



Dynamics of zonally elongated transient flows

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(Received 1 March 2020; revised 1 September 2020; accepted 21 November 2020)

This study examines the dynamics of zonally elongated transient flows (ZELTs) in the context of quasi-geostrophic turbulence. Unlike stationary zonal jets considered in previous studies, these flow features do not span the entire oceanic basin and propagate in the zonal direction at a speed slower than baroclinic Rossby waves. The analysis of potential vorticity balance in a statistically steady state shows that ZELTs are maintained by the vorticity flux divergences associated with the eddy-eddy interactions whereas the eddy-mean flow interactions play a secondary role. The divergences of the eddy fluxes of barotropic relative vorticity and buoyancy are shown to be the dominant contributors. The importance of specific eddy-eddy interactions are further studied using a dynamical model with the removed eddy-eddy vorticity flux divergences, which is equivalent to the fluid system with an absent cascade of eddy energy. Simulations with this reduced-dynamics model exhibit a complete disappearance of ZELTs, confirming the expectations from the analysis of the vorticity balance. Additional reduced-dynamics simulations demonstrate that the eddy kinetic energy transport leads to the emergence of ZELTs, with the transport in the baroclinic mode playing the leading role, while the potential energy transport acts to damp them.

Key words: baroclinic flows, geostrophic turbulence, quasi-geostrophic flows

1. Introduction

Dominant modes of mesoscale variability at midlatitudes appear as zonally elongated transient flows, or ZELTs (Maximenko, Bang & Sasaki 2005; Rudko *et al.* 2018). Unlike stationary zonal jets, which can be clearly observed in the atmospheres of Jupiter and other gaseous planets, ZELTs have a long, but finite zonal extent, are weaker in magnitude than the background flow field and vary in time. These properties complicate identification

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of ZELTs in oceanic flows, because straightforward low-pass filtering can lead to spurious flow patterns (Schlax & Chelton 2008; Rudko *et al.* 2018). ZELTs explain a significant part of anisotropy in the spatial distribution of the velocity variance (Huang *et al.* 2007; Scott *et al.* 2008; Stewart *et al.* 2015) and Lagrangian particle dispersion (Rypina *et al.* 2012; Kamenkovich, Rypina & Berloff 2015). Because of this inherent anisotropy associated with ZELTs, climate models that cannot reproduce these flow patterns can have large biases in energy and tracer distributions (Kamenkovich *et al.* 2015). Thus, understanding the processes leading to ZELT emergence and equilibration is of particular importance for reliable forecasts of the present and future climates.

Two mechanisms have been proposed to explain the emergence of zonal flows in geophysical turbulence. The first is due to inverse kinetic energy cascade, which occurs as a result of the nonlinear interactions between transient flow anomalies ('eddies'). The energy is deposited to ever longer scales until it reaches the longest available scale. In the geophysical context, meridional variations of the Coriolis parameter (the β -effect) introduce asymmetry into the fluid flow; the flow undergoes anisotropization, and the energy flux is redirected into zonal modes. The anisotropization of energy propagation occurs at the Rhines scale (Rhines 1975), defined by the balance between the nonlinear and β -terms. In fluid systems with imposed small-scale external forcing, there is an additional length scale defined as a cross-over between the Rossby wave spectrum and Kolmogorov–Kraichman spectrum (Vallis & Maltrud 1993). It has been shown that if these two scales are separated widely enough, barotropic turbulence develops an inertial range ('zonostrophic regime') with prominent zonal flows (Huang, Galperin & Sukoriansky 2001; Sukoriansky, Dikovskaya & Galperin 2007).

Dynamics of mesoscale ocean currents involves several additional processes. First, non-uniform stratification of oceanic flows entails the difference in the directions of cascading kinetic and available potential energies (Danilov & Gurarie 2000). To the leading order, the stratification can be represented by the barotropic and first baroclinic modes, with the latter being surface intensified (Pedlosky 2013). Scott & Arbic (2007) shows that, for oceanographically relevant parameters, transport of the baroclinic kinetic energy is 10 times larger than the transport of the barotropic kinetic energy. Second, in order for the flow with the inverse energy cascade to reach an equilibrium, there must be a sink of energy at large scales; the energy is typically removed with large-scale drag, which can effect the width of inertial ranges (Sukoriansky, Galperin & Chekhlov 1999). For example, zonal jets appear as an equilibrated state in simulations of baroclinic turbulence; the equilibrium is achieved as a balance between bottom drag and nonlinear forcing with Reynolds stresses (flux of relative vorticity) supporting jets and form stresses (flux of buoyancy) resisting them (Berloff, Kamenkovich & Pedlosky 2009b). This result is further elaborated by Khatri & Berloff (2018b), who suggest that Reynolds stresses force jets in both layers, while form stress act as a carrier of momentum from the top to the bottom layers. Last, mesoscale flows in the ocean receive the energy either from instability of large-scale currents or from the wind or external heating - the energy is being deposited at the length scales of several Rossby deformation radii, which contradicts the assumptions for the existence of zonostrophic inertial ranges. As inferred from both idealized and full-physics models and satellite data, the inertial ranges in the ocean are narrow or virtually non-existent (Scott & Wang 2005; Scott & Arbic 2007).

The second mechanism of the development of zonal flows involves linear instability of large-scale oceanic currents: the emergence of modes with small zonal wavenumbers that later equilibrate to finite amplitudes in the fully nonlinear regime. These modes can emerge as weakly damped modes but be energized by the triad interactions with the most

unstable mode (Wang *et al.* 2012), or be the most unstable modes on their own – baroclinic instability of the combined zonally uniform vertical shear and a meridional wave (a Fourier mode with a zero meridional wavenumber l = 0) (Berloff, Kamenkovich & Pedlosky 2009*a*). Furthermore, Berloff & Kamenkovich (2013*a*,*b*) demonstrate that under certain conditions spectral properties of fully equilibrated turbulent flow can be ascertained from the linear dynamics. Additionally, Khatri & Berloff (2018*a*, 2019) demonstrate that linear dynamics can explain the meridional drift and an off-zonal tilt of the multiple jets over a uniform topographic slope.

The key difference between the two scenarios is the relative importance of the nonlinear processes. The relevance of these processes can be efficiently estimated in the dynamical systems, which retain only certain types of interactions. Connaughton *et al.* (2010) show that the instability of the meridional wave in the dynamical system with four interacting modes leads to the emergence of zonal or zonally elongated flow patterns depending on the magnitude of the nonlinearity parameter. Similarly, quasi-stationary barotropic zonal jets emerge as a result of instability of the dynamical system, in which only eddy–mean flow interactions are retained (Farrell & Ioannou 2007, 2008; Srinivasan & Young 2012). This latter dynamical system is energetically consistent with the fully nonlinear model in that the net total energy is preserved while the cascade of eddy energy is absent. O'Gorman & Schneider (2007) and Marston, Conover & Schneider (2008) (see also Abramov & Majda 2003) show that, for some values of model parameters, fully nonlinear and reduced-dynamics simulations compare fairly well.

In this manuscript, we examine the dynamics of ZELTs in a two-layer quasi-geostrophic model. The technical details of the model and the examples of its output are provided in § 2. We perform simulations with different parameter values corresponding to an anisotropic flow with well-pronounced ZELTs, an anisotropic flow without ZELTs and an isotropic flow (Rudko *et al.* 2018). In each case, we examine the role of nonlinear processes sustaining the leading modes of mesoscale variability. Additionally, we further explore the relevance of different types of energy transfers leading to the emergence of ZELTs by performing simulations in the reduced-dynamics models.

2. Numerical model

We use a two-layer quasi-geostrophic model (Pedlosky 2013). The governing equations are the conservation of potential vorticity in each layer, augmented with bottom drag and viscosity to remove the energy from large scales and enstrophy from small scales, respectively,

$$\frac{\partial\xi_1}{\partial t} + J(\psi_1, \xi_1) + (\beta + S_1 U) \frac{\partial\psi_1}{\partial x} = -U \frac{\partial\xi_1}{\partial x} + \nu \nabla^4 \psi_1, \qquad (2.1)$$

$$\frac{\partial \xi_2}{\partial t} + J(\psi_2, \xi_2) + (\beta - S_2 U) \frac{\partial \psi_2}{\partial x} = -\gamma \nabla^2 \psi_2 + \nu \nabla^4 \psi_2, \qquad (2.2)$$

where the potential vorticity anomalies are given by

$$\xi_1 = \nabla^2 \psi_1 - S_1(\psi_1 - \psi_2), \xi_2 = \nabla^2 \psi_2 - S_2(\psi_2 - \psi_1),$$
(2.3)

and where ψ_n is the streamfunction in the *n*th layer (n = 1, 2; hereafter, indices 1 and 2 refer to the top and bottom layers, respectively), $J(a, b) = (\partial a/\partial x)(\partial b/\partial y) - (\partial a/\partial y)(\partial b/\partial x)$ is the Jacobian operator, ν is the lateral eddy viscosity and γ is the bottom drag coefficient. The eastward background flow is restricted to the upper layer only, $U_1 = 6 \text{ cm s}^{-1}$ and $U_2 = 0 \text{ cm s}^{-1}$. Such a background flow is subject to baroclinic instability with the most unstable mode occurring at l = 0 ('noodle' mode; Pedlosky (2013)). Although properties of the mesoscale variability generated within a westward background flow can be different (Berloff *et al.* 2009*b*), we restrict this study to the eastward shear only.

The model was integrated in the rectangular domain $(L_x \times L_y, L_y = 3600 \text{ km} \text{ and } L_x = 7200 \text{ km})$. The number of grid points in the zonal and meridional directions are $N_x = 512$ and $N_y = 256$, which gives a resolution of approximately 14 km. The first baroclinic Rossby deformation radius is $R_d = 25$ km, which means that the length scale associated with the most unstable modes is $\sim 7 \times R_d = 175$ km, should fall within the resolvable range. We also carried out some of the simulations with the doubled resolution and confirmed that the results are nearly the same. To confirm that the spatial resolution is sufficient for resolving the most important spatial scales, we repeat our main simulations with a doubled spatial resolution. The spectral characteristics of the flow are verified to be nearly unchanged. The model was integrated from the state of rest to 70 000 days, or approximately 192 years.

We follow the study by Rudko *et al.* (2018) in defining ZELTs as several leading empirical orthogonal functions (EOFs) for which the anisotropic ratio is more than 0.6. The anisotropic ratio $\alpha = (\langle u'^2 \rangle - \langle v'^2 \rangle)/(\langle u'^2 \rangle + \langle v'^2 \rangle)$, where $\langle \rangle$ indicates spatial averaging, ' is the transient flow component with removed zonal mean. In line with Rudko *et al.* (2018), we compute these EOFs as the eigenvectors of the streamfunction covariance matrix. Before computing the EOFs, the zonal and time mean components have been removed from the flow. Such defined flow structures are transient and do not extend across the entire computational domain in the zonal direction. Equivalently, the spectral power (Fourier spectrum) associated with these flow structures at frequency ($\omega = 0$) and wavenumber (k = 0) is zero. This is opposite to zonal jets, which are stationary ($\omega = 0$) and extend entirely across the oceanic basin (k = 0). Rudko *et al.* (2018) show that model solutions are particularly sensitive to variations in β and γ , and identified ranges of values of those parameters that are conducive to ZELT appearance.

For this study, we present the model simulations for three different $\gamma - \beta$ pairs, each corresponding to a distinct flow regime. Note that the parameter dependence was explored earlier by Rudko et al. (2018) and is not repeated here. The ZELT-dominated regime ($\gamma = 3 \times 10^{-7} \text{ s}^{-1}$, $\beta = 2.15 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$), in which the leading empirical orthogonal functions (EOFs) are associated with ZELTs, corresponds to $\alpha \sim 0.8$. The two-dimensional (2-D) wavenumber spectrum contains a well-pronounced peak at small zonal wavenumbers and an area of enhanced power at intermediate zonal wavenumbers (figure 1b). The leading EOF for this case displays prominent ZELTs (figure 1e); the autocorrelation (AC) function of the leading principal component (AC1) exhibits regular oscillations with the slight decay (figure 1h), thereby suggesting that ZELTs are persistent, low-frequency flow patterns. The other two flow regimes discussed below are characterized by the absence of ZELTs. In the isotropic regime with high bottom friction ($\gamma = 5 \times 10^{-7} \text{ s}^{-1}$, $\beta = 1.14 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$), $\alpha \ll 1$ and ZELTs are not observed (figure 1f). The 2-D wavenumber (Fourier) spectrum has a doughnut-like shape with the power distributed almost uniformly within a range of the total wavenumbers (figure 1c). The leading EOFs show chaotically distributed anomalies around the domain, and AC1 decays rapidly with time, indicating the lack of persistent patterns (figure 1i). Finally, we also consider the case with low bottom friction, for which α for the leading EOFs exhibits unexpectedly low value ($\gamma = 1 \times 10^{-7} \text{ s}^{-1}$, $\beta = 2.15 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$).

Zonal flows



Figure 1. The spatial Fourier spectra, leading EOF and AC function of leading principal component for model solution with the parameter values $(a,d,g) \gamma = 1 \times 10^{-7} \text{ s}^{-1}$, $\beta = 2.15 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$, $(b,e,h) \gamma = 3 \times 10^{-7} \text{ s}^{-1}$, $\beta = 2.15 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$ and $(c,f,i) \gamma = 5 \times 10^{-7} \text{ s}^{-1}$, $\beta = 1.14 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$.

We term this case as 'quirky' as it basically represents the special case reported in Rudko *et al.* (2018) (see figure 18 in that paper). The spatial structure of the leading EOF displays rather irregular arrays of eddies and ZELTs are not visible (figure 1*d*). The spatial 2-D Fourier spectrum displays two areas with enhanced power, one that is situated at small zonal wavenumbers and the second that covers intermediate zonal wavenumbers and a wide range of meridional wavenumbers (figure 1*a*). Unlike the simulation with prominent ZELTs, whose spectrum has a somewhat similar shape, these two areas are well separated and the spectral peak at small zonal wavenumbers is not as intense. The AC1 for this case displays several oscillations with vanishing magnitude at a 12 000 day time lag (figure 1*g*). We note in passing that the 'quirky' regime is also characterized by prominent stationary zonal jets. The ZELT-dominated regime, therefore, corresponds to the intermediate values of bottom drag and can be interpreted as the transition from strongly anisotropic to isotropic turbulence.

We are closing this section by discussing the limitations of the quasi-geostrophic model. Simulations in a more realistic model would certainly entail some differences. ZELTs may not show up as leading EOF modes since the mesoscale variability can be obscured by the seasonal cycle and variability in the atmospheric forcing. Some additional filtering may be required to separate ZELTs from the background field. Nevertheless, non-stationary striations were reported in several general circulation model based studies (Richards *et al.* 2006; Kamenkovich, Berloff & Pedlosky 2009; Melnichenko *et al.* 2010). Most recently, ZELTs were also found in altimetry data by Chen, Kamenkovich & Berloff (2016). We expect, however, that it suffices to use our two-layer quasi-geostrophic model to represent the dominant processes associated with the nonlinear baroclinic dynamics of ZELTs.

Abbreviation	Term	Physical meaning
F_MBT1	$\langle J(\overline{\psi_p},q_p'),\phi_i angle$	Mean barotropic advection of eddy barotropic PV
F_MBT2	$\langle J(\psi_p',\overline{q_p}),\phi_i angle$	Eddy barotropic advection of mean barotropic PV
F_MBC1	$\theta_{11}\theta_{12}\langle J(\overline{\psi_c},q_c'),\phi_i\rangle$	Mean baroclinic advection of eddy baroclinic PV
F_MBC2	$\theta_{11}\theta_{12}\langle J(\psi_c',\overline{q_c}),\phi_i\rangle$	Eddy baroclinic advection of mean baroclinic PV
F_MREL1	$\langle J(\overline{\psi_p},\xi_c'),\phi_i angle$	Mean barotropic advection of eddy baroclinic RV
F_MREL2	$\langle J(\psi_p',\overline{\xi_c}),\phi_i angle$	Eddy barotropic advection of mean baroclinic RV
F_MX11	$\langle J(\overline{\psi_c},q_p')),\phi_i angle$	Mean baroclinic advection of eddy barotropic RV
F_MX12	$\langle J(\psi_c', \overline{q_p}), \phi_i angle$	Eddy baroclinic advection of mean barotropic RV
F_MB1	$(S_1 + S_2) \langle J(\overline{\psi_p}, \psi_c'), \phi_i \rangle$	Mean barotropic advection of eddy buoyancy
F_MB2	$(S_1 + S_2) \langle J(\psi'_p, \overline{\psi_c}), \phi_i \rangle$	Eddy barotropic advection of mean buoyancy
F_MBC11	$\langle (\theta_{11}^2 - \theta_{12}^2) \langle J(\overline{\psi_c}, q'_c), \phi_i \rangle$	Mean baroclinic advection of eddy baroclinic PV
F_MBC12	$\langle (\theta_{11}^2 - \theta_{12}^2) \langle J(\psi_c', \overline{q_c}), \phi_i \rangle$	Mean baroclinic advection of eddy baroclinic PV
F_EBT	$\langle J(\psi_p',q_p')',\phi_i angle$	Eddy barotropic advection of eddy barotropic RV
F_EBC	$ heta_{11} heta_{12}\langle J(\psi_c',q_c')',\phi_i angle$	Eddy baroclinic advection of eddy baroclinic PV
F_EREL	$\langle J(\psi_p',\xi_c')',\phi_i angle$	Eddy barotropic advection of eddy baroclinic RV
F_MX2	$\langle J(\psi_c',q_p')',\phi_i angle$	Eddy baroclinic advection of eddy barotropic PV
F_EB	$(S_1+S_2)\langle J(\psi'_p,\psi'_c)',\phi_i\rangle$	Eddy baroclinic advection of eddy buoyancy
F_EBC1	$(\theta_{11}^2 - \theta_{12}^2) \langle J(\psi_c', q_c')', \phi_i \rangle$	Eddy baroclinic advection of eddy baroclinic PV

Table 1. Projection of the nonlinear forcing onto EOFs. PV - potential vorticity, RV - relative vorticity.

3. Steady state dynamics

We examine which nonlinear terms in the potential vorticity balance play dominant roles in the ZELT dynamics. This approach represents an extension of a similar analysis for stationary zonal jets (Kamenkovich et al. 2009; Berloff et al. 2009a). We apply our analysis to the barotropic and baroclinic balances for the zonally and time-dependent potential vorticity components (see appendix A). In order to quantify the impact of nonlinearity on ZELTs, we project the dynamical balance onto several leading EOFs of the streamfunction. Note that the same EOFs are used to define ZELTs in the study. Our main focus is on the advection of the potential vorticity, which represents the internally generated nonlinear forcing. This nonlinear forcing is due to interactions between eddies and mean state (EME) and due to interactions between eddies only (EEE). The projections of the EME components are F_MBT1, F_MBT2, F_MBC1, F_MBC2, F_MREL1, F_MREL2, F_MB1, F_MB2, F_MBC11, F_MBC12, the projections of EEE components are F_EBT, F_EBC, F_EREL, F_EB, F_EBC1 (table 1). The acronyms follow these conventions: F stands for forcing, M - eddy-mean component, E - eddy-eddy component, BT barotropic, BC - baroclinic and MX - mixed barotropic/baroclinic. When potential vorticity is further split into the relative vorticity and buoyancy terms we use REL for the relative vorticity, B for the buoyancy. All projections are conveniently summarized in table 1. We report on the magnitude of the projections (averaged in time) and on a time correlation between the projections of the tendency terms and the eddy forcing. The magnitude of the projections informs us of the relative contribution of each components of the nonlinear forcing to sustain ZELTs, while the correlations tell us whether the forcing works in favour or against ZELTs.

911 A61-6

https://doi.org/10.1017/jfm.2020.1056 Published online by Cambridge University Press



Figure 2. The projection of different components of the nonlinear forcing onto the nine leading EOFs in the 'quirky' case: (a,b) barotropic mode, (c,d) baroclinic mode.

In order to emphasize the particularity of the regime in which ZELTs appear as dominant modes of mesoscale variability, we carry out the analysis for three different cases discussed in the previous section. In line with Rudko *et al.* (2018), who defined ZELTs as 9 leading EOFs, we consider the projections of 9 EOFs in all three cases considered here as well. The EME forcing dominates the eddy forcing in the low-friction case with no ZELTs ('quirky' case; figure 2(a,c)), thereby suggesting that the mean state imposes a strong control on the structure and magnitude of the eddying field. This is reminiscent of the 'linear control' reported in Berloff & Kamenkovich (2013*a*,*b*) in a similar regime. In contrast, the EEE forcing dominates the eddy forcing in the ZELT-dominated regime, suggesting a strongly nonlinear dynamics (figure 3*a*,*c*). Both the EEE and EME forcing components are of the same order of magnitude in the isotropic turbulence simulation (figure 4*a*,*c*) with high bottom friction. In all cases, the projections of various components of the EME forcing tend to cancel each other in both the barotropic and baroclinic modes (figures 2*b*, 3*b*, 4*b*).

We next turn our attention to the specific EEE forcing components, contrasting the ZELT-dominated and isotropic regimes, since the eddy-eddy forcing is important in both cases. The EEE forcing components in the barotropic balance always act in accord with each other in the ZELT-dominated case: F_EBT and F_EBC support all EOFs (figure 3a). The same is true in the isotropic regime (figure 4a). The EEE forcing in the baroclinic balance exhibits a different behaviour. In the ZELT-dominated regime,





Figure 3. The projection of the different components of the nonlinear forcing onto the nine leading EOFs in the ZELT-dominated case: (a,b) barotropic mode, (c,d) baroclinic mode.

advection of potential vorticity by baroclinic eddies, F_MX2 and F_EBC1 both resist ZELTs (figure 3b). In contrast, advection of eddy buoyancy F_EB and eddy baroclinic relative vorticity F_EREL by barotropic eddies always counteract each other, with F_EREL supporting ZELTs and F_EB resisting them. However, the magnitudes of the F_MX2 and F_EB projections are higher than the projections of other EEE forcings, thereby suggesting that, in a steady state, the dynamics of ZELTs is predominantly regulated by the advections of eddy barotropic potential vorticity and buoyancy, F_MX2 and F_EB (figure 3b). The same two terms, F_MX2 and F_EB, also tend to be important in the isotropic regime, although the significance of F_EREL and F_EBC1 is harder to establish.

In summary, the ZELT dynamics is dominated by the eddy forcing associated with eddy–eddy interactions, whereas the eddy–mean flow interactions play one of the leading roles in the cases with no ZELTs. Two eddy forcing components that are particularly important in the ZELT dynamics are the advection of eddy barotropic potential vorticity and eddy buoyancy, F_MX2 and F_EB. In the next section, we explicitly examine the relative importance of various types of EEE forcing for ZELT existence.



Figure 4. The projection of the different components of the nonlinear forcing onto the nine leading EOFs in the isotropic case: (a,b) barotropic mode, (c,d) baroclinic mode.

4. Reduced-dynamics models

In this section, we discuss simulations with fully or partially precluded EEE forcing, as it is this type of forcing that is associated with the cascades of eddy energy. Once can identify a group of EEE terms that correspond to each type of eddy energy cascade. Setting these EEE terms to zero in our numerical simulations effectively precludes the corresponding energy cascade. We consider four reduced-dynamics sensitivity experiments with: (*a*) precluded cascade of total eddy energy, (*b*) precluded eddy kinetic energy cascade in the barotropic mode, (*c*) precluded eddy kinetic energy cascade in the baroclinic mode, (*d*) precluded cascade of eddy potential energy. Table 2 lists the EEE terms that are set to zero and corresponding energy cascades that are precluded in each of these sensitivity experiments. In all cases the net energy is preserved. The duration of each simulation and the values of parameters are the same as for the fully nonlinear simulations.

The ZELT-dominated simulation with no eddy energy cascade exhibits a complete lack of power at the small zonal wavenumbers, implying the absence of ZELTs (figure 9a). The complete disappearance of ZELTs is further confirmed by the spatial structure of the the leading EOF, which displays meridionally elongated flow patterns similar to the most unstable mode of the baroclinically unstable background flow (figure 6a). The AC1 for this case (figure 12a) exhibits high-frequency variability, which is at odds with the evolution of AC1 in the fully nonlinear simulations. Similarly, the spectral power is dramatically

Model

Physical meaning

No total eddy energy transport

$$\begin{split} &J(\psi'_{c}, q'_{c})'_{c} \to 0 \\ &J(\psi'_{p}, q'_{p})' \to 0 \\ &J(\psi'_{c}, q'_{p})' \to 0 \\ &J(\psi'_{c}, q'_{p})' \to 0 \\ &(S_{1} + S_{2})J(\psi'_{c}, \psi'_{p})' \to 0 \end{split}$$

 $\begin{array}{l} J(\psi_p',q_p')' \rightarrow 0 \ J(\psi_c',q_c')_p' \rightarrow 0 \\ J(\psi_p',q_c')' \rightarrow 0 \ J(\psi_c',q_p')' \rightarrow 0 \end{array}$

No kinetic eddy energy transport in barotropic mode No eddy kinetic energy transport in baroclinic mode No eddy potential energy transport





Figure 5. Reduced-dynamics simulations for the 'quirky' case. Leading EOF for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.

reduced at small zonal wavenumbers in the cases with no ZELTs: the high-friction isotropic and 'quirky' cases (figures 8(a) and 10(a), respectively). These results suggest that the accumulation of energy at long zonal length scales in those two cases and the emergence of ZELTs in the ZELT-dominated case, are due to nonlinear interactions between eddies. This was expected for the ZELT-dominated regime simulations, because the EEE terms play a key role in the potential vorticity balance. The importance of EEE interactions in the 'quirky' case may look surprising, given the fact that the potential vorticity balance is dominated by the eddy–mean flow interactions. Additionally, in both isotropic and 'quirky' cases, the leading EOF shows no signs of zonal anisotropy (figures 5a and 7a), while the AC1 indicates much higher temporal variability than in the fully nonlinear simulations (figures 11a and 13a).

Removing the eddy kinetic energy cascade in the barotropic mode retains some spectral power at small zonal wavenumbers for the ZELT-dominated and 'quirky' cases (figures 8b and 9b). However, the leading EOF does not display zonally elongated patterns in either case, although the tendency of organization of the flow into chains of eddies ('eddy trains', Chen *et al.* (2016)) is still discernible (figures 5b and 6b). AC1 shows rapid decay with ensuing fluctuating around zero, illustrating fast decorrelation of these eddies. In the isotropic case, the spatial Fourier spectrum bears a lot of resemblance to the spectrum of the fully nonlinear simulations (figure 5b). Interestingly, the leading EOF is anisotropic



Figure 6. Reduced-dynamics simulations for the ZELT-dominated case. Leading EOF for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.



Figure 7. Reduced-dynamics simulations for the isotropic case. Leading EOF for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.

in this case (figure 7b). We recall that the barotropic eddy–eddy interactions are acting to enhance leading EOFs in the full isotropic simulation (figure 8), but these EOFs are isotropic. When the barotropic energy cascade is removed, these isotropic modes disappear and the latent anisotropy becomes visible.

The spectra for the simulation with no eddy kinetic energy cascade in the baroclinic mode resemble the simulation with no eddy energy transport: there is a negligible amount of spectral power at small zonal wavenumbers (figures 8c, 9c and 10c). It is interesting that the removal of the baroclinic energy cascade in the ZELT-dominated case leads to a significantly larger reduction in the spectral power than in the same case with no barotropic kinetic energy cascade. The leading EOF in all three cases display arrays of isolated eddies (figures 5c, 6c and 7c). The AC1 shows a slow decay in the 'quirky' and ZELT-dominated cases (figures 11c and 12c); the AC1 in the isotropic and fully nonlinear cases varies in a similar manner. We can certainly claim that the cascade of the eddy kinetic energy



Figure 8. Reduced-dynamics simulations for the 'quirky' case. Spatial Fourier spectra for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.

in the baroclinic mode plays a leading role in assisting the emergence of ZELTs in the ZELT-dominated case – the expected effect from the analysis of the potential vorticity balances in the previous section.

In both the 'quirky' and ZELT-dominated cases, the simulation with no eddy potential energy cascade exhibits spectral peaks at small zonal wavenumbers (figures 8d and 10d). The leading EOFs are zonally elongated in all three cases, including the isotropic regime (figures 5d, 6d and 7d). The AC1 exhibits a regular behaviour with rapidly decaying oscillations, two long oscillations and slowly decaying oscillations (figures 11d, 12d and 13d). We recall that the F_EB term plays a key role in the baroclinic potential vorticity balance, but acts to dissipate the flow patterns associated with the leading EOFs. It is, therefore, not surprising that the removal of the potential energy cascade enhances ZELTs in the ZELT-dominated case. The emergence of ZELTs in the isotropic and 'quirky' cases is an interesting result, suggesting that the potential energy cascade dissipates ZELTs and explains why they are not visible in either of the fully nonlinear simulations. Lastly, we note an overall similarity of the reduced-dynamics simulations in the ZELT-dominated and 'quirky' regimes.

5. Summary and discussion

This study is concerned with the origins and mechanisms of mesoscale variability in the mid-latitude oceans. This mesoscale variability is anisotropic, and a previous study by Maltrud & Vallis (1991) reported that the dominant modes of this variability



Zonal flows

26 26 -1.51.5 3.5 -3.5 -1.51.5 3.5 -3.5 $k \,(\mathrm{m}^{-1} \times 10^{-5})$ $k \,(\mathrm{m}^{-1} \times 10^{-5})$ Figure 9. Reduced-dynamics simulations for the ZELT-dominated case. Spatial Fourier spectra for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy

kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.

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-1.5

have the form of ZELTs. ZELTs vary in the zonal direction and time and are, thus, different from stationary zonal jets that have been the subject of extensive studies of anisotropic turbulence. In this paper, we have elucidated the mechanisms governing the evolution of ZELTs, in the context of quasi-geostrophic turbulence. We used a two-layer, quasi-geostrophic model with a resolution of 14 km. The governing equations are the conservation of layerwise potential vorticity with added bottom drag and viscosity. We have studied the dynamics of ZELTs using diagnostic (steady state dynamical balance) and prognostic approaches (reduced-dynamics simulations). We have studied three different flow regimes in which: (i) ZELTs appear as leading EOFs and the spectrum is anisotropic (ZELT-dominated case); (ii) the spatial structure of the leading EOFs and the spectrum is isotropic (isotropic case); and (iii) the leading EOFs display a quite irregular array of flow anomalies, but the spectrum is anisotropic ('quirky' case). The key findings of this study are that: (i) ZELTs are nonlinear phenomena that emerge as a result of eddy-eddy interactions; (ii) kinetic energy cascade is essential for ZELT emergence, with the baroclinic cascade being dominant; (iii) the potential energy cascade acts to damp ZELTs.

To distinguish ZELTs from previously studied zonal jets we decomposed the flow into zonally averaged ('mean') and deviation ('eddy') components. We have projected the governing equations onto several leading EOFs and analysed the projections of the nonlinear terms that are due to interactions between eddies ('eddy-mean' forcing) and the mean flow and between eddies only ('eddy-eddy' forcing). In the simulations with well-pronounced ZELTs (ZELT-dominated case), the eddy-eddy forcing dominates the

 $l\,(m^{-1}\times 10^{-5})$

 $l~(m^{-1}\times 10^{-5})$

-1.5

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Figure 10. Reduced-dynamics simulations for the isotropic case. Spatial Fourier spectra for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.



Figure 11. Reduced-dynamics simulations for the 'quirky' case. AC function for the leading principal component for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.



Figure 12. Reduced-dynamics simulations for the ZELT-dominated case. AC function for the leading principal component for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.



Figure 13. Reduced-dynamics simulations for the isotropic case. AC function for the leading principal component for simulations with (a) no eddy energy transport, (b) no eddy kinetic energy transport in the barotropic mode, (c) no eddy kinetic energy transport in the baroclinic mode and (d) no eddy potential energy transport.

potential vorticity balance: the largest contributing components are the divergences of the eddy barotropic vorticity flux and the eddy buoyancy flux. These components of eddy forcing entail the fluxes of eddy kinetic and eddy potential energies, and they tend to balance each other in all three regimes. In the 'quirky' case, the eddy-mean flow forcing dominates the dynamics, while the eddy-eddy interactions play a secondary role. This result is consistent with previous studies that reported the importance of the linear control in this flow regime (Berloff & Kamenkovich 2013a,b) and the results of quasilinear theory (Farrell & Ioannou 2007, 2008; Srinivasan & Young 2012). In the isotropic simulation, both types of nonlinear interaction are of the same order of magnitude.

To examine the importance of each type of energy transfer in the ZELT dynamics, we have considered several reduced-dynamics models, in which certain types of eddy-eddy interactions are truncated. Although the net energy is still conserved in all the experiments, the regimes they correspond to are different from the original simulations and are sensitive to the particular choice of truncation. The purpose of this exercise is to explore this sensitivity and demonstrate the importance of a specific type of energy exchange for the existence of ZELTs. The simulation with the removed transfer of the eddy energy shows no spectral power at small zonal wavenumbers and EOFs that are not zonally elongated. These results collectively demonstrate that ZELTs are a product of nonlinear interactions between eddies, confirming our conclusions from the analysis of the steady state nonlinear forcing. Analysis of the simulations, in which either the barotropic or baroclinic kinetic energy fluxes are blocked, also demonstrates the absence of ZELTs, confirming the importance of these types of energy cascades for ZELT emergence. The removal of the baroclinic cascade, however, leads to a particularly dramatic reduction in spectral power. Instead, the flow is dominated by eddies propagating along zonal tracks. These eddy trains have been reported previously in both model simulations and satellite data (Chen et al. 2016), and our results here further demonstrate that they become preferred modes of mesoscale variability once the kinetic energy cascade is suppressed.

Finally, the simulations with the removed cascade of the eddy potential energy show that the zonally elongated patterns are amplified and appear as dominating modes for all parameter choices of this study. Since the cascade of the eddy potential energy is directed downscale, and the corresponding term is shown to damp ZELTs, its removal leads to the accumulation of energy in the long scales. Additionally, the removal stops downward transfer the energy and weakens the energy dissipation by the bottom drag (Khatri & Berloff 2018b). The change is particularly dramatic in isotropic and 'quirky' cases, which implies that this damping effect explains the lack of ZELTs in these regimes. The damping effect of the eddy buoyancy advection, compensated by the relative vorticity advection, is analogous to a similar balance in the stationary zonal jets, and is likely to be a fundamental property of anisotropic turbulence in the ocean. These results demonstrate the importance of baroclinic dynamics and the potential energy transfer, which are often ignored in the analysis of ocean energetics. This importance does not mean that ZELTs cannot be observed in barotropic flows. In fact, we expect zonally elongated modes of mesoscale variability to be ubiquitous in geostrophic turbulence with and without vertical stratification. For example, similar structures, termed 'zonons', have been observed in barotropic flows with small-scale forcing (Danilov & Gurarie 2004; Sukoriansky, Dikovskaya & Galperin 2008; Galperin & Sukoriansky & Dikovskaya 2010). Similarly, stationary zonal jets are prominent features of barotropic turbulence (Rhines 1994; Galperin et al. 2004), despite the importance of buoyancy transfers for their baroclinic counterparts (Panetta 1993; Berloff et al. 2009b).

The presence of the anisotropic flow patterns in oceanic circulation gives rise to asymmetry in the distribution of momentum, energy and oceanic tracers. Although the present study improves our understanding of the origins of anisotropy in mesoscale turbulence, the scope of the work is limited due to the simplicity of the model. Studies with general circulation models would definitely expand the current view on the issue.

Acknowledgement. The authors would like to thank M. Iskandarani for helping with model configuration.

Funding. M.R. was supported by NSF grant OCE-1154923. I.K. was supported by NOAA grant NA16OAR4310165.

Declaration of interests. The authors report no conflict of interest.

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Appendix A. Dynamical balance

We derive the dynamical balance in several steps. First, the vertical structure of the two-layer quasi-geostrophic system can be fully described by the barotropic and the first baroclinic modes (Pedlosky 2013). The projection of the governing equations onto these two modes gives

$$\begin{aligned} \frac{\partial q_p}{\partial t} + J(\psi_p, q_p) + \theta_{11}\theta_{12}J(\psi_c, q_c) + \beta \frac{\partial \psi_p}{\partial x} + US_1\theta_{11}\frac{\partial \psi_c}{\partial x} \\ &= -U\theta_{11}\frac{\partial q_p}{\partial x} - U\theta_{11}\theta_{12}\frac{\partial q_c}{\partial x} - \gamma \theta_{12}q_p + \gamma \theta_{11}\theta_{12}\xi_c + \nu \nabla^2 q_p, \end{aligned}$$
(A1)
$$\begin{aligned} \frac{\partial q_c}{\partial t} + J(\psi_p, q_c) + J(\psi_c, q_p) + (\theta_{11}^2 - \theta_{12}^2)J(\psi_c, q_c) \\ &+ (\beta + U(S_1\theta_{12} - S_2\theta_{11}))\frac{\partial \psi_c}{\partial x} + U(S_1 + S_2)\frac{\partial \psi_c}{\partial x} \\ &= -U\frac{\partial q_c}{\partial x} - U\theta_{12}\frac{\partial q_c}{\partial x} - \gamma q_p + \gamma \theta_{11}\xi_c + \nu \nabla^2 \xi_c, \end{aligned}$$
(A2)

where

 q_c

$$\theta_{11} = \frac{H_1}{H_1 + H_2} = \frac{\frac{H_1}{H_2}}{\frac{H_1}{H_2} + 1} = \frac{\delta}{\delta + 1},$$

$$\theta_{12} = \frac{H_2}{H_1 + H_2} = \frac{1}{\frac{H_1}{H_2} + 1} = \frac{1}{\delta + 1},$$

$$q_p = \nabla^2 \frac{H_1 \psi_1 + H_2 \psi_2}{H_1 + H_2} = \nabla^2 \psi_p,$$

$$= \nabla^2 (\psi_1 - \psi_2) - (S_1 + S_2)(\psi_1 - \psi_2) = \nabla^2 \psi_c - (S_1 + S_2)\psi_c = \xi_c - (S_1 + S_2)\psi_c.$$

(A3)

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Decomposing the flow field into 'mean' (zonally averaged) and 'eddy' (deviation from zonally averaged) components leads to a set of four equations

$$\frac{\partial \overline{q_p}}{\partial t} = -\overline{J(\psi_p', q_p')} - \theta_{11}\theta_{12}\overline{J(\psi_c', q_c')} - \gamma\theta_{12}\overline{\xi_p} + \gamma\theta_{11}\theta_{12}\overline{\xi_c} + \nu\nabla^2\overline{\xi_p}, \quad (A4)$$

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$$\frac{\partial q'_p}{\partial t} = -J(\overline{\psi_p}, q'_p) - J(\psi'_p, \overline{q_p}) - J(\psi'_p, q'_p)' - \theta_{11}\theta_{12}[J(\overline{\psi_c}, q'_c) + J(\psi'_c, \overline{q_c}) + J(\psi'_c, q'_c)']
- \beta \frac{\partial \psi'_p}{\partial x} - US_1\theta_{11}\frac{\partial \psi'_c}{\partial x} - U\theta_{11}\frac{\partial q'_p}{\partial x} - U\theta_{11}\theta_{12}\frac{\partial q'_c}{\partial x}
- \gamma \theta_{12}\xi'_p + \gamma \theta_{11}\theta_{12}\xi'_c + \nu \nabla^2 \xi'_p,$$
(A5)

$$\frac{\partial \overline{q_c}}{\partial t} = -\overline{J(\psi_p', q_c')} - \overline{J(\psi_c', q_p')} - (\theta_{11}^2 - \theta_{12}^2)\overline{J(\psi_c', q_c')} - \gamma \overline{\xi_p} + \gamma \theta_{11} \overline{\xi_c} + \nu \nabla^2 \overline{\xi_c}, \quad (A6)$$

$$\frac{\partial q'_c}{\partial t} = -J(\overline{\psi_p}, q_c) - J(\psi'_p, \overline{q_c}) - J(\psi'_p, q'_c)' - J(\overline{\psi_c}, q'_p) - J(\psi'_c, \overline{q_p}) - J(\psi'_c, q'_p)'
- (\theta_{11}^2 - \theta_{12}^2)[J(\overline{\psi_c}, q'_c) + J(\psi'_c, \overline{q_c}) + J(\psi'_c, q'_c)']
- (\beta + U(S_1\theta_{12} - S_2\theta_{11}))\frac{\partial \psi'_c}{\partial x} - U(S_1 + S_2)\frac{\partial \psi'_p}{\partial x} - U\frac{\partial q'_p}{\partial x} - U\theta_{12}\frac{\partial q'_c}{\partial x}
- \gamma \xi'_p + \gamma \theta_{11}\xi'_c + \nu \nabla^2 \xi'_c.$$
(A7)

Equations (A4) and (A6) describe the dynamics of stationary ($\omega = 0, k = 0$) and drifting zonal jets ($\omega \neq 0, k = 0$), while equations (A5) and (A7) govern the evolution of 'eddies' ($\omega \neq 0, k \neq 0$). Since ZELTs are a part of the 'eddy' flow component, we discuss equations (A5) and (A7) only. The left-hand sides of these equations are the tendency terms, which describe the rate of change in the 'eddy' potential vorticity, whereas the right-hand side consists of several nonlinear terms ('eddy forcing'), as well as linear terms that contain the modified β -terms, external forcing terms and large- and small-scale friction.

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https://doi.org/10.1017/jfm.2020.1056 Published online by Cambridge University Press