Characterization of a loaded high impedance surface

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A high impedance surface (HIS) consisting of metallic square patches electrically connected one to each other with resistors is shown. Tunability of the absorption factor is achieved by the resistor value. The absorbing band of the loaded HIS is determined by the phase of the signal reflected by this structure. The main contribution of the paper is to demonstrate the absorption behavior over a wide range of incidence angle for both Transverse Electric (TE) and Transverse Magnetic (TM) polarizations. Using an equivalent circuit the resistor effect is investigated. It is shown that at resonance, the judicious choice of the resistor may lead to a significant absorption. The use of a waveguide simulator to characterize the performance of the loaded HIS is investigated. These methods have been used to design an ultra-thin absorber about $\lambda_{8.4 \text{GHz}}/35$ thick.

Keywords: High impedance surface (HIS), Ultra-thin radar absorbing material, Salisbury screen, Resistor, Waveguide simulator

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I. INTRODUCTION

Radar absorbing material (RAM) has largely been studied in the literature. The simplest and best known are the Salisbury and the Jaumann screens [1, 2]. The Salisbury screen consists of a resistive sheet mounted one-quarter wavelength in front of a ground plane. The Jaumann absorber is similar to the Salisbury screen except that resistive sheets are stacked over each other and separated by dielectrics slabs about $\lambda/4$ thick. The wideband absorption of the aforementioned techniques is achieved by creating additional $\lambda/4$ -resonance and hence increasing the weight and the height of these structures. A solution to synthesize low-profile absorber is the use of frequency selective surface or high impedance surface (HIS) [3-6]. These solutions are closely similar to the Salisbury screen: the resonance is achieved by the capacitive sheet and the absorption by the resistive sheet. In this paper, a resistive HIS (R-HIS) is studied: the HIS is considered to define the absorbing frequency range by the reflection phase diagram and the desired absorption is achieved by loading the HIS with resistors. The main use of HIS is to operate as an artificial magnetic conductor, so that the quarter wavelength over the ground plane is no longer necessary, decreasing the thickness of the structure. The R-HIS has already been used to reduce the thickness of an Archimedean spiral [7] and the mutual coupling between two radiators [8]. The behavior of this structure has been described in the literature [9, 10]. However, the analytical and numerical results were only obtained for a normal incident angle. One of the aims of this contribution is to

II. RESISTIVE HIS DESIGN

The absorber under study is illustrated in Fig. 1. The structure consists of a planar array of metallic square patches located above a grounded dielectric layer. The planar grid of metallic square patches has a capacitive response which, in conjunction with the inductive response of the metal backed substrate, forms a resonator. By altering L or C, the resonance frequency of the resonant circuit can be changed: $\omega = 1/\sqrt{LC}$. In order to keep a low-profile structure, it is more convenient to adjust the capacitance C than the inductance L. The desired absorption is defined by introducing losses in the structure through connection of adjacent patches by a resistor.

Where w is the width of the metallic square patches, g is the gap between the adjacent patches, and h the thickness of the grounded substrate. k_0 is the free space wave vector, ε_r and μ_r are, respectively, the relative permittivity and relative permeability of the substrate.

The equivalent circuit used to determine the absorbing band by the reflection phase diagram is illustrated in Fig. 2. The R-HIS is treated as the load of a transmission line model with free space characteristic impedance $Z_{\rm o.}$ The expressions for the reflection coefficients Γ^{TE} and Γ^{TM}

The expressions for the reflection coefficients Γ^{IE} and Γ^{IM} corresponding to the two polarizations of the incident wave (respectively *TE* and *TM*) are [14]:

$$\Gamma^{TE} = \frac{Z_s^{TE} \cos \theta - Z_o}{Z_c^{TE} \cos \theta + Z_o},\tag{1}$$

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propose a fast method to design an R-HIS, based on equivalent transmission line circuit for both TE and TM incidence polarizations. The analytical results are compared to those obtained with CST Microwave Studio (CST MWS). The proposed design is finally analyzed in a waveguide simulator setup [11–13].

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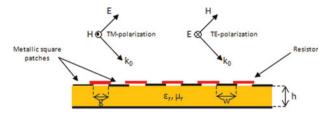


Fig. 1. Side view of the R-HIS illuminated by TE and TM polarization of the plane wave incident.

$$\Gamma^{TM} = \frac{Z_s^{TM} - Z_0 \cos \theta}{Z_s^{TM} + Z_0 \cos \theta},\tag{2}$$

where $Z_s^{TE/TM}$ refers to the surface impedance of the R-HIS for the TE and TM polarized incident fields and θ is the incident angle. The surface impedance Z_s of the R-HIS can be considered to be a parallel connected capacitance C, an inductance L and a resistor R:

$$(Z_s^{TE/TM})^{-1} = R^{-1} + (Z_C^{TE/TM})^{-1} + (Z_L^{TE/TM})^{-1}.$$
 (3)

From [15], the formulas of the capacitance and inductance for each polarization of the incident field are

$$Z_{c}^{-1^{TM}} = j\omega \frac{P}{\pi} \varepsilon_{0}(1 + \varepsilon_{r}) \log \left(\csc \left(\frac{\pi g}{2P} \right) \right), \tag{4}$$

$$Z_{c}^{-1^{TE}} = j\omega \frac{P}{\pi} \varepsilon_{o} (1 + \varepsilon_{r}) \log \left(\csc \left(\frac{\pi g}{2P} \right) \right) \cdot \left(1 - \frac{k_{o}^{2}}{k_{eff}^{2}} \sin^{2} \theta \right), \tag{5}$$

$$Z_L^{TE/TM} = j\omega \,\mu_0 \frac{\tan(\beta h)}{\beta} \left(\frac{1}{l_t} - \frac{k_t k_t}{k^2} \right), \tag{6}$$

where P=w+g is the period of the structure, $\beta=\sqrt{k^2-k_t^2}$ is the normal component of the wave vector in the substrate with k the wave vector in the substrate and k_t the tangential wave vector component imposed by the incident wave. $k_{eff}=k_{\rm o}\sqrt{\epsilon_{eff}}$ is the wave vector in the effective host medium, $\varepsilon_{\rm o}$ and $\mu_{\rm o}$ are, respectively, the permittivity and permeability of free space, $Z_{\rm o}=\sqrt{\mu_{\rm o}/\varepsilon_{\rm o}}$ is the free space impedance and \overline{l}_t is the dyadic unit. To improve the

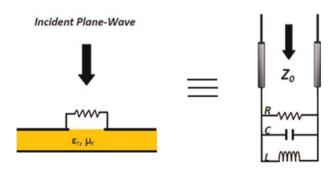


Fig. 2. Electric equivalent circuit of the R-HIS

accuracy of the expression of ε_{eff} , the closed expression given by Schneider has been used [16]:

$$\varepsilon_{eff} = \frac{\varepsilon_r + 1}{2} + \frac{(\varepsilon_r - 1)/2}{\sqrt{1 + 10 \, h/w}}.\tag{7}$$

Following the notations above, the dimensions of the structure studied are: P=4 mm, g=0.4 mm, h=1 mm, and $\varepsilon_r=10.2$. The value of the permittivity has been chosen to reduce the dependency on angle of the absorber. The analytical results are compared with numerical simulations obtained with CST MWS. The simulation model of the R-HIS is depicted in Fig. 3. The periodicity of the unit cell is achieved by using Floquet port and periodic boundary conditions.

III. INFLUENCE OF THE RESISTOR ON THE HIS

The equivalent circuit allows us to quickly determine the frequency resonance of the HIS. This frequency corresponds to 8.7 GHz observed in Fig. 4 when the HIS is illuminated by a normal incident plane wave. This result slightly differs from the simulation carried out with CST MWS: the difference is 300 MHz that is approximately 3.5%. Due to the all limitations of the electric model (quasi-static nature), the agreement between the results is considered reasonably good.

From the expressions (1) and (2), at resonance, a HIS exhibits infinite surface impedance which occurs with the free space impedance, hence the electromagnetic incident wave is totally reflected. The surface impedance can be decreased by the use of resistors, absorbing the incoming wave when the surface impedance of the R-HIS is matched to the free space impedance 377 Ω (see Fig. 4(c)). At resonance, the expression of the reflexion coefficient can be written as

$$\Gamma_{f=f_0} = \frac{Re(Z_s) - Z_0}{Re(Z_s) + Z_0} = \frac{R - \eta_0}{R + \eta_0}.$$
 (8)

The absorption coefficient is plotted for several values of the resistors in Fig. 4(c) for a normal incident angle of the incoming wave: as expected the absorption performance is best for a value of resistance of 377 Ω . Moreover when the resistor value is increased, an abrupt change of the phase reflection is observed: at resonance, when the resistor value

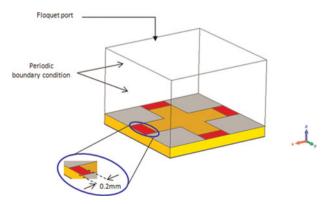


Fig. 3. View of the unit cell for simulation.

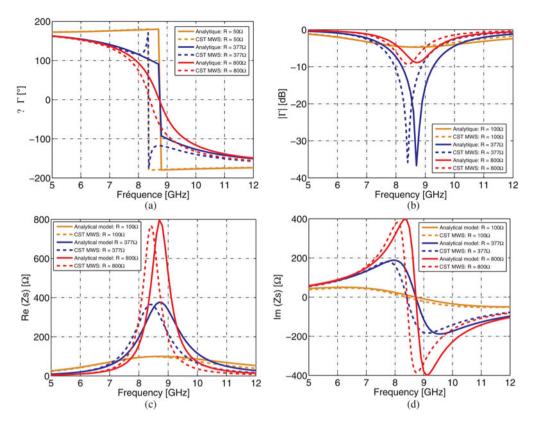


Fig. 4. Comparison between analytical results and CST MWS 2009: reflection coefficients versus frequency for several values of resistors: (a) phase reflection, (b) absorption, (c) real part of the surface impedance Z_s , and (d) imaginary part of the surface impedance Z_s .

R is less than the free space impedance η_0 , the phase of the reflection coefficient is equal to $\pm \pi$. As explained above, by inserting losses in the HIS, the PMC condition cannot be reached anymore.

The reflectivity of the HIS loaded by a resistor $R=377\,\Omega$ is plotted in Fig. 5 for normal incidence and for 30 and 60° incidence angle, for both TE and TM polarizations. The analytical results agree with CST MWS with a slight at the lower frequency for the numerical simulations. The performance of the R-HIS is affected by the change of incident angle. As for the Salisbury screen the R-HIS exhibits a narrow bandwidth in frequency and in angle. As expected the resonance frequency for TE polarization of the incident wave is affected (see expression (5)).

The equivalent electric circuit can be used to design rapidly the absorber and a simulation can be used to accurate the absorption band and the resonance of the structure.

IV. EXPERIMENTAL RESULTS

In order to validate the method, a measurement has been set up. A oversized rectangular waveguide is used to measure the absorption performance of the R-HIS. This measure uses the principle of images: the walls of the waveguide act as pairs of image planes which make the enclosed structure an infinity periodic environment. Waveguide simulators that are used to characterize antenna arrays can also be applied to periodic

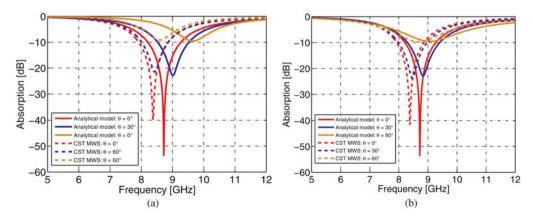
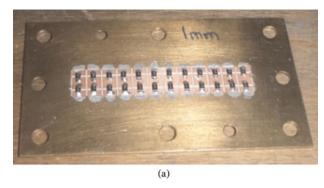


Fig. 5. Absorption coefficient for different incident angles: (a) TE polarization and (b) TM polarization.



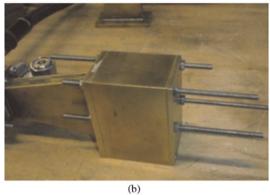


Fig. 6. (a) The fabricated R-HIS and (b) The R-HIS placed at the end of the waveguide simulator.

arrays such as FSS. Advantages and limitations of this method are described in [17]. The cross section of the waveguide must be commensurate to the periodicity of the structure. The dimensions of the waveguide simulator are $a \times b = 48 \times 8$ mm, where a is the large side of the waveguide. However this method has some limitations: the plane waves associated to the TE₁₀ mode are incident at angles:

$$\theta = \sin^{-1}\left(\frac{c}{2af}\right). \tag{9}$$

Moreover, measurements cannot be made outside the bandwidth of the TE_{10} mode. In the present case, the ultrathin RAM has a 12 \times 2 periodicity, and is positioned at the end of the waveguide (see Fig. 6). The 48 mm cross section

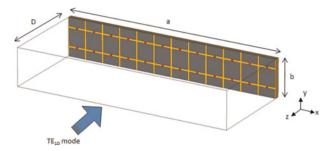


Fig. 7. The rectangular waveguide simulator simulation model (a=48 mm, b=8 mm, D=30 mm).

of the guide, corresponds to $\theta = 20.05^{\circ}$ at f = 8.4 GHz. The structure analyzed is simulated using CST MWS to be compared to measurement (see Fig. 7). In Fig. 8 the phase reflection and the absorption of a HIS and an R-HIS loaded by resistor value of 300 Ω are plotted. Without resistors mounted on the HIS, the measurement is well matched to the numerical simulation (Fig. 8(a)). Applying the same process for the R-HIS, a slight shift of 100 MHz in the upper frequency is observed with the measurement. Moreover, a 4 dB difference between the simulation and measurement is observed on the absorption (Fig. 8(b)). This magnitude difference may be due to the fabrication process: the resistor may not be accurate in high frequencies and the structure is very sensitive to the height of the substrate. However the experimental results agree with the simulations for these two studies cases, indicating the proposed analytical and numerical model are accurate to design an ultra-thin absorber.

V. CONCLUSION

An ultra-thin absorber has been investigated: the total thickness of the R-HIS is $\lambda_{8.4 {\rm GHz}}/35$. The absorption level of the RAM can be controlled by the choice of the resistor value, whereas the geometric parameters define the absorption band. The use of an electric equivalent circuit based on the transmission line approach allows a quick design of the absorber. The effects of the resistor on the R-HIS have been studied for TE and TM polarizations of the incident wave. The R-HIS performance is best when the HIS is loaded by a resistor equal to the free space impedance. The analytical results have been

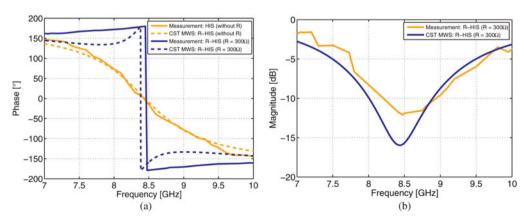


Fig. 8. Experimental and CST MWS results of the reflection coefficients of a R-HIS $(R = 300 \ \Omega)$ and a HIS (without R): (a) phase and (b) magnitude.

compared to simulations done with CST MWS. A good agreement has been observed between the results despite a slight shift in frequency: a simulation can be done to get accurate results. All these results have been validated with the use of a waveguide simulator.

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