding transmission is itself likely to be most efficient when nymphal and larval ticks are synchronous (Randolph et al. 2000).

Seasonal asynchrony of immature *I. scapularis* tick vectors and strong inter-annual fluctuations in *P. leucopus* rodent and *I. scapularis* vector abundance are the norm in nature in northeastern USA (Jones *et al.* 1998). Our model suggests, therefore, that traits



Fig. 7. Joint threshold curves for persistence of ticks and tick-borne pathogens obtained in model simulations under conditions of different deer and rodent host densities. In (A) separate curves are shown for the ticks and each of 4 pathogens: *Borrelia burgdorferi* strains BL206 and B348, *Anaplasma phagocytophilum* and a theoretical pathogen as described in the text. Arrows indicate the sides of the curves on which rodent and deer densities permit persistence of the pathogens. In (B) the curve obtained for *A. phagocytophilum* when larval and nymphal *Ixodes scapularis* were seasonally asynchronous was compared against that obtained when these instars were more synchronous.

permitting one of (i) highly efficient transmission from acutely infected hosts, (ii) longer lived acute or 'carrier' infections in the host, and (iii) efficient transmission amongst co-feeding ticks are essential for emergence and persistence of *I. scapularis*-borne pathogens in northeastern North America.

Persistent, highly transmissible microparasite infections require efficient but costly mechanisms to evade host immunity such as binding of host proteins and down-regulation of immunogenic surface proteins (for *B. burgdorferi* s.l.: Kurtenbach *et al.* 2002; Liang *et al.* 2004; Lederer *et al.* 2005) or antigenic variation (for *A. phagocytophilum*: Barbet *et al.* 2003), which may entail specialization for a host species (Nelson *et al.* 2005). The high mortality often associated with highly efficient host-to-tick transmission in livestock (O'Callaghan *et al.* 1998; Ogden *et al.* 2003) is not seen in *P. leucopus* infected with *B. burgdorferi* (Hofmeister *et al.* 1999; Bunikis *et al.* 2004). By implication, *B. burgdorferi* strain BL206 is more specialized for *P. leucopus* than strain B348 by having an immune-evasion mechanism that is more effective in this host, enhances pathogen survival, yet the greater abundance of the microparasite doesn't increase host mortality (Gilchrist and Sasaki 2002; Alizon and van Baalen, 2005). This raises the hypothesis that seasonal asynchrony of immature *I. scapularis* drives specialization for different host species (multiple niche polymorphism: Levene, 1953).

The dynamics of infection in, and transmission from experimental mice, and the capacity for local dissemination (and thus possibly co-feeding transmission: Ogden *et al.*1997; Richter *et al.* 2002) vary amongst *B. burgdorferi* strains and in part correlate with clinical disease in humans (Liveris *et al.* 2002; Wang *et al.* 2002; Steere *et al.* 2004). Thus, traits that evolve to enhance transmission from natural hosts could affect the severity or type of clinical disease seen in humans.

Our study suggests that the degree of seasonal asynchrony between nymphal I. scapularis infecting hosts, and larvae acquiring infection from hosts sets minimum values for the duration and efficiency of transmission of host infections (or co-feeding transmission) that are consistent with survival of the I. scapularis-borne microparasites. This may in turn drive host specialization amongst populations of I. scapularis-borne microparasites. Thus, abiotic forcings that determine the degree of asynchrony in seasonal tick abundance (day length and climate: Yuval and Spielman, 1990; Ogden et al. 2006) may have important implications for the public health risk from tick-borne zoonoses because: (i) adaptation to different host species may be associated with differences in pathogenicity and clinical disease in humans; and (ii) variations in tick seasonality at different latitudes, and with climate change (Ogden et al. 2006), may result in variation in the geographical range of different species and strains of tick-borne zoonoses. Further modelling and empirical studies are required to specifically investigate effects of host infection dynamics and transmission (related to different species and genotypes), rodent population biology and the dilution effect on transmission cycles and public health risk from tick-borne zoonoses. Our study highlights the importance in general of field and laboratory studies to more fully parameterize and validate models of tick-borne zoonoses transmission, and to investigate the predictions for pathogen evolution and geographical distribution of our modelling studies.

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#### APPENDIX 1

#### Equations of the Ixodes scapularis population model

STELLA calculates changes at four steps per time unit using difference equations, but approximates a differential equation by integration of the difference equation (Peterson and Richmond, 1997). Equations have left-hand-side notation as for a differential equation, except those containing predictions for tick development events, which have a resolution of one day.

1. Rate of change of egg-laying adult females:

$$\frac{\Delta ELA}{\Delta t} = EA_{t-x} - ELA_{t-y}$$

2. Rate of change of number of eggs:

$$\frac{\Delta E}{\Delta t} = ELA * f^{FA} * p - E_{t-q} - \mu_e * E$$

3. Rate of change in the number of hardening larvae:

$$\frac{\Delta HL}{\Delta t} = E_{t-q} - HL_{t-z} - \mu_{hl} * HL$$

4. Rate of change in the number of questing larvae:

$$\frac{dQL}{dt} = HL_{t-z} - (\lambda_{qlir} + \lambda_{qlnr} + \lambda_{qld}) * QL * \theta^{i} - \mu_{ql} * QL$$

5. Rate of change in the number of feeding larvae acquiring infection from rodents:

$$\frac{\Delta FL^{ir}}{\Delta t} = \lambda_{qlir} * QL * \theta^{i} - FL^{ir}_{t-r} - \mu_{fl} * FL^{ir}$$

6. Rate of change in the number of feeding larvae not acquiring infection from rodents:

$$\frac{\Delta FL^{nr}}{\Delta t} = \lambda_{qlnr} * QL * \theta^{i} - FL_{t-r}^{nr} - \mu_{fl} * FL^{nr}$$

7. Rate of change in the number of larvae feeding on deer:

$$\frac{\Delta FL^{d}}{\Delta t} = \lambda_{qld} * QL * \theta^{i} - FL^{d}_{t-r} - \mu_{fl} * FL^{d}$$

8. Rate of change in the number of infected engorged larvae that fed on rodents:

$$\frac{\Delta EL^{ir}}{\Delta t} = FL^{ir}_{t-r} - EL^{ir}_{t-s} - \mu_{el} * EL^{ir}$$

9. Rate of change in the number of uninfected engorged larvae that fed on rodents:

$$\frac{\Delta EL^{nr}}{\Delta t} = FL_{t-r}^{nr} - EL_{t-s}^{nr} - \mu_{el} * EL^{nr}$$

10. Rate of change in the number of engorged larvae that fed on deer:

$$\frac{\Delta EL^d}{\Delta t} = FL^d_{t-r} - EL^d_{t-s} - \mu_{el} * EL^d$$

11. Rate of change in the number of uninfected questing nymphs:

$$\frac{dQN}{dt} = EL_{t-s}^{nr} + EL_{t-s}^{d} - (\lambda_{qnr} + \lambda_{qnd}) * QN * \theta^{i}$$
$$-\mu_{qn} * QN$$

12. Rate of change in the number of infected questing nymphs:

$$\frac{dQN^{i}}{dt} = EL_{t-s}^{ir} - (\lambda_{qnr} + \lambda_{qnd}) * QN^{i} * \theta^{i} - \mu_{qn} * QN^{i}$$

13. Rate of change in the number of nymphs feeding on rodents:

$$\frac{\Delta FN^{r}}{\Delta t} = \lambda_{qnr} * (QN^{i} + QN) * \theta^{i} - FN_{t-u}^{r} - \mu_{fnr} * FN^{r}$$

14. Rate of change in the number of nymphs feeding on deer:

$$\frac{\Delta F N^d}{\Delta t} = \lambda_{qnd} * (QN^i + QN) * \theta^i - FN^d_{t-u} - \mu_{fnd}$$
$$* FN^d$$

15. Rate of change in the number of engorged nymphs:

$$\frac{\Delta EN}{\Delta t} = FN_{t-u}^r + FN_{t-u}^d - EN_{t-v} - \mu_{en} * EN$$

16. Rate of change in the number of questing adults:

$$\frac{dQA}{dt} = EN_{t-v} - \lambda_{qa} * QA * \theta^a - \mu_{qa} * QA$$

17. Rate of change in the number of feeding adults:

$$\frac{\Delta FA}{\Delta t} = \lambda_{qa} * \frac{QA}{2} * \theta^a - FA_{t-w} - \mu_{fa} * FA$$

18. Rate of change in the number of engorged adult females:

$$\frac{\Delta EA}{\Delta t} = FA_{t-w} - EA_{t-x} - \mu_{ea} * EA$$

APPENDIX 2

*Equations of the* Peromyscus leucopus *population model* 

1. Rate of change in the number of uninfected trappable juvenile/sub-adult males:

$$\frac{\Delta SAM}{\Delta t} = \mathcal{J}M_{t-30} - g * SAM - \lambda_i * SAM - \mu_r SAM$$

2. Rate of change in the number of uninfected adult males:

$$\frac{\delta AM}{\delta t} = g * SAM - \mu_r * AM - \lambda_i * AM$$

3. Rate of change in the number of trappable juvenile/sub-adult males with acute infections:

$$\frac{\delta SAM^{i}}{\delta t} = \lambda_{i} * SAM - g * SAM^{i} - \gamma * SAM^{i} - \mu_{r}SAM^{i}$$

4. Rate of change in the number of adult males with acute infections:

$$\frac{\delta AM^{i}}{\delta t} = \lambda_{i} * AM + g * SAM^{i} - \gamma * AM^{i} - \mu_{r} * AM^{i}$$

5. Rate of change in the number of trappable juvenile/sub-adult males with carrier infections:

$$\frac{\delta SAM^{c}}{\delta t} = \gamma * SAM^{i} - g * SAM^{c} - \mu_{r}SAM^{c}$$

6. Rate of change in the number of adult males with carrier infections:

$$\frac{\delta AM^{c}}{\delta t} = g * SAM^{c} + \gamma AM^{i} - \mu_{r} * AM^{c}$$

7. Rate of change in the number of uninfected trappable juvenile/sub-adult females:

$$\frac{\delta SAF}{\delta t} = \mathcal{J}F_{t-30} - g * SAF - \lambda_i SAF - \mu_r SAF$$

8. Rate of change in the number of uninfected adult females:

$$\begin{split} \frac{\delta AF}{\delta t} = &g*SAF + LF_{t-1} - \lambda_i * AF \\ &- (\beta - (40*(1-K)))*\chi * AF - \mu_r * AF \end{split}$$

9. Rate of change in the number of uninfected pregnant females:

$$\frac{\delta PF}{\delta t} = (\beta - (40 * (1 - K))) * \chi * AF - \varpi * PF - \mu_r * PF$$

10. Rate of change in the number of uninfected litter-bearing females:

$$\frac{\Delta LF}{\Delta t} = \varpi * PF - LF_{t-1}$$

11. Rate of change in the number of trappable juvenile/sub-adult females with acute infections:

$$\frac{\delta SAF^{i}}{\delta t} = \lambda_{i} * SAF - g * SAF^{i} - \gamma * SAF^{i} - \mu_{r}SAF^{i}$$

12. Rate of change in the number of adult females with acute infections:

$$\begin{split} & \frac{\delta AF^{i}}{\delta t} = g * SAF^{i} + \lambda_{i} * AF + LF^{i}_{t-1} \\ & -(\beta - (40 * (1 - K))) * \chi * AF^{i} - \gamma * AF^{i} - \mu_{r} * AF^{i} \end{split}$$

13. Rate of change in the number of pregnant females with acute infections:

$$\frac{\delta PF^{i}}{\delta t} = (\beta - (40 * (1 - K))) * \chi * AF^{i} + \lambda_{i} * PF^{i}$$
$$- \varpi * PF^{i} - \gamma * PF^{i} - \mu_{r} * PF^{i}$$

14. Rate of change in the number of litter-bearing females with acute infections:

$$\frac{\Delta LF^{i}}{\Delta t} = \varpi * PF^{i} - LF^{i}_{t-1}$$

15. Rate of change in the number of trappable juvenile/sub-adult females with carrier infections:

$$\frac{\delta SAF^{c}}{\delta t} = \gamma * SAF^{i} - g * SAF^{c} - \mu_{r}SAF^{c}$$

16. Rate of change in the number of adult females with carrier infections:

$$\frac{\delta AF^c}{\delta t} = g * SAF^c + \gamma * AF^i + LF^c_{t-1}$$
$$-(\beta - (40 * (1 - K))) * \chi * AF^c - \mu_r * AF^c$$

17. Rate of change in the number of pregnant females with carrier infections:

$$\frac{\delta PF^{c}}{\delta t} = (\beta - (40 * (1 - K))) * \chi * AF^{c} + \gamma * PF^{i}$$
$$- \varpi * PF^{c} - \mu_{r} * PF^{c}$$

18. Rate of change in the number of litter-bearing females with carrier infections:

$$\frac{\Delta LF^c}{\Delta t} = \varpi * PF^c - LF^c_{t-1}$$

19. Rate of change in the numbers of non-trappable juvenile males:

$$\frac{\delta \mathcal{J}M}{\delta t} = \left( \left( \left( \varepsilon - \left( \left( 1 - K \right) * 300 \right) \right) * \chi \right) / 2 \right) \\ * \left( LF + LF^{i} + LF^{c} \right) - \mathcal{J}M_{t-30} \right)$$

20. Rate of change in the numbers of non-trappable juvenile females:

$$\frac{\delta \mathcal{I}F}{\delta t} = (((\varepsilon - ((1 - K) * 300)) * \chi)/2) \\ * (LF + LF^{i} + LF^{c}) - \mathcal{I}F_{t-30}$$

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