

UNTOUCHABLE OR UNREPEATABLE? THE UPPER END OF THE OLD BABYLONIAN METROLOGICAL SYSTEMS FOR CAPACITY AND AREA

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This article re-examines the cuneiform evidence for the upper end of the Old Babylonian metrological systems for capacity and area. We demonstrate that the reading $1(\text{šar}_2)$ gal šu nu-tag “one large šar_2 that the hand cannot touch” is not supported by that evidence, and show instead that the phrase’s final sign is not tag but gi_4 “return” or “repeat”. We then consider several likely interpretations of this reading, arguing that the size of the largest units in both systems is probably sixty times smaller than previously assumed, but nevertheless more than adequate for practical needs. Editions of two important metrological cuneiform texts are appended.

In the past decade there has been a resurgence of interest in metrological systems, both as taught in Old Babylonian scribal schools (e.g. Robson 2002; Proust 2008b) and as implemented by traders and regulatory authorities (Chambon 2011). The relationships between mathematical word problems and Ur III and Old Babylonian administrative praxis have been relatively well explored (e.g. Nemet-Nejat 1993; Robson 1996; 1999: 138–67; Friberg 2001). However, it is rare for studies of metrological systems to consider the interactions between the theoretical metrologies of the school texts and their practical counterparts in the administrative and legal record. In this article we consider the very largest capacity and area measures, as learned by trainee scribes and used by professional surveyors and accountants in early Mesopotamia.¹

Untouchable?

It is often presented as an established historical fact that the classic Old Babylonian capacity and area systems each ended with the entry $1(\text{šar}_2)$ gal šu nu-tag,² literally “one large šar_2 that the hand cannot touch” or “reach”, and that this was a unit sixty times larger than the immediately preceding entry $1(\text{šar}_2)$ gal “one large šar_2 ” (e.g. Friberg 1982: 14; 1986: 15; 1987–90: 538; Proust 2007: 102–3, 2008a: 13). Indeed, Christine Proust (2000: 302) even suggests that this unit was the largest possible quantity representable on a hypothetical abacus board which was somehow constrained to just five sexagesimal places.³

The existence of a metrological “unit” $1(\text{šar}_2)$ gal šu nu-tag seems to stem from a reading of CBS 10990, a large compilation of metrological lists from Nippur first published in copy by Hilprecht (1906: no. 29), which would now be described as a Type I tablet in Civil (1969: 27–28) and Veldhuis’s (1997: 28–40) classification of Old Babylonian elementary school tablets. However, the reading and interpretation of $1(\text{šar}_2)$ gal šu nu-tag does not seem to be Hilprecht’s, for he postponed discussion of the metrological tablets in *BE* 20/1 to the never-to-appear *BE* 20/2 (Hilprecht 1906: 35). As Friberg (1982: 17) notes, shortly afterwards Barton (1909: 16) suggested a reading šAR_2 -GAL

¹ We are very grateful to Professor Eva Cançik-Kirschbaum and colleagues on the TOPOI project of the Freie Universität Berlin for facilitating and funding our first work session on this topic in July 2009.

² There are many ways of transliterating early Mesopotamian metrological units. Here we follow the conventions of the Cuneiform Digital Library Initiative = CDLI (<http://oracc.org/doc/builder/numbers/numref.pdf>), in which the notations such as $3(\text{bur}_3)$ mean three repetitions of the sign BUR_3 (i.e. $\text{bur}_3 \text{ bur}_3 \text{ bur}_3$). However, instead of CDLI’s $1(\text{šargal})^{\text{gal}}$ we write $1(\text{šar}_2)$ gal because the frequent writing gal-la(-am₃), as shown below, demonstrates that—in Old Babylonian school contexts, at least—the sign GAL is not a determinative.

³ Proust (2000: 302) also dismisses the possibility of Old Babylonian “dust abaci”—namely *ad hoc* counting surfaces drawn out on any convenient flat surface—on the grounds of work by Høystrup (2000: 4; Proust cites a preprint). In fact Høystrup argues there for “*calculi* placed on a counting board and not . . . *written numbers* on a dust abacus” (our emphasis), that is, for calculations using counters instead of numerals, not for or against formal apparatus of any particular sort. The evidence for Mesopotamian counting boards remains scant at best, while Netz (2002) has argued convincingly for the ubiquity of dust abaci used with counters in antiquity. There is no reason why the arguments put forward by Høystrup (2000) should not hold as well for informal dust abaci as for formal counting boards.

šu-nu-šum “the great šar, its double”. He derived a noun *šunnû* from *šanû* “to do twice, repeat” but without attempting to explain the erroneous substitution of the dative verbal suffix *-šum* “to/for him, it” for the nominal suffix *-šu* “his, its”. Neugebauer and Sachs (1945: 102–3) did not mention this phrase in their consideration of the equation tag = *šaḡālu(m)*, while Powell (1972: 176, 219) assumed that both CBS 10990 and the early Mesopotamian area, capacity and weight systems all stopped at 1(šar₂) gal.

The first relevant readings of this phrase we have been able to identify are Friberg’s ŠAR×GEŠ.GAL šu-nu-taga_x (1982: 14) and šár-gal šu-nu-taga_x “the great šár the hand does not reach” (1986: 14–15), which he links with the much earlier Eblaite phrase in 6(šar’u_x) gal nu-da-šid, a number that “cannot be counted”, in TM.75.G.1693 (Friberg 1986: 10).⁴ Note, though, that this Ebla text appears to be a list of large numbers in the discrete counting system, not capacities or areas, and is from a city on the edge of cuneiform culture, with its own very particular writing and counting conventions. It is *prima facie* unlikely to be pertinent to Old Babylonian educational practice.

The relevant passages of CBS 10990 are both badly damaged. They read:

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| <p>1. CBS 10990 obv. iii (Fig. 1a–b)</p> <p>1. 8(šar₂) ṛgur[†]</p> <p>2. 9(šar₂) ṛgur[†]</p> <p>3. 1(šar₂×u) ṛgur[†]</p> <p>4. 1(šar₂×man) gur</p> <p>5. 1(šar₂×eš) gur</p> <p>6. 1(šar₂×ilimmu) gur</p> <p>7. 1(šar₂×ninnu) gur</p> <p>8. 1(šar₂) gal gur</p> <p>9. 1(šar₂) gal šu nu-x ṛgur[†]</p> | <p>2. CBS 10990 rev. iii (Fig. 1c–d)</p> <p>1'. [. . .] ṛGANA₂[†]</p> <p>2'. [. . .] GANA₂</p> <p>3'. [. . .] GANA₂</p> <p>4'. [. . .] GANA₂</p> <p>5'. 1(šar₂×ilimmu) GANA₂</p> <p>6'. 1(šar₂×ninnu) GANA₂</p> <p>7'. 1(šar₂×geš₂) gal GANA₂</p> <p>8'. 1(šar₂×geš₂) gal šu nu-y GANA₂</p> |
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As photographed and drawn in Fig. 1a–d, the two damaged signs *x* and *y* that occur in the closing lines of these excerpts could well be tag (ŠUM); the first is badly abraded, the second compressed into a very full line. However, there are at least four further Old Babylonian metrological lists from Nippur which preserve the same lines more clearly and unequivocally show a different reading:⁵

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| <p>3. CBS 8214 rev. ii' (Type II; unpublished; Fig. 1e–f)</p> <p>1'. [. . .] ṛgur[†]</p> <p>2'. [. . .]+1(šar'u) gur</p> <p>3'. [. . .]+3(šar'u) gur</p> <p>4'. [. . .] gal-la gur</p> <p>5'. [. . .] ṛgal[†]-la ṛšu[†] nu-ṛgi₄[†] gur</p> <p>4. CBS 10181+CBS 10207+Ist Ni 10135 rev. i (Type II; Proust 2007: 353, pls. XLII–XLIII; Fig. 1g–i)⁶</p> <p>1'. [1(šar'u)] ṛ8(šar₂) gur[†]</p> <p>2'. 1(šar'u) 9(šar₂) gur</p> <p>3'. 1(šar₂×man) gur</p> | <p>4'. 1(šar₂×eš) gur</p> <p>5'. 1(šar₂×ilimmu) gur</p> <p>6'. 1(šar₂×ninnu) gur</p> <p>7'. 1(šar₂) gal gur</p> <p>8'. 1(šar₂) gal šu nu-gi₄ gur</p> <p>5. HS 249 obv. iv (Type I; Proust 2008a: no. 3; Fig. 1j–k)</p> <p>4. ṛ1(šar'u) 9(šar₂) ṛ gur</p> <p>5. ṛ1(šar₂×man) ṛ gur</p> <p>6. ṛ1(šar₂×eš) ṛ gur</p> <p>7. ṛ1(šar₂×ilimmu) ṛ gur</p> <p>8. 1(šar₂×ninnu) gur</p> <p>9. 1(šar₂×geš₂) gal-la gur⁷</p> |
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⁴ The sign transliterated here by šar'u_x comprises two concentric circular impressions with a KASKAL-like double-hatching over them.

⁵ The unpublished Philadelphia tablets were first catalogued and photographed by Robson in the late 1990s. A copy of the resulting database was given to Proust in May 2003 to help with her work on the Istanbul metrological tablets (Proust 2007). They were collated and rephotographed by Robson in September 2010, thanks to generous funding from the CSIC-funded research project *Libros, archivos y bibliotecas de la antigua Mesopotamia*, directed by Manuel Molina, Barbara Böck and Ignacio Márquez Rowe.

Márquez Rowe is currently preparing to publish all the Old Babylonian metrological tablets in Philadelphia. Photographs of all the Philadelphia tablets are scheduled to appear online at CDLI (<http://cdli.ucla.edu>) over the course of 2011–12, thanks to funding by the Mellon Foundation.

⁶ These lines are on the fragment CBS 10181.

⁷ Proust (2008a: 23) reads ll. 4–8 as: [1(šar'u)] gur, [2(šar'u)] gur, [3(šar'u)] gur, [4(šar'u)] gur, [5(šar'u)] gur, 1(šar₂) gal gur, although (traces of) the metrological units are clearly visible on the photograph reproduced on the accompanying CD-Rom; see Fig. 1j–k.

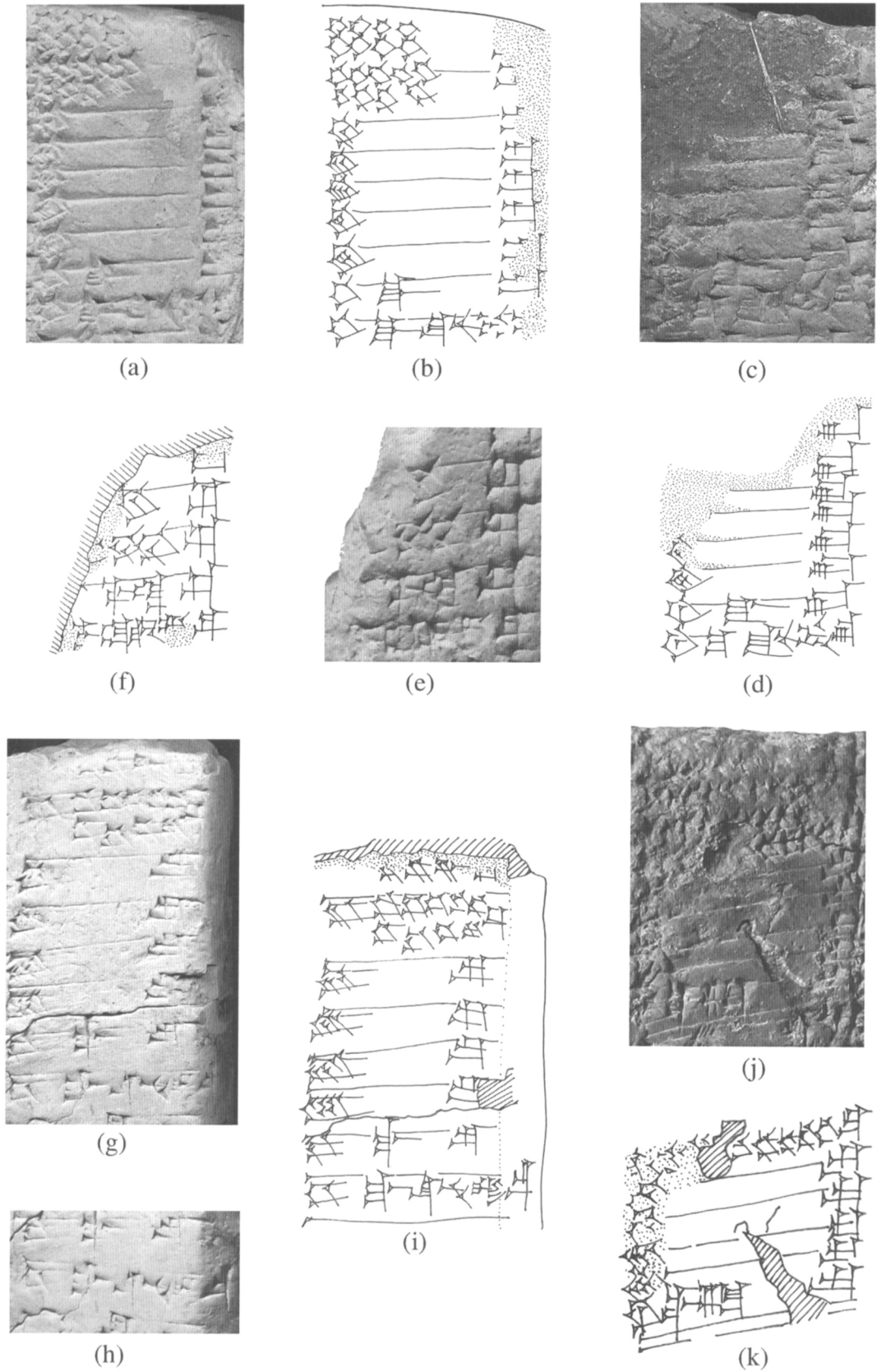


Fig. 1 Metrological lists Nos. 1–5. Photographs from CDLI, copies by Eleanor Robson.

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| <p>6. HS 249 rev. ii (Type I; Proust 2008a: no. 3; Fig. 2a–b)</p> <p>33'. 1(šar'u) 9(šar₂) GANA₂</p> <p>34'. 1(šar₂×man) GANA₂</p> <p>35'. 1(šar₂×eš) GANA₂</p> <p>36'. 1(šar₂×ilimmu) GANA₂</p> <p>37'. 1(šar₂×ninnu) GANA₂</p> <p>38'. 1(šar₂×geš₂) gal-la¹ {la} GANA₂'(DIŠ)</p> <p>39'. 1(šar₂×geš₂) gal-la¹ šu nu-gi₄⁸</p> | <p>7. Ist Ni 4840+UM 29-13-711 rev. v (Type II; Proust 2007: 343, pl. XXVI; Fig. 2c–e)⁹</p> <p>17'. 1(šar'u) 9(šar₂) gur¹</p> <p>18'. 1(šar₂×man)¹ gur</p> <p>19'. [1(šar₂×eš)] gur</p> <p>20'. [1(šar₂×ilimmu)] gur</p> <p>21'. [1(šar₂×ninnu)] gur</p> <p>22'. [1(šar₂)] gal-la gur</p> <p>23'. 1(šar₂) šu nu-gi₄</p> |
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In each instance, the sign following NU is clearly GI₄, a reading that would also comfortably fit the traces on both entries in CBS 10990 (Fig. 1a–d).¹⁰ As Mittermayer (2006: no. 214) shows, Old Babylonian cursive forms of GI₄ may omit the central upright wedges, as on CBS 10990 (see in particular Mittermayer's final two examples).

Unrepeatable?

What, then, does šu nu-gi₄ mean in this context? The basic sense of the Sumerian compound verb šu—gi₄ is “to repeat” (Karahashi 2000: 160). It is often equated with the Akkadian verb *šanû* “to do twice, repeat”, and also with *šullumu* “to repay” and *gimilla turru* “to avenge”. It is difficult to imagine a pertinent sense for the latter two translations within a metrological list, so we are left with the basic idea that 1(šar₂) šu nu-gi₄ is “unrepeatable”, i.e. cannot be reduplicated or multiplied.

But is the entry 1(šar₂) gal šu nu-gi₄ itself a metrological unit, as previous commentators have assumed, or just a comment on the unit 1(šar₂) gal(-la) in the preceding line? In two of the lists quoted above, Nos. 6 (HS 249) and 7 (UM 29-13-711, which also omits the word gal-la) the line does not end with a metrological unit as all the other lines in the text do, suggesting that this is a comment, not a unit. Conversely, the comparable lines in lists Nos. 3 (CBS 8124) and 4 (CBS 10181), as well as Nos. 1–2 (CBS 10990), do end with metrological units. The presence or absence of such a unit can easily be seen in Table 1.

Note too that the capacity list No. 5 (on HS 249) ends with 1(šar₂×geš₂) gal-la gur while the area list No. 6 (also on HS 249) ends with 1(šar₂×geš₂) gal-la GANA₂, 1(šar₂×geš₂) gal-la šu nu-gi₄. That is, the šu nu-gi₄ line is not entered consistently from list to list, even on the same tablet. Similarly, there is little consistency in the writing of the numeral before the GAL sign. While most tablets show 1(šar₂), lists Nos. 5–6 (HS 249 obv. iv and rev. ii), and No. 2 (CBS 10990 rev. iii, in contrast to obv. iii) clearly write 1(šar₂×geš₂), namely 1(šar₂) with the sign for sixty inscribed inside it.¹¹

Collectively these data thus suggest that the status of the šu nu-gi₄ line was ambiguous—or at least unclear to the trainee scribes of Old Babylonian Nippur. The apparent redundancy of the writing 1(šar₂×geš₂) gal-la in lists Nos. 6 (HS 249) and 7 (CBS 10990) highlights the confusion. However, it also appears significant that no known metrological list or table has any intermediate lines between 1(šar₂) gal(-la) and 1(šar₂) gal(-la) šu nu-gi₄, even though one could potentially add entries from 2(šar₂) gal to 5(šar'u) gal. On present evidence, then, it appears that the scribes who added a metrological unit to the end of the latter line did so inappropriately, and that we (and they) should really understand it as a statement that capacity and area metrologies were not extensible beyond 1(šar₂) gal. In other words, the phrase šu nu-gi₄ may have been a comment as much on the systems as a whole as on the particular unit with which they ended.

Looking at the Old Babylonian sources from places other than Nippur, we find substantial evidence to corroborate this hypothesis (see Table 2). BM 96949 is a Type I list of capacities, written

⁸ Proust (2008a: 24) reads ll. 38'–39' as: 1(šar₂) gal-la GANA₂, 1(šar₂) gal-la šu-nu-tag? GANA₂. However, in the published photograph we see traces of the head of GEŠ₂ inside both ŠAR₂ signs, a duplicated LA in l. 38' and no GANA₂ at the end of l. 39'.

⁹ These lines are on the fragment UM 29-13-711. Proust's copy (2007: pl. XXVI) shows very little in this final column, although most signs are in fact legible.

¹⁰ Proust (2007: 103) states that the tablet HS 224, a Type

III table of weights, also ends 1(šar₂) gal šu nu-tag gu₂. However, HS 224 is in fact a Type III table of square integers (Proust 2008a: no. 61) and none of the other Hilprecht Sammlung tablets published by her (Proust 2008a) fits this description; nor do any of the other known Old Babylonian Type III tablets from Nippur.

¹¹ However, for convenience, in general statements we shall continue to write 1(šar₂) gal for both 1(šar₂) gal and 1(šar₂×geš₂) gal.

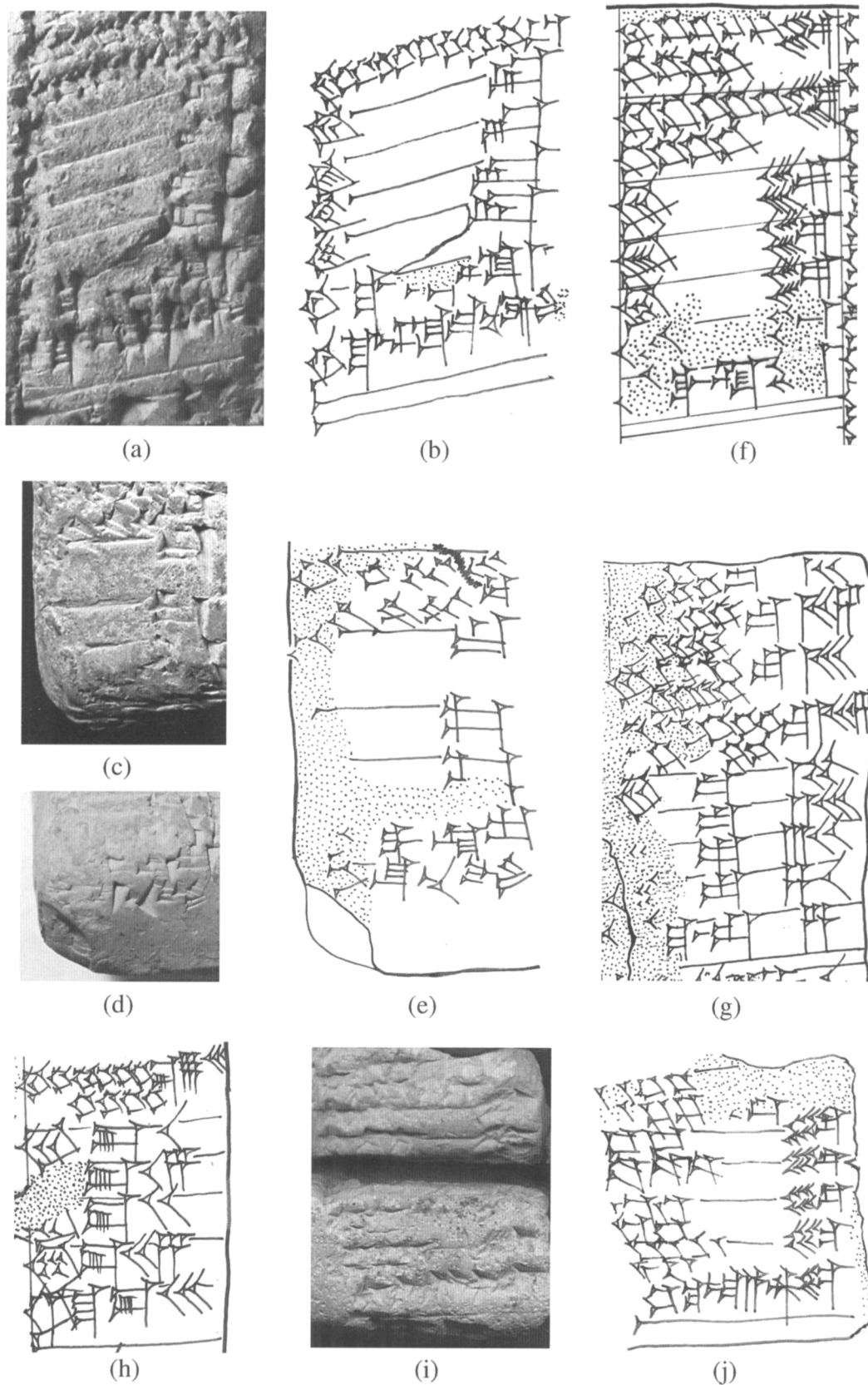


Fig. 2 Metrological lists Nos. 6–11. Photographs from CDLI, copies by Eleanor Robson.

TABLE 1: šu nu-gi₄ phrases in capacity and area lists from Old Babylonian Nippur, with and without a metrological unit.

Phrase	Source
1(šar ₂ ×geš ₂) gal šu nu-gi ₄ UNIT	No. 2 (CBS 10990 rev. iii)
1(šar ₂) gal šu nu-gi ₄ UNIT	Nos. 4 (CBS 10181), 1 (CBS 10990 obv. iii)
[. . .] gal-la šu nu-gi ₄ UNIT	No. 3 (CBS 8214)
1(šar ₂ ×geš ₂) gal-la šu nu-gi ₄	No. 6 (HS 249 rev. ii)
1(šar ₂) šu nu-gi ₄	No. 7 (UM 29-13-711)

TABLE 2: The final entries of Old Babylonian capacity and area lists known from places other than Nippur.

Phrase	Source
1(šar ₂ ×geš ₂) gal UNIT	Nos. 9–10 (YBC 2392); No. 14 (Ash 1931.137)
1(šar ₂ ×geš ₂ [?]) gal-la UNIT	No. 8 (BM 96949)
1(šar ₂) gal-la-am ₃ UNIT	Nos. 11–12 (CBS 472)
1(šar ₂) šu-ši UNIT	No. 15 (VA 2596)

by a scribe named ʾarīdum,¹² “Fugitive”, in Samsu-iluna year 14 (*ca* 1735 BCE by the middle chronology) probably in Sippar. It ends, like the capacity list No. 5 (HS 249 obv. iv), without a šu nu-gi₄ statement:

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| 8. BM 96949 rev. iii (Type I; Robson 2004: 35–7; Fig. 2f) | 4. 1(šar ₂ ×eš) še-gur |
| 1. 1(šar ^u) 8(šar ₂) še-gur | 5. 1(šar ₂ ×ilimmu) še-gur |
| 2. 1(šar ^u) 9(šar ₂) še-gur | 6. ʾ1(šar ₂ ×ninnu) ʾ še-gur |
| 3. 1(šar ₂ ×man) še-gur | 7. ʾ1(šar ₂ ×geš ₂ [?]) ʾ gal-la še-gur |

The capacity and area tables on the Type I prism YBC 2392 (Appendix 1), which may be from Larsa, similarly end with [1(šar₂×geš₂[?])] gal gur and 1(šar₂×geš₂) gal GANA₂ respectively:

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| 9. YBC 2392 col. v (Appendix 1; Fig. 2g) | 10. YBC 2392 col. xi (Appendix 1; Fig. 2h) |
| 4. 1(šar ^u) 9(šar ₂) gur 1 35 | 24. 1(šar ^u) 9(šar ₂) GANA ₂ 9 30 |
| 5. ʾ1(šar ₂ ×man) ʾ gur 1 40 | 25. 1(šar ₂ ×man) GANA ₂ 10 |
| 6. ʾ1(šar ₂ ×eš) ʾ gur 2 30 | 26. [1(šar ₂ ×eš)] GANA ₂ 15 |
| 7. ʾ1(šar ₂ ×ilimmu) ʾ gur 3 20 | 27. [1(šar ₂ ×ilimmu)] GANA ₂ 20 |
| 8. ʾ1(šar ₂ ×ninnu) ʾ gur 4 10 | 28. 1(šar ₂ ×ninnu) GANA ₂ 25 |
| 9. [1(šar ₂ ×geš ₂ [?])] gal gur 5 | 29. 1(šar ₂ ×geš ₂) gal GANA ₂ 30 |

Further, the relevant lists on the unpublished Type I tablet CBS 472+ (from the Khabaza collection, perhaps from late Old Babylonian Sippar but certainly not from Nippur) end with 1(šar₂) gal-la-am₃ še-gur and 1(šar₂) gal-la-am₃ GANA₂ a-ša₃ respectively:

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| 11. CBS 472+ obv. iii (unpublished; Fig. 2i–j) | 12. CBS 472+ rev. iv (unpublished; Fig. 3a–b) |
| 31'. ʾ1(šar ^u _x) 9(šar ₂) še-gur ¹³ | 14. 1(šar ^u _x) 9(šar ₂) GANA ₂ a-ša ₃ |
| 32'. 2(šar ^u _x) še-gur | 15. 2(šar ^u _x) GANA ₂ a-ša ₃ |
| 33'. 3(šar ^u _x) še-gur | 16. 3(šar ^u _x) GANA ₂ a-ša ₃ |
| 34'. 4(šar ^u _x) še-gur | 17. 4(šar ^u _x) GANA ₂ a-ša ₃ |
| 35'. 5(šar ^u _x) še-gur | 18. 5(šar ^u _x) GANA ₂ a-ša ₃ |
| 36'. 1(šar ₂) gal-la-am ₃ še-gur | 19. 1(šar ₂) gal-la-am ₃ GANA ₂ a-ša ₃ |

¹² Not Ardam, as tentatively proposed in Robson (2004: 35). We are grateful to Frans van Koppen (pers. comm., 20 October 2009) for the correct reading.

¹³ On this tablet, the sign šar^u_x is not ŠAR₂×U but simply a larger version of ŠAR₂.

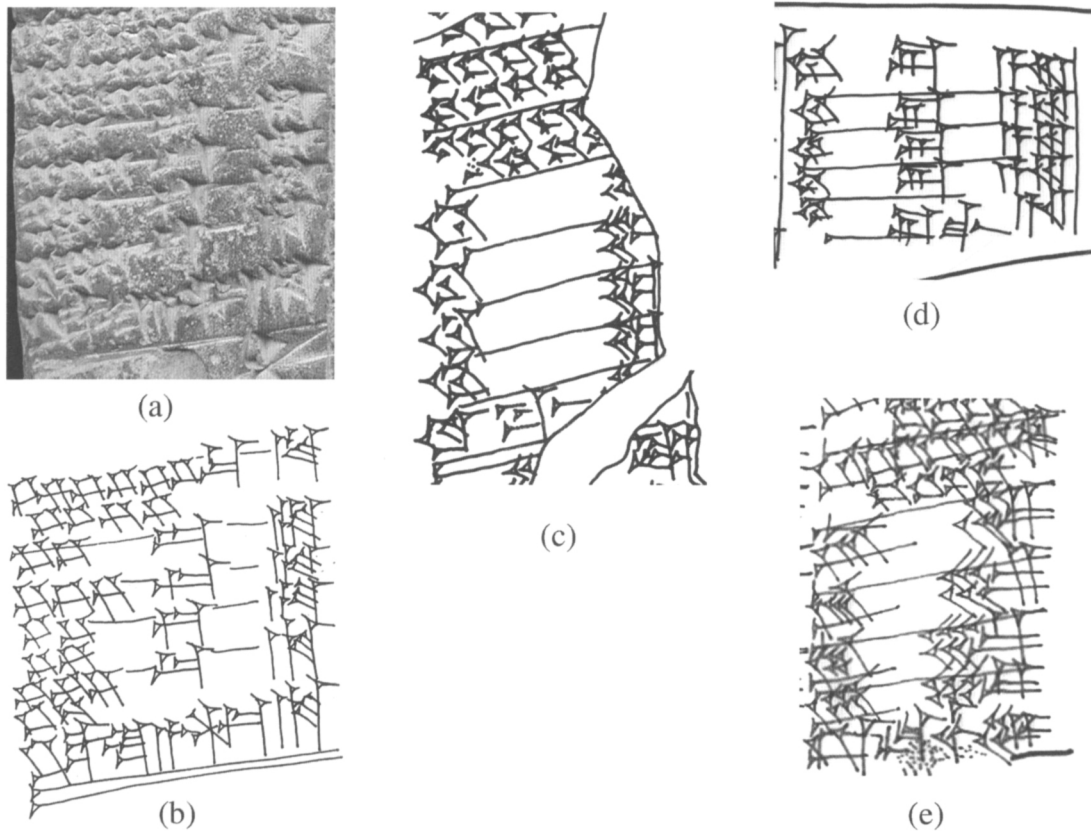


Fig. 3 Metrological lists Nos. 12–15. Photographs from CDLI, copies by Eleanor Robson.

The capacity and area lists on the Type I tablet Ashmolean 1931.137 (Robson 2004: 30–35), possibly from Kish, are not very competently written. The former finishes with $1(\text{šar}_2 \times \text{man}) + \text{diš gal gur}$ and the latter with $1(\text{šar}'\text{u}) \text{GANA}_2 \text{ gal a-ša}_3$, both after four or five repetitions of $1(\text{šar}'\text{u})$ UNIT. However badly the scribe misinterpreted the sequence of numerals represented by lists Nos. 1–2 (CBS 10990), 4 (CBS 10181), 5–6 (HS 249), 8 (BM 96949) and 9–10 (YBC 3292), it is clear that he took a unit equivalent to $1(\text{šar}_2)$ gal to be the largest unit of both the area and the capacity systems.

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| <p>13. Ash 1931.137 obv. iv (Robson 2004: 31; Fig. 3c)</p> <p>23. $8(\text{šar}_2)$ [še-gur]</p> <p>24. $9(\text{šar}_2)$ [še-gur]</p> <p>25. $1(\text{šar}'\text{u})$ še-[gur]</p> <p>26. $1(\text{šar}'\text{u})$ še-rgur¹</p> <p>27. $1(\text{šar}'\text{u})$ še-gur</p> <p>28. $1(\text{šar}'\text{u})$ še-gur</p> <p>29. $1(\text{šar}_2 \times \text{man}) + \text{diš gal rše-gur}^1$</p> | <p>14. Ash 1931.137 left edge iii (Robson 2004: 34; Fig. 3d)</p> <p>1. $1(\text{šar}'\text{u}) \text{GANA}_2 \text{ a-ša}_3$</p> <p>2. $1(\text{šar}'\text{u}) \text{GANA}_2 \text{ a-ša}_3$</p> <p>3. $1(\text{šar}'\text{u}) \text{GANA}_2 \text{ a-ša}_3$</p> <p>4. $1(\text{šar}'\text{u}) \text{GANA}_2 \text{ a-ša}_3$</p> <p>5. $1(\text{šar}'\text{u}) \text{GANA}_2 \text{ gal a-ša}_3$</p> |
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Finally, and perhaps most interestingly, the capacity list on the unprovenanced Type I cylinder VA 2596 (Meissner 1893: pl. 58 and below, Appendix 2), writes $1(\text{šar}_2) 1 \text{šu-ši gur}$ “sixty šar_2 gur” as an alternative writing for $1(\text{šar}_2)$ gal gur:

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| <p>15. VA 2596 col. viii (Fig. 3e)</p> <p>10. $1(\text{šar}'\text{u}) 9(\text{šar}_2)$ še-gur</p> <p>11. $1(\text{šar}_2 \times \text{man})$ še-gur</p> <p>12. $1(\text{šar}_2 \times \text{eš})$ še-gur</p> | <p>13. $1(\text{šar}_2 \times \text{ilimmu})$ še-gur</p> <p>14. $1(\text{šar}_2 \times \text{ninnu})$ še-gur</p> <p>15. $1(\text{šar}_2 \times \text{geš}_2)$ ršu-ši še-gur</p> |
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In sum, then, it appears that the upper ends of the Old Babylonian capacity and area systems were not, after all, considered to be “untouchable” but rather “unrepeatable”; and that the “large šar₂”, at sixty times the šar₂, was their largest unit, not any unit sixty times bigger than that. This brings them back into line with the weight system which, it is agreed (e.g. Proust 2007: 313), also stops at 1(šar₂) gal.

Unsurpassable?

Finally, we should consider these units in real-world terms, in relation to modern measures and to early Mesopotamian school and scribal practice. In the area system, 1(šar₂) gal is 3600 (60²) times larger than 1(bur₃), roughly 235 km² (Powell 1987–90: 480–81). In the capacity system, 1(šar₂) gal is 216,000 (60³) times larger than 1 gur, just over one million litres or 1000 m³ (Powell 1987–90: 497–98). These units would have been more than adequate for all possible practical needs, as evidenced by the fact that they rarely, if ever (to our knowledge), appear in early Mesopotamian training exercises and administrative records.

Within the small Sargonic mathematical corpus, comprising around twenty tablets, three word-problems from Girsu or its vicinity involve finding the areas of very large squares, using the 1(šar₂) gal unit (Foster and Robson 2004: 2; Robson 2008: 56, 303–4).¹⁴ In the much larger Old Babylonian corpus of over a thousand tablets, by contrast, the largest square area calculated is just 1(bur₃) 2(eše₃) 4(iku) GANA₂ (NCBT 1913, ed. Neugebauer and Sachs 1945: 10; Robson 2008: 18). There are no Sargonic or Old Babylonian word-problems or calculations about particularly large capacity measures.

A similar pattern appears in the early Mesopotamian administrative record. A search of the CDLI database revealed no usages of the phrases šu nu-tag or šu nu-gi₄ in metrological contexts, and no especially large capacity measures.¹⁵ Sargonic accounts apparently use no area or capacity units larger than the šar₂.¹⁶ From the Ur III period just fifteen or so agricultural accounts from Girsu record area measures in units of 1(šar₂) gal, the largest of which—over 9(šar₂) gal—is in fact the total area of land cultivated over a decade, not in a single year.¹⁷ In the absence of a unified online corpus, the administrative documents of the Old Babylonian period are harder to survey with confidence, and an exhaustive search of the relevant literature would go far beyond the constraints of this article, but, just as in the Sargonic period, we have found no area units larger than the šar₂. Indeed, given the decentralised nature of administration at this time, and the concomitantly smaller areas of land managed institutionally, we should not expect to find metrological units in use that were larger than those of the Ur III period.¹⁸

¹⁴ A 5443 (Whiting 1984: 60) finds a square area of over 1(šar₂) gal, or just under 280 km². PUL 28 (*DPA* 37, Limet 1973) finds an area of more than 2(šar₂) gal, roughly 550 km². Ash 1924.689 (*MAD* 5 112) finds an area larger than 7(šar₂) gal, written erroneously as 7(šar₂).LIL₂, approximately 1800 km².

¹⁵ <http://www.cdli.ucla.edu/cdlisearch/search/index.html>, accessed 1 January 2011.

¹⁶ The largest area recorded on the Obelisk of Maništušu (*OIP* 104 40) is 9(šar₂) 3(iku) GANA₂. The tablet YBC 8460 (*BIN* 8 198, unprovenanced) totals three areas as rather more than 7(šar₂), written erroneously as 1(bur'u) 6(šar₂), while IM 50603 (*HSS* 10 133) from Gasur apparently records a capacity measure of at least 2(šar₂) 6(geš₂). As both are badly written and lack administrative detail it is possible that they are not in fact administrative records but scribal exercises (see Robson 2008: 58 for relevant criteria).

¹⁷ BM 18060 (Maekawa 1981: 50 no. 1) is a 10-year summary of agricultural accounts, from Shulgi 42 to Amar-Suen 3, over a total area of more than 9(šar₂) gal or about 2,200 km². Similarly, all the other very large units appear to be theoretical areas—expressions of agricultural work owed

or completed—rather than actual areas under cultivation (see Englund 1991 on the principles and practice of Ur III labour accounts; Maekawa 1981; 1990 on Ur III agricultural accounts; Robson 2008: 69–73 for a worked example). AO 3448 (*RTC* 407; Nissen, Damerow and Englund 1993: 140–42), also a Girsu agricultural account, calculates a theoretical amount of grain owed at over 3(šar'u) 4(šar₂) gur, about 440,000 litres.

¹⁸ We are very grateful to Frans van Koppen for his help on this matter; he draws our attention to *UET* 5 666, an account of the god Nanna's estate near Ur, which records an area of 3(šar₂) 5(bur₃) GANA₂ (Butz 1979: 323–25). Similarly, *BIN* 7 161 from Larsa describes a field of 3(šar₂) GANA₂ exactly (Walters 1970: no. 24), while Mauer (1987) no. 50, from Sin-kashid's palace in Uruk, lists an area of 2(šar₂) 4(bur'u) 3(bur₃) GANA₂ (Renger 1995: 158). These areas are all in the range 11–14 km². The largest Old Babylonian area measure known to van Koppen is in *ARMT* 23 464 from Mari, where 37,890 iku (just under 140 km²) is written decimally as 3 GAL 7 li-mi 8 ME 90 IKU, equivalent in Old Babylonian metrological units to 3(šar'u) 5(šar₂) 5(bur₃).

It turns out, then, that it was not strictly true that 1(šar₂) gal was “unrepeatable” in the sense of “unsurpassable”. On rare occasions, in both training and professional contexts, the šAR₂ sign could be replicated up to nine times—but could never, it appears (on current evidence), be followed by a larger unit. It was, for all intents and purposes, the upper end of the area and capacity measuring systems in both theory and practice in early Mesopotamia.

Conclusion

On re-examination, the large metrological unit 1(šar₂) šu nu-tag, “1 šar₂ that the hand cannot touch”, appears to be an artefact of the mid-twentieth century, not a historically attested area or capacity measure of the Old Babylonian period. It seems to have been created through a desire to create continuity with the still-enigmatic Eblaite phrase nu-da-šid “uncountable” or “unsayable”, attested several hundred years earlier and from a very particular culture of cuneiform literacy. Now that further, better-preserved examples of the phrase have come to light, and we have the means to relate school exercises to contemporary scribal practice, this apparently “untouchable” metrological unit recedes further from our grasp. Instead we are left with a rather smaller area or capacity measure, which is nevertheless at the upper end of professional utility, and the comment that it is (usually) “unrepeatable” or as large as one practically needs.

Further, it is now clear that in Old Babylonian school contexts—but not in earlier administrative practice—the correct (or at least majority) sequence of the six very largest units comprises a single šAR₂ sign inscribed with the numerals 10, 20, 30, 40, 50 and 60 (i.e. u, man, eš, ilimmu, ninnu, geš₂) respectively. Thus an alternative (or additional) hypothesis presents itself: the “unrepeatability” may equally refer to the way these signs are written. In the middle and upper ranges of the area and the capacity series, quantity and unit are bundled into a single grapheme, just as must have been the case with their precursors, the preliterate accounting tokens (cf. Nissen, Damerow and Englund 1993). The bundled graphemes are repeated as needed; for instance, the quantity “five šar₂” is not written with the numeral 5 followed by the unit sign šAR₂ but as five šAR₂ signs one after another (transliterated as 5(šar₂)). By contrast, the correct writing of “twenty šar₂” seems not to have been the repeated 20(šar₂) or 2(šar’u) but the unrepeated 1(šar₂×20). Could the phrase šu nu-gi₄ have simply been a reminder to the trainee scribes of Nippur that at the upper end of the area and capacity series they were not to carry on as before? If so, it seems that it was only the scribe of list No. 3 (CBS 8214, Fig. 1e–f) who did not do as he was told.

We have proposed several possible meanings for the phrase šu ni-gi₄: graphical, conceptual and utilitarian. On current evidence, much of it written by learners with varying degrees of scribal competence, we are reluctant to choose definitively between them. Indeed, the definitive, “correct” interpretation of šu nu-gi₄ may never be found, just as it is futile to try recover the “original” meanings of other multivalent scribal exercises of early Mesopotamia, whether lexical or literary. The wide variety of writing conventions we have presented here suggests likewise that šu nu-gi₄ took on different meanings for different individuals and scribal groups, depending on their degree of literacy and numeracy, and on local traditions of interpretation.

Appendix 1: YBC 2392

YBC 2392 is a four-sided prism, approximately 22 cm high and 10 cm wide, with a cylindrical hole of ca 15 mm diameter running through its centre. The top of the prism is badly abraded but the bottom is lightly marked with four lines, each running from the hole to a corner of the tablet (Fig. 4).

Each of the four faces is divided into two or three columns containing three Old Babylonian metrological tables in the standard order (Figs. 5–8): capacity measures (i 1–v 8), weights (v 9–viii 13), and areas (viii 14–end). It concludes with a catchline to the next table in the series, that on lengths, and the date 26 7ebētu but otherwise has no colophon. The numerals 4, 7 and 8 are written “non-mathematically” in both sides of the table: that is, with two rows of wedges, not three.

The tablet was copied and photographed by Eleanor Robson in November 2006. We are grateful to Professor Benjamin R. Foster for permission to publish and to Ulla Kasten for her ever-generous assistance in the Babylonian Collection at Yale University.

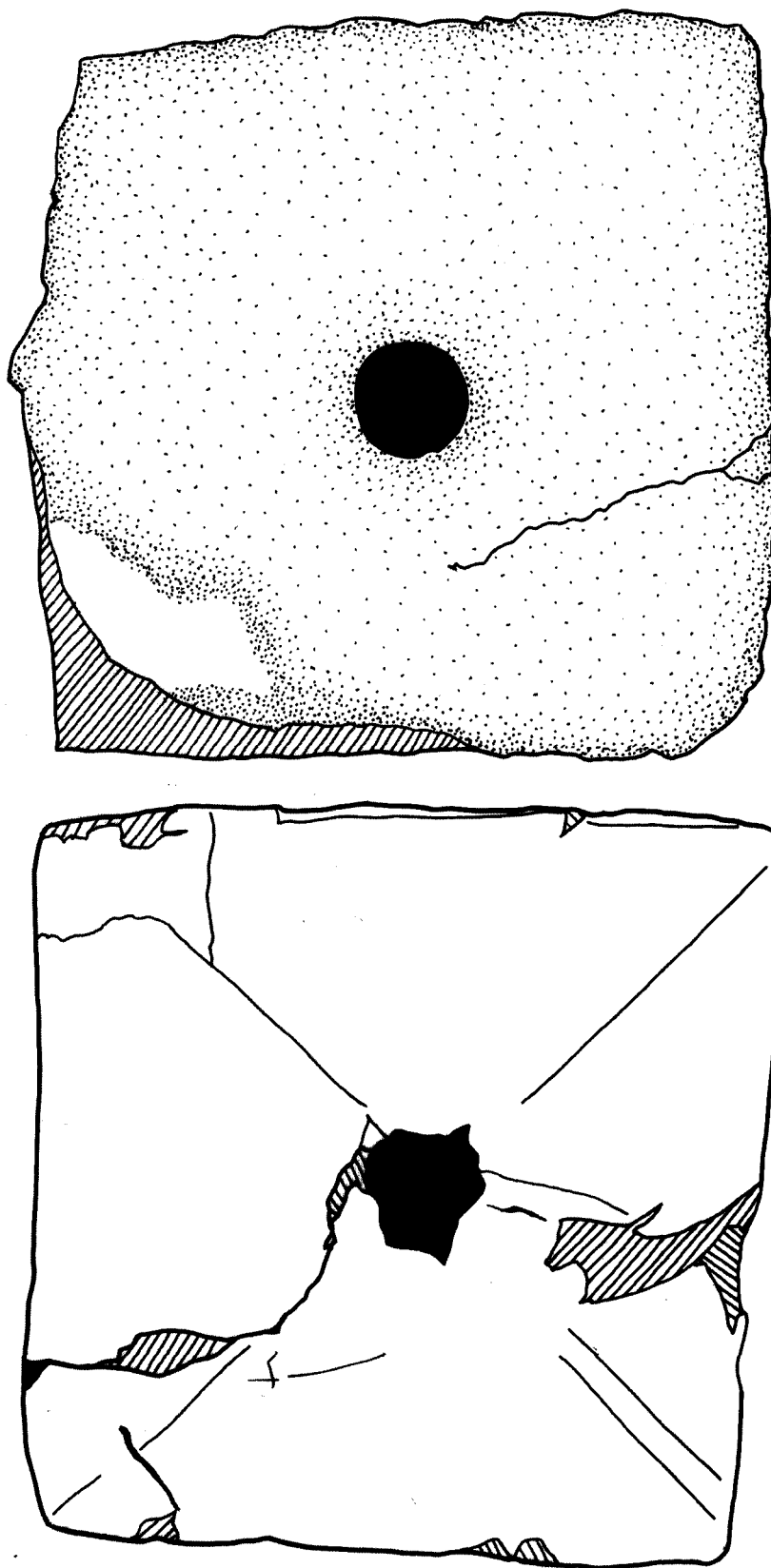


Fig. 4 Prism YBC 2392 top and bottom. Copy by Eleanor Robson.

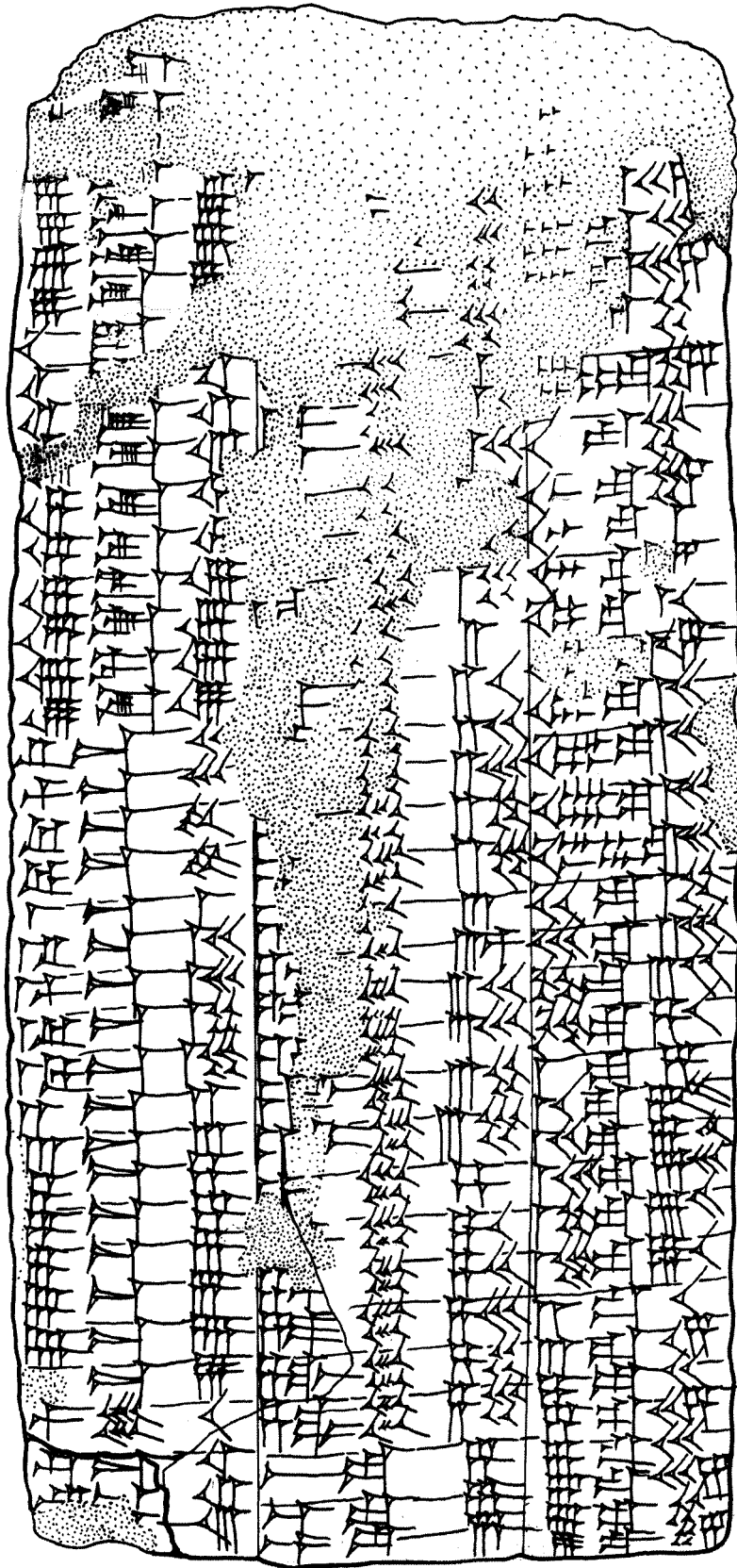


Fig. 5 Prism YBC 2392 side a cols. i-iii. Copy by Eleanor Robson.

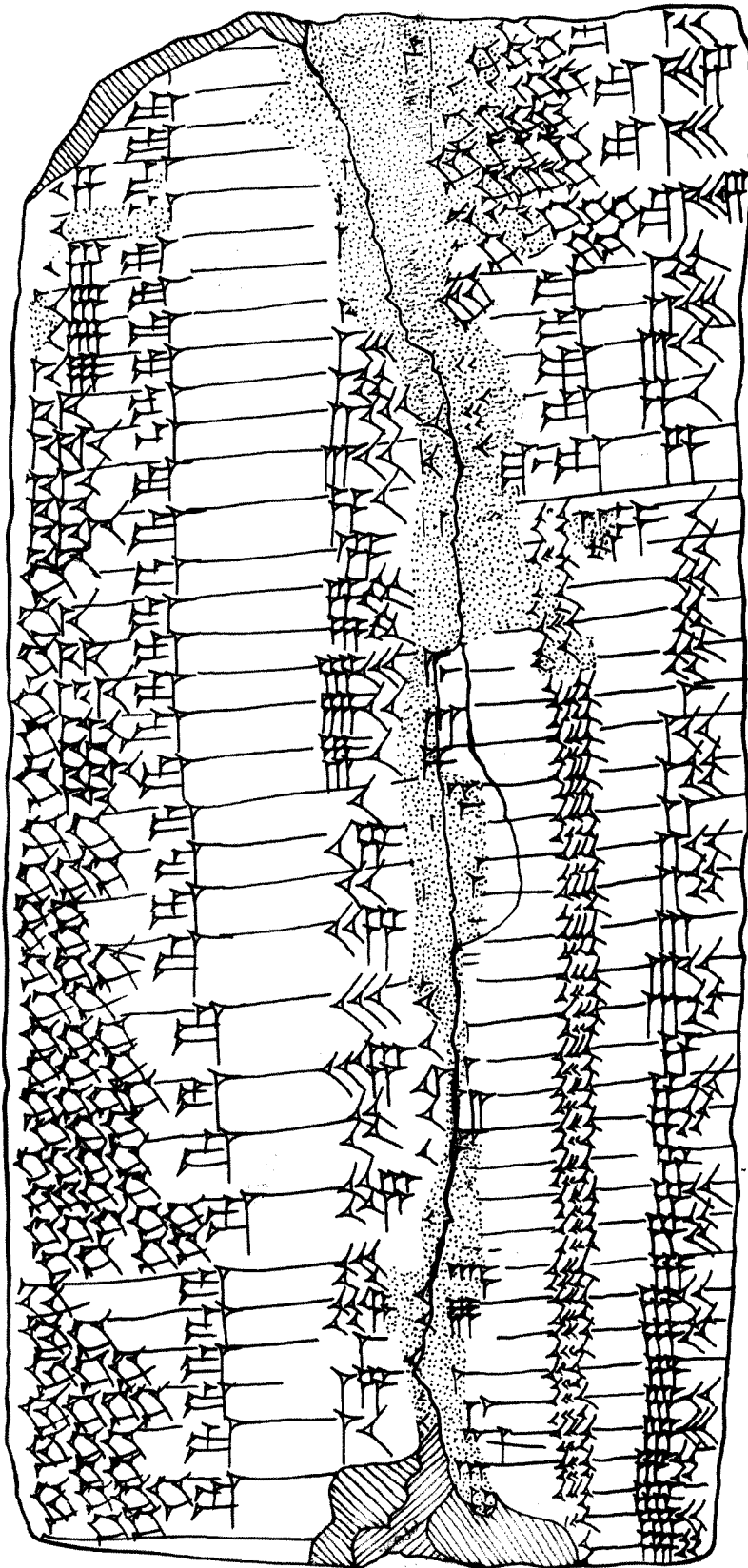


Fig. 6 Prism YBC 2392 side b cols. iv–v. Copy by Eleanor Robson.



Fig. 7 Prism YBC 2392 side c cols. vi-viii. Copy by Eleanor Robson.

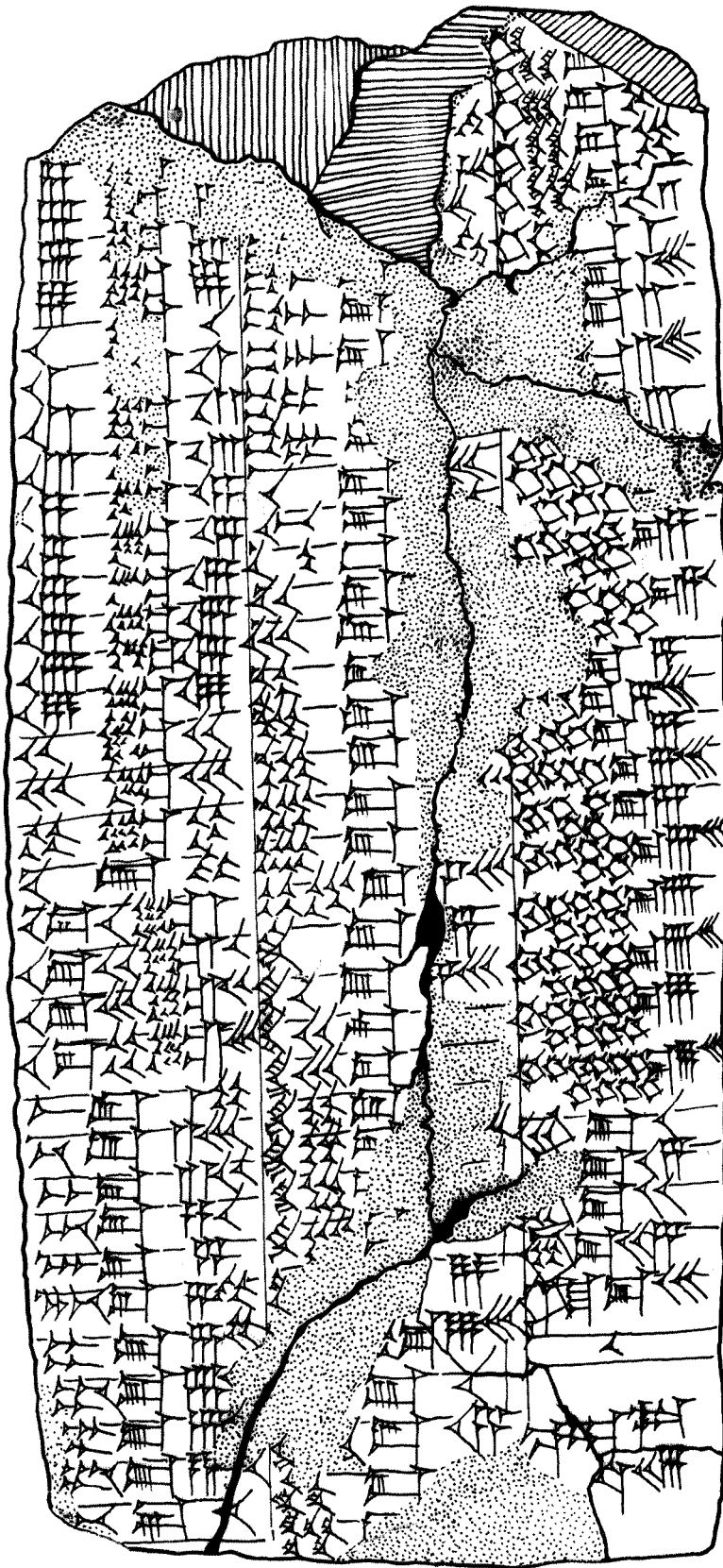


Fig. 8 Prism YBC 2392 side d cols. ix–xi. Copy by Eleanor Robson.

<i>Side a col. i</i>		<i>Side a col. ii</i>		<i>Side a col. iii</i>	
[1 gin ₂	1]	<i>Top of column badly abraded</i>		[1(aš) 3(barig) gur	8]
[2] rgin ₂	[2]	[1(ban ₂) 4 sila ₃	14]	[1(aš) 4(barig) gur	9]
[3] rgin ₂	[3]	[1(ban ₂) 5 sila ₃	15]	[2(aš) gur	10]
[4] rgin ₂	[4]	[1(ban ₂) 6 sila ₃	16]	[3(aš) gur	15]
5 rgin ₂	5 ¹	[1(ban ₂) 7 sila ₃	17]	[4(aš) gur	20]
6 gin ₂	6	[1(ban ₂) 8 sila ₃	18]	[5(aš) gur]	r25 ¹
7 gin ₂	7	[1(ban ₂) 9 sila ₃	19]	[6(aš)] rgur ¹	30
8 gin ₂	8	[2(ban ₂) še	20]	7 rgur ¹	35
9 gin ₂	9	[3(ban ₂) še	30]	8(aš) rgur ¹	40
10 gin ₂	[10]	[4(ban ₂) še	40]	r9(aš) ¹ gur	45
11 rgin ₂	11	[5(ban ₂) še	50]	[1(u)] rgur ¹	50
12 gin ₂	12	[1(barig) še	1]	r1(u) 1(aš) gur ¹	55
[13] gin ₂	13	[1(barig) 1(ban ₂) še	1 10]	r1(u) 2(aš) gur	1 ¹
14 gin ₂	r14 ¹	[1(barig) 2(ban ₂) še	1 20]	r1(u) 3(aš) gur	1 05 ¹
15 gin ₂	r15 ¹	[1(barig) 3(ban ₂) še	1 30]	r1(u) 4(aš) gur	1 10 ¹
16 gin ₂	16	[1(barig) 4(ban ₂) še	1 40]	r1(u) 5(aš) gur	1 15 ¹
17 gin ₂	17	[1(barig) 5(ban ₂) rše	1 50 ¹	r1(u) 6(aš) gur	1 20 ¹
18 gin ₂	18	[2(barig)] rše	2 ¹	1(u) 7(aš) rgur	1 25 ¹
19 gin ₂	19	[2(barig)] r1(ban ₂) še ¹	2 10	1(u) 8(aš) gur	1 30
½ sila ₃	20	[2(barig) 2(ban ₂) rše ¹	2 20	1(u) 9(aš) gur	1 35
½ sila ₃	30	[2(barig) 3(ban ₂) rše ¹	2 30	2(u) gur	1 40
¾ sila ₃	40	r2(barig) 4(ban ₂) še ¹	2 40	3(u) gur	2 30
¾ sila ₃	50	2(barig) r5(ban ₂) ¹ še	2 50	4(u) gur	3 20
1 sila ₃	1	3(barig) rše ¹	3	5(u) gur	4 10
1 ⅓ sila ₃	1 20	3(barig) [1(ban ₂)] še	3 10	1(geš ₂) gur	5
1 ½ sila ₃	1 30	3(barig) [2(ban ₂)] še	3 20	1(geš ₂) 1(u) gur	5 50
1 ⅔ sila ₃	1 40	3(barig) [3(ban ₂)] še	3 30	1(geš ₂) 2(u) gur	6 40
1 ⅝ sila ₃	1 50	3(barig) r4(ban ₂) ¹ še	3 40	1(geš ₂) 3(u) gur	7 30
2 sila ₃	2	3(barig) r5(ban ₂) ¹ še	3 50	1(geš ₂) 4(u) gur	8 20
3 sila ₃	3	r4(barig) ¹ še	4	1(geš ₂) 5(u) gur	9 10
4 sila ₃	4	[4(barig)] r1(ban ₂) ¹ še	4 10	2(geš ₂) gur	10
5 sila ₃	5	4(barig) r2(ban ₂) ¹ še	4 20	3(geš ₂) gur	15
6 sila ₃	6	4(barig) 3(ban ₂) še	4 30	4(geš ₂) gur	20
7 sila ₃	7	4(barig) 4(ban ₂) še	4 40	5(geš ₂) gur	25
8 sila ₃	8	4(barig) 5(ban ₂) še	4 50	6(geš ₂) gur	30
r9 sila ₃	9	1(aš) gur	5	7(geš ₂) gur	35
1(ban ₂) še	10	1(aš) 1(barig) gur	6	8(geš ₂) gur	40
1(ban ₂) 1 sila ₃	11	1(aš) 2(barig) gur	7	9(geš ₂) gur	45
1(ban ₂) 2 sila ₃	12				
1(ban ₂) 3 sila ₃	13				

Side b col. iv

[1(geš ¹ u) gur	50]
[11(geš ₂) gur	55]
1(geš ¹ u) 2(geš ₂) rgur ¹	[1]
1(geš ¹ u) 3(geš ₂) rgur ¹	[1 05]
1(geš ¹ u) 4(geš ₂) rgur ¹	[1 10]
[1(geš ¹ u) 5(geš ₂)] rgur ¹	[1 15]
r1(geš ¹ u) 6(geš ₂) ¹ gur	[1 20]
1(geš ¹ u) 7(geš ₂) gur	[1 25]
1(geš ¹ u) 8(geš ₂) gur	[1 30]
1(geš ¹ u) 9(geš ₂) gur	r1 35 ¹
2(geš ¹ u) gur	1 40
3(geš ¹ u) gur	2 30
4(geš ¹ u) gur	3 20
5(geš ¹ u) gur	4 10
1(šar ₂) gur	5
1(šar ₂) 1(geš ¹ u) gur	5 50
1(šar ₂) 2(geš ¹ u) gur	6 40

Side b col. v

1(šar ¹ u) 6(šar ₂) gur	1 20
1(šar ¹ u) 7(šar ₂) gur	1 25
1(šar ¹ u) 8(šar ₂) gur	1 30
1(šar ¹ u) 9(šar ₂) gur	1 35
r1(šar ₂ ×man) ¹ gur	1 40
r1(šar ₂ ×eš) ¹ gur	2 30
r1(šar ₂ ×ilimmu) ¹ gur	3 20
r1(šar ₂ ×ninnu) ¹ gur	4 10
[1(šar ₂ ×geš ₂ ?) gal gur	5
[½] rše kug-babbar ¹	10
[1] še	20
[1 ½] še	30
[2] še	40
[2 ½] še	50
[3] še	1
[4] še	1 20
[5] še	1 40

<i>Side b col. iv</i>		<i>Side b col. v</i>	
1(šar ₂)3(geš'u) gur	7 30	[6] še	2
1(šar ₂)4(geš'u) gur	8 20	[7] še	2 20
1(šar ₂)5(geš'u) gur	9 10	[8] še	2 40
2(šar ₂) gur	10	ṛ9ṛ še	3
3(šar ₂) gur	15	ṛ10ṛ še	3 20
4(šar ₂) gur	20	ṛ11ṛ še	3 40
5(šar ₂) gur	25	ṛ12ṛ še	4
6(šar ₂) gur	30	ṛ13ṛ še	4 20
7(šar ₂) gur	35	[14] še	4 40
8(šar ₂) gur	40	[15] še	5
9(šar ₂) gur	45	[16] še	5 20
1(šar'u) gur	50	[17] še	5 40
1(šar'u) 1(šar ₂) gur	55	ṛ18ṛ še	6
1(šar'u) 2(šar ₂) gur	1	ṛ19ṛ še	6 20
1(šar'u) 3(šar ₂) gur	1 05	[20] še	6 40
1(šar'u) 4(šar ₂) gur	1 10	[21] še	7
1(šar'u) 5(šar ₂) gur	[1 15]	[22] še	7 20
		[22] ½ še	7 30
		[23] še	7 40
		[24] še	8
		[25] še	8 20
		[26] še	8 40

<i>Side c col. vi</i>		<i>Side c col. vii</i>		<i>Side c col. viii</i>	
27 še	9	1 [ma-na	1]	[1(u) 2(aš) gu ₂	12]
28 še	9 20	1 ½ [ma-na	1;20]	[1(u) 3(aš) gu ₂	13]
29 še	9 40	1 ½ ma-na	ṛ1;30ṛ	ṛ1(u) 4(aš)ṛ [gu ₂	14]
igi-6-gal ₂	10	1 ⅔ ma-na	1;40	ṛ1(u) 5(aš)ṛ [gu ₂	15]
igi-6-gal ₂ 5	11 40	1 ⅝ ma-na	1;50	1(u) 6(aš) gu ₂	16
igi-6-gal ₂ 10	13 20	2 ma-na	2	1(u) 7(aš) gu ₂	17
igi-4-gal ₂	15	3 ma-na	3	1(u) 8(aš) gu ₂	18
igi-4-gal ₂ 5	16 40	4 ma-na	4	1(u) 9(aš) gu ₂	19
igi-4-gal ₂ 10	18 20	5 ma-na	5	2(u) gu ₂	20
½ gin ₂	20	6 ma-na	6	3(u) gu ₂	30
⅓ gin ₂	30	7 ma-na	7	4(u) gu ₂	40
⅔ gin ₂	40	8 ma-na	8	5(u) gu ₂	50
⅝ gin ₂	50	9 ma-na	9	1(šar ₂) gu ₂ kug-babbar	1
1 gin ₂	1	10 ma-na	10	1 gin ₂ ṛsarṛ	1
1 gin ₂ igi-6-gal ₂	1 10	11 ma-na	11	2 gin ₂	2
1 gin ₂ igi-4-gal ₂	1 15	12 ma-na	12	3 gin ₂	3
1 ⅓ gin ₂	1 20	13 ma-na	13	4 gin ₂	4
1 ½ gin ₂	1 30	14 ma-na	14	5 gin ₂	5
1 ⅔ gin ₂	1 40	15 ma-na	15	6 gin ₂	6
1 ⅝ gin ₂	1 50	16 ma-na	16	7 gin ₂	7
2 gin ₂	2	17 ma-na	17	8 gin ₂	8
3 gin ₂	3	18 ma-na	18	9 gin ₂	9
4 gin ₂	4	19 ma-na	19	10 gin ₂	10
5 gin ₂	5	20 ma-na	20	11 gin ₂	11
6 gin ₂	6	30 ma-na	30	12 gin ₂	12
7 gin ₂	7	40 ma-na	40	13 gin ₂	13
8 gin ₂	8	50 ma-na	50	14 gin ₂	14
9 gin ₂	9	1(aš) gu ₂	1	15 gin ₂	15
10 gin ₂	10	1(aš) gu ₂ 10 ma-na	1 10	16 gin ₂	16
11 gin ₂	11	1(aš) gu ₂ 20 ma-na	1 20	17 gin ₂	17
12 gin ₂	12	1(aš) gu ₂ 30 ma-na	1 30	18 gin ₂	18
13 gin ₂	13	1(aš) gu ₂ 40 ma-na	1 40	19 gin ₂	19
14 gin ₂	14	1(aš) gu ₂ 50 ma-na	1 50	½ sar	20
15 gin ₂	15	2(aš) gu ₂	2	½ sar	30
16 gin ₂	16	3(aš) gu ₂	3	⅔ sar	40

<i>Side c col. vi</i>		<i>Side c col. vii</i>		<i>Side c col. viii</i>	
17 gin ₂	17	4(aš) gu ₂	4	⅔ sar	50
18 gin ₂	18	5(aš) gu ₂	5	1 sar	1
19 gin ₂	19	6(aš) gu ₂	6	1 ½ sar	1;20
⅓ ma-na	20	7(aš) gu ₂	7	1 ⅓ sar	1;30
½ ma-na	30	8(aš) gu ₂	8	1 ⅔ sar	1;40
⅔ ma-na	40	9(aš) gu ₂	9	1 ¾ sar	1;50
⅞ ma-na	50	1(u) gu ₂	10		
		1(u) 1(aš) gu ₂	11		
<i>Side d col. ix</i>		<i>Side d col. x</i>		<i>Side d col. xi</i>	
[2 sar	2]	[1(eše ₃) 1(iku) GANA ₂	11 40]	[1(šar ₂) GANA ₂	30]
[3 sar	3]	[1(eše ₃) 2(iku) GANA ₂	13 20]	[1(šar ₂) 1(bur ^u) [GANA ₂	35]
[4 sar	4]	[1(eše ₃) 3(iku) GANA ₂	15]	1(šar ₂) 2(bur ^u) GANA ₂	[40]
[5 sar	5]	[1(eše ₃) 4(iku) GANA ₂	16 40]	1(šar ₂) 3(bur ^u) GANA ₂	ṛ45 ^ṛ
ṛ6 [sar	6]	[1(eše ₃) 5(iku) GANA ₂	18 20]	1(šar ₂) 4(bur ^u) GANA ₂	50
7 ṛsar ^ṛ	[7]	[2(eše ₃) GANA ₂	20]	1(šar ₂) 5(bur ^u)	ṛ55 ^ṛ
8 ṛsar ^ṛ	[8]	[2(eše ₃) 1(iku) GANA ₂	21 40]	2(šar ₂) GANA ₂	1
9 sar	9	[2(eše ₃) 2(iku) GANA ₂	23 20]	[3(šar ₂)] GANA ₂	1 30
10 ṛsar	10 ^ṛ	ṛ2(eše ₃) 3(iku) GANA ₂ ^ṛ	[25]	[4(šar ₂)] GANA ₂	2
11 ṛsar ^ṛ	11	ṛ2(eše ₃) 4(iku) GANA ₂ ^ṛ	[26 40]	[5(šar ₂)] GANA ₂	2 30
12 sar	12	2(eše ₃) 5(iku) ṛGANA ₂ ^ṛ	[28 20]	ṛ6(šar ₂) GANA ₂ ^ṛ	3
13 sar	13	1(bur ₃) ṛGANA ₂ ^ṛ	[30]	ṛ7(šar ₂) ^ṛ [GANA ₂	3 30]
14 sar	14	1(bur ₃) ṛ1(eše ₃) GANA ₂ ^ṛ	[40]	8(šar ₂) GANA ₂	4
15 sar	15	1(bur ₃) ṛ2(eše ₃) GANA ₂ ^ṛ	[50]	9(šar ₂) GANA ₂	4 30
16 sar	16	2(bur ₃) GANA ₂	[1]	[1(šar ^u)] GANA ₂	5
17 sar	17	3(bur ₃) GANA ₂	[1 30]	1(šar ^u) 1(šar ₂) GANA ₂	5 30
18 sar	18	4(bur ₃) GANA ₂	[2]	1(šar ^u) 2(šar ₂) GANA ₂	6
19 sar	19	5(bur ₃) GANA ₂	[2 30]	1(šar ^u) 3(šar ₂) GANA ₂	6 30
20 sar	20	6(bur ₃) GANA ₂	[3]	1(šar ^u) 4(šar ₂) GANA ₂	7
30 sar	30	7(bur ₃) GANA ₂	[3 30]	1(šar ^u) 5(šar ₂) GANA ₂	7 30
40 sar	40	8(bur ₃) GANA ₂	[4]	1(šar ^u) 6(šar ₂) GANA ₂	8
½(iku) GANA ₂	50	9(bur ₃) GANA ₂	4 30	1(šar ^u) 7(šar ₂) GANA ₂	8 30
½(iku) GANA ₂ 10 sar	1	1(bur ^u) GANA ₂	5	1(šar ^u) 8(šar ₂) GANA ₂	9
½(iku) GANA ₂ 20 sar	1 10	1(bur ^u) 1(bur ₃) GANA ₂	5 30	1(šar ^u) 9(šar ₂) GANA ₂	9 30
½(iku) GANA ₂ 30 sar	1 20	1(bur ^u) 2(bur ₃) GANA ₂	[6]	1(šar ₂ ×man) GANA ₂	10
½(iku) GANA ₂ 40 sar	1 30	1(bur ^u) 3(bur ₃) GANA ₂	[6 30]	[1(šar ₂ ×eš)] GANA ₂	15
1(iku) GANA ₂	1 40	1(bur ^u) 4(bur ₃) GANA ₂	[7]	[1(šar ₂ ×ilimmu)] GANA ₂	20
1 ½(iku) GANA ₂	2 30	1(bur ^u) 5(bur ₃) GANA ₂	[7 30]	1(šar ₂ ×ninnu) GANA ₂	25
2(iku) GANA ₂	3 20	1(bur ^u) 6(bur ₃) ṛGANA ₂ ^ṛ	[8]	1(šar ₂) gal GANA ₂	30
2 ½(iku) GANA ₂	4 10	ṛ1(bur ^u) 7(bur ₃) GANA ₂ ^ṛ	[8 30]	10	
3(iku) GANA ₂	5	ṛ1(bur ^u) 8(bur ₃) ^ṛ [GANA ₂	9	ⁱⁱⁱ ab-e ₃ -[a] ud 26-[kam]	
3 ½(iku) GANA ₂	5 50	[1(bur ^u) 9(bur ₃)] GANA ₂	9 30		
4(iku) GANA ₂	6 40	[2(bur ^u)] GANA ₂	10	1 šu-si 10?	
4 ½(iku) GANA ₂	7 30	ṛ3(bur ^u) ^ṛ GANA ₂	15		
5(iku) GANA ₂	8 20	4(bur ^u) GANA ₂	[20]		
5 ½(iku) GANA ₂	9 10	5(bur ^u) [GANA ₂	25]		
1(eše ₃) GANA ₂	10				

Appendix 2: VA 2596

VA 2596 (not VAT 2596, as it is sometimes cited) is a slightly convex clay cylinder, almost perfectly preserved, just under 12 cm high and 8 cm in diameter at its widest extent (Fig. 9). A cylindrical hole of ca 2 cm diameter runs down its centre parallel to the cylindrical surface. There are no signs of rotational wear inside it, but there are a few fine vertical striations around the edges of the hole, in particular at the bottom of the cylinder, where the hole is slightly distorted to one side. About half-way down this central hole there is a trapezoidal depression, slightly smaller than a fingertip but with straight edges. The flat surfaces of the top and bottom are each divided into quadrants by four lines radiating from the central hole; top and bottom lines align with each other but not with any of the column rulings on the cylindrical writing surface. This surface is divided exactly into eight columns

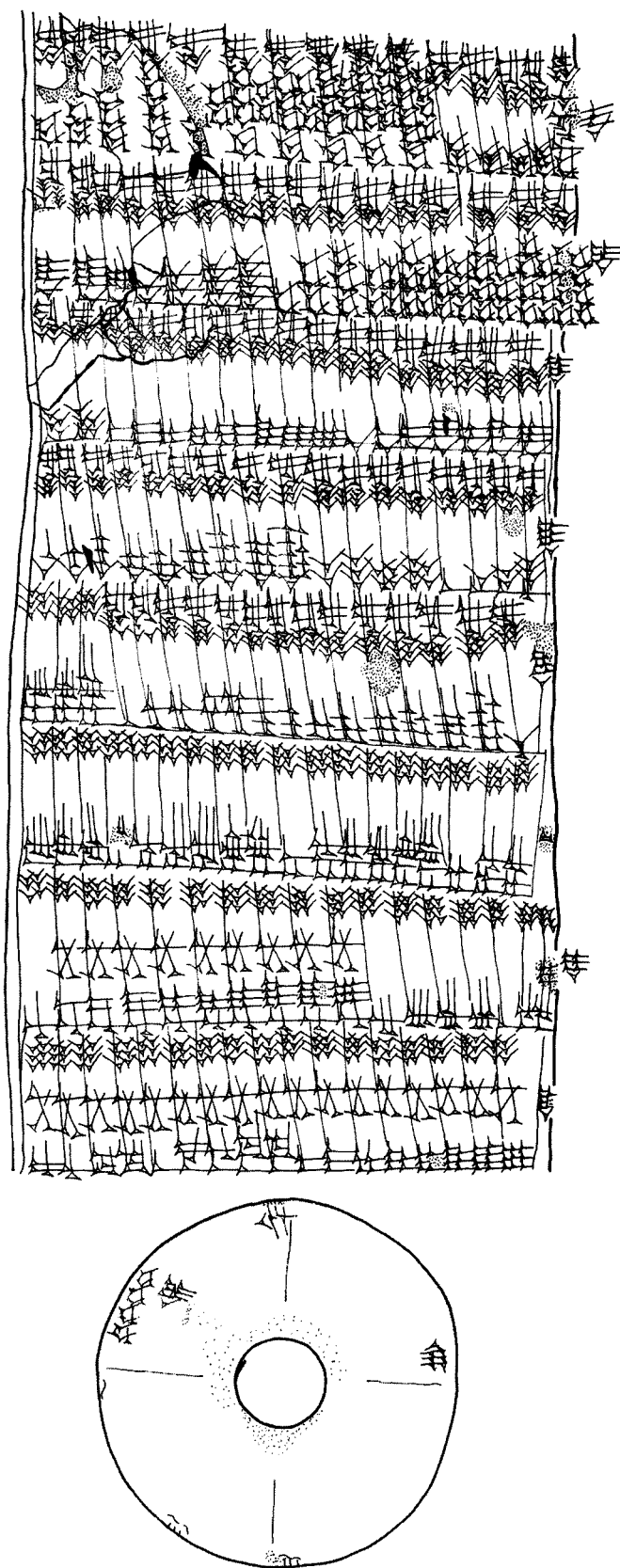


Fig. 9 Cylinder VA 2596. Copy by Eleanor Robson.

of almost equal width, each containing fifteen to eighteen lines of text plus a line-count at the end of each. The metrological list of capacities it contains fits almost perfectly on to it, except in col. vii where the final line spills on to the bottom surface. It is a quiet masterpiece of the scribal art.

The text was first copied by Meissner (1893: Taf. 58), long before cuneiform metrology was fully understood, and has been cited regularly in the literature ever since (e.g. Friberg 1987–90: 542). However, we felt that a new copy was needed in order to represent the material form and textual contents of the cylinder more accurately than Meissner could, given the fledgling state of mathematical Assyriology in the late nineteenth century.

The tablet was copied and photographed by Eleanor Robson with the assistance of Grégory Chambon in July 2010. We are very grateful to Joachim Marzahn and his team at the Vorderasiatisches Museum, Berlin, for their kind assistance and permission to republish it.

<i>Col. i</i>		<i>Col. ii</i>		<i>Col. iii</i>		<i>Col. iv</i>	
1/3 sila ₃	še	1(ban ₂)	še	1(barig) 3(ban ₂)	še	4(barig) 3(ban ₂)	še
1/2 sila ₃	še	1(ban ₂) 1 sila ₃	še	1(barig) 4(ban ₂)	še	4(barig) 4(ban ₂)	še
2/3 sila ₃	še	1(ban ₂) 2 sila ₃	še	1(barig) 5(ban ₂)	še	4(barig) 5(ban ₂)	še
3/4 sila ₃	še	1(ban ₂) 3 sila ₃	še	2(barig)	še	1(aš)	še-gur
1 sila ₃	še	1(ban ₂) 4 sila ₃	še	2(barig) 1(ban ₂)	še	1(aš) 1(barig)	še-gur
1 1/3 sila ₃	še	1(ban ₂) 5 sila ₃	še	2(barig) 2(ban ₂)	še	1(aš) 2(barig)	še-gur
1 1/2 sila ₃	še	1(ban ₂) 6 sila ₃	še	2(barig) 3(ban ₂)	še	1(aš) 3(barig)	še-gur
1 2/3 sila ₃	še	1(ban ₂) 7 sila ₃	še	2(barig) 4(ban ₂)	še	1(aš) 4(barig)	še-gur
1 3/4 sila ₃	še	1(ban ₂) 8 sila ₃	še	2(barig) 5(ban ₂)	še	2(aš)	še-gur
2 sila ₃	še	1(ban ₂) 9 sila ₃	še	3(barig)	še	3(aš)	še-gur
3 sila ₃	še	2(ban ₂)	še	3(barig) 1(ban ₂)	še	4(aš)	še-gur
4 sila ₃	še	3(ban ₂)	še	3(barig) 2(ban ₂)	še	5(aš)	še-gur
5 sila ₃	še	4(ban ₂)	še	3(barig) 3(ban ₂)	še	6(aš)	še-gur
6 sila ₃	še	5(ban ₂)	še	3(barig) 4(ban ₂)	še	7(aš)	še-gur
7 sila ₃	še	1(barig)	še	3(barig) 5(ban ₂)	še	8(aš)	še-gur
8 sila ₃	še	1(barig) 1(ban ₂)	še	4(barig)	še	9(aš)	še-gur
9 sila ₃	še	1(barig) 2(ban ₂)	še	4(barig) 1(ban ₂)	še	1(u)	še-gur
				4(barig) 2(ban ₂)	še		
	17		16 sic		18		17

<i>Col. v</i>		<i>Col. vi</i>		<i>Col. vii</i>		<i>Col. viii</i>	
1(u) 1(aš)	še-gur	1(geš ₂) 4(u)	še-gur	1(geš ^u) 7(geš ₂)	še-gur	1(šar ^u)	še-gur
1(u) 2(aš)	še-gur	1(geš ₂) 5(u)	še-gur	1(geš ^u) 8(geš ₂)	še-gur	1(šar ^u) 1(šar ₂)	še-gur
1(u) 3(aš)	še-gur	2(geš ₂)	še-gur	1(geš ^u) 9(geš ₂)	še-gur	1(šar ^u) 2(šar ₂)	še-gur
1(u) 4(aš)	še-gur	3(geš ₂)	še-gur	2(geš ^u)	še-gur	1(šar ^u) 3(šar ₂)	še-gur
1(u) 5(aš)	še-gur	4(geš ₂)	še-gur	3(geš ^u)	še-gur	1(šar ^u) 4(šar ₂)	še-gur
1(u) 6(aš)	še-gur	5(geš ₂)	še-gur	4(geš ^u)	še-gur	1(šar ^u) 5(šar ₂)	še-gur
1(u) 7(aš)	še-gur	6(geš ₂)	še-gur	5(geš ^u)	še-gur	1(šar ^u) 6(šar ₂)	še-gur
1(u) 8(aš)	še-gur	7(geš ₂)	še-gur	1(šar ₂)	še-gur	1(šar ^u) 7(šar ₂)	še-gur
1(u) 9(aš)	še-gur	8(geš ₂)	še-gur	2(šar ₂)	še-gur	1(šar ^u) 8(šar ₂)	še-gur
2(u)	še-gur	9(geš ₂)	še-gur	3(šar ₂)	še-gur	1(šar ^u) 9(šar ₂)	še-gur
3(u)	še-gur	1(geš ^u)	še-gur	4(šar ₂)	še-gur	1(šar ₂ ×man)	še-gur
4(u)	še-gur	1(geš ^u) 1(geš ₂)	še-gur	5(šar ₂)	še-gur	1(šar ₂ ×eš)	še-gur
5(u)	še-gur	1(geš ^u) 2(geš ₂)	še-gur	6(šar ₂)	še-gur	1(šar ₂ ×ilimmu)	še-gur
1(geš ₂)	še-gur	1(geš ^u) 3(geš ₂)	še-gur	7(šar ₂)	še-gur	1(šar ₂ ×ninnu)	še-gur
1(geš ₂) 1(u)	še-gur	1(geš ^u) 4(geš ₂)	še-gur	7(šar ₂) sic	še-gur	1(šar ₂ ×geš ₂) 1(šar ₂ ×šar ₂)	še-gur
1(geš ₂) 2(u)	še-gur	1(geš ^u) 5(geš ₂)	še-gur	8(šar ₂)	še-gur		
1(geš ₂) 3(u)	še-gur	1(geš ^u) 6(geš ₂)	še-gur				
	17		17		16		15

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