

Crystal structure of $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ and $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ double vanadates

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Polycrystalline samples of $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ (I) and $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ (II) were synthesized using the nitrate–citrate method (I) and conventional solid state reaction (II). The structural refinement based on X-ray powder diffraction data showed that the crystal structure of (I) is characterized by monoclinic symmetry with unit-cell parameters $a = 6.8044(1)$ Å, $b = 14.4876(3)$ Å, $c = 11.2367(2)$ Å, $\beta = 99.647(1)^\circ$ [space group $P2_1/c$ (No. 14), $Z = 4$], and the crystal structure of (II) is triclinic with unit-cell parameters $a = 7.03813(6)$ Å, $b = 12.9085(1)$ Å, $c = 6.99961(5)$ Å, $\alpha = 90.7265(5)^\circ$, $\beta = 96.3789(5)^\circ$, $\gamma = 94.9530(6)^\circ$, $V = 629.470(8)$ Å³ [space group $P\bar{1}$ (No. 2), $Z = 2$]. © 2018 International Centre for Diffraction Data. [doi:10.1017/S0885715618000441]

Key words: double vanadates, X-ray powder diffraction, crystal structure

I. INTRODUCTION

The pyrovanadates $M_2\text{V}_2\text{O}_7$, where $M = \text{Ca}$, Sr , Pb , Ba , Mg , Zn , Co , Ni , Cu , Mn , Cd , demonstrate promising magnetic (Bhatia *et al.*, 2010; Basiev *et al.*, 2011; Sanchez-Andujar *et al.*, 2011), optical (Cid-García *et al.*, 2012; Dalal *et al.*, 2015; Takahashi *et al.*, 2016), and electrical (Cowin *et al.*, 2011) properties. The physico-chemical properties and structures of divalent metal vanadates have been studied in depth. Double vanadates of nominal compositions $MM'\text{V}_2\text{O}_7$ and $M_{1.5}M'_{0.5}\text{V}_2\text{O}_7$, where $M, M' = \text{Ca}$, Sr , Pb , Ba , Mg , Zn , Co , Ni , Cu , Mn , Cd , were synthesized mainly in the period between 1985 and 1999. At the same time, not only the unit-cell parameters were determined for a number of compounds, but also the crystal structures were described (Table I). A systematic study of the crystal structure of divalent metal vanadates has cast doubt on the correctness of isolation of the pyroanion $\text{V}_2\text{O}_7^{4-}$ in their chemical formula, since the data obtained showed a more complex anion structure (Zhuravlev *et al.*, 1982; Murashova *et al.*, 1989; Murashova *et al.*, 1991; Vogt and Muller-Buschbaum, 1991a). In addition to vanadates with anionic groups $\text{V}_2\text{O}_7^{4-}$, compounds containing anionic groups $\text{V}_4\text{O}_{14}^{8-}$ and $[(\text{V}_3\text{O}_{10})(\text{VO}_4)]^{8-}$ were also described. In Table I, a part of the formula of double vanadates is presented taking into account the data on the V–O distances in the vanadium–oxygen groups; the other part is presented in the form given in the original sources.

In this paper, the results of goal-oriented synthesis of double vanadates of calcium and zinc, lead, and cadmium (Table I) and their crystal structures are reported, and changes in the configuration and vanadium–oxygen polyhedra of related compounds are considered.

II. EXPERIMENTAL

Samples of $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ were synthesized using the citrate method. $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ was obtained via solid-phase synthesis. Calcium–zinc and calcium–manganese vanadates were prepared by dissolving an equimolar amount of manganese (zinc) oxides and calcium carbonate of reactive purity in nitric acid. An equivalent amount of V_2O_5 was separately dissolved in citric acid in the ratio 1:4 during heating. After complete dissolution of the V_2O_5 sample, the vanadium solution acquired a blue colour, indicating the formation of vanadyl citrate,



The formation of nitrate–citrate complexes followed the coacervation of vanadyl citrate solutions and nitrates of calcium, manganese, and zinc, preventing salting out and leading, under heating, to the formation of xerogels of variable composition. Evaporation was carried out at about 100 °C until a viscous mass was formed. After the formation of the xerogel, the temperature was raised to 250–300 °C, initiating a redox process in the reaction mass. The reaction proceeded without release of nitrogen oxides because of the excess of citric acid reducing agent. The resulting powder was brownish-yellow because of the presence of unburned carbon particles. The precursor was ground in an agate mortar and annealed at 500 and 650 °C, whereupon the product acquired a white colour. According to XRPD, it became single phase after annealing at ~650 °C.

$\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ was synthesized using cadmium carbonate, lead oxide, and vanadium (V) oxide. The initial components were mixed and subjected to multistage annealing in the temperature range from 450 to 600 °C. The annealing time at the final stage of synthesis was 30 h.

The X-ray powder diffraction (XRPD) patterns were collected at room temperature on a STADI P (Stoe)

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TABLE I. Crystallographic characteristics of double vanadates of divalent metals.

Compound	<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	β (°)	<i>Z</i>	Sp.gr.	References
I							
Sr ₂ Mg ₂ (V ₄ O ₁₄)	6.829 (2)	14.857 (4)	11.309 (4)	98.78 (2)	4	<i>P</i> 2 ₁ / <i>c</i>	Velikodnyi <i>et al.</i> (1985)
SrCoV ₂ O ₇	6.8360 (20)	14.822 (2)	11.2710 (10)	99.430 (20)	8	<i>P</i> 2 ₁ / <i>c</i>	PDF 00-044-455
SrMnV ₂ O ₇	6.876 (1)	15.031 (3)	11.591 (2)	96.96 (2)	8	<i>P</i> 2 ₁ / <i>c</i>	Zhuravlev <i>et al.</i> (1993)
Pb ₂ Zn ₂ (V ₄ O ₁₄)	6.911 (2)	14.853 (2)	11.338 (2)	99.51 (1)	4	<i>P</i> 2 ₁ / <i>c</i>	Murashova <i>et al.</i> (1991)
Pb ₂ Mg ₂ (V ₃ O ₁₀)(VO ₄)	6.854 (1)	15.007 (5)	11.490 (2)	97.84 (2)	4	<i>P</i> 2 ₁ / <i>c</i>	Murashova <i>et al.</i> (1991)
PbCoV ₂ O ₇	6.8657 (7)	14.8610 (20)	11.3300 (20)	99.590 (10)	8	<i>P</i> 2 ₁ / <i>c</i>	PDF 00-051-0134
Pb ₂ Mn ₂ (V ₃ O ₁₀)(VO ₄)	6.9255 (6)	15.0841 (10)	11.6710 (10)	97.006 (8)	4	<i>P</i> 2 ₁ / <i>c</i>	PDF 00-051-0418
Ca ₂ Mg ₂ (V ₄ O ₁₄)	6.756 (2)	14.495 (3)	11.253 (2)	99.12 (2)	8	<i>P</i> 2 ₁ / <i>c</i>	Murashova <i>et al.</i> (1993)
Ca ₂ Co ₂ (V ₄ O ₁₄)	6.769 (1)	14.472 (2)	11.225 (2)	99.52 (1)	4	<i>P</i> 2 ₁ / <i>c</i>	Murashova <i>et al.</i> (1993)
Ca ₂ Zn ₂ (V ₄ O ₁₄)	6.8044 (1)	14.4876 (3)	11.2367 (2)	99.647 (1)	4	<i>P</i> 2 ₁ / <i>c</i>	*
II							
SrCuV ₂ O ₇	14.496 (2)	5.469 (1)	7.425 (1)		4	<i>Pnma</i>	Vogt, and Muller-Buschbaum (1991b)
BaCuV ₂ O ₇	15.0511 (69)	5.5136 (24)	7.5134 (17)		4	<i>Pnma</i>	Vogt, and Muller-Buschbaum (1991a)
BaCaV ₂ O ₇	15.508 (3)	5.814 (1)	7.343 (2)		4	<i>Pnma</i>	Murashova <i>et al.</i> (1989)
α -BaZnV ₂ O ₇	15.048 (3)	5.5700 (10)	7.55580 (20)		4	<i>Pnma</i>	Murashova <i>et al.</i> (1989)
BaCdV ₂ O ₇	15.400 (2)	5.712 (1)	7.412 (1)		4	<i>Pnma</i>	Murashova <i>et al.</i> (1989)
BaMgV ₂ O ₇	15.062 (2)	5.5799 (1)	7.578 (1)		4	<i>Pnma</i>	PDF 00-046-0758
III							
β -BaZnV ₂ O ₇	5.573 (1)	15.175 (1)	7.429 (1)	96.45 (1)	4	<i>P</i> 2 ₁ / <i>n</i>	Murashova <i>et al.</i> (1989)
BaMnV ₂ O ₇	5.623 (1)	15.287 (3)	7.401 (2)	95.55 (2)	4	<i>P</i> 2 ₁ / <i>n</i>	Zhuravlev <i>et al.</i> (1993)
SrZnV ₂ O ₇	7.425 (2)	6.697 (2)	11.977 (5)	95.98 (5)	4	<i>P</i> 2 ₁ / <i>n</i>	Velikodnyi <i>et al.</i> (1989)
IV							
Sr ₃ Mn(V ₂ O ₇) ₂	6.997 (1)		25.443 (8)		4	<i>P</i> 4 ₁ 2 ₁ 2	Zhuravlev <i>et al.</i> (1993)
Sr ₃ Ca(V ₂ O ₇) ₂	7.012		25.4500		4	<i>P</i> 4 ₁	Zhuravlev <i>et al.</i> (1990)
Sr ₃ Cd(V ₂ O ₇) ₂	7.057 (1)		25.566 (2)		4	<i>P</i> 4 ₁ 2 ₁ 2	Velikodnyi <i>et al.</i> (1993a)
V							
Pb ₂ Cd ₂ (V ₃ O ₁₀)(VO ₄) ^a	6.99961 (5)	7.03813 (6)	12.9085 (1)	94.9530 (5) 90.7265 (5) 96.3789 (5)	2	<i>P</i> $\bar{1}$	^b
Ba ₃ PbV ₄ O ₁₄ ^a	7.2932 (15)	7.2997 (15)	13.379 (3)	99.68 (3) 93.68 (3) 91.49 (3)	2	<i>P</i> $\bar{1}$	Sivakumar <i>et al.</i> (2007)
VI							
CaCuV ₂ O ₇	10.010 (37)	8.8454 (51)	10.1899 (19)	91.032 (17)	8	<i>P</i> 2/ <i>c</i>	Vogt and Muller-Buschbaum (1991b)

^aThe reduced cells are shown.^bData obtained in this study.TABLE II. Crystal data and structure refinement for Ca₂Zn₂(V₄O₁₄) and Pb₂Cd₂(V₃O₁₀)(VO₄).

Structure formula	Ca ₂ Zn ₂ (V ₃ O ₁₀)(VO ₄)	Pb ₂ Cd ₂ (V ₃ O ₁₀)(VO ₄)
Formula weight, Mr, g/mol	638.69	1066.974
Temperature, K	298 (2)	298 (2)
Crystal system, space group	Monoclinic, <i>P</i> 2 ₁ / <i>c</i> (No. 14)	Triclinic, <i>P</i> $\bar{1}$ (No. 2)
Unit-cell parameters		
<i>a</i> , Å	6.8093 (2)	7.03813 (6)
<i>b</i> , Å	14.5094 (3)	12.9085 (1)
<i>c</i> , Å	11.2568 (3)	6.99961 (5)
α , °	90	90.7265 (5)
β , °	99.471 (12)	96.3789 (5)
γ , °	90	94.9530 (5)
<i>V</i> , Å ³	1092.8 (3)	629.470 (8)
Formula unit, <i>Z</i>	4	2
Calculated density, g/cm ³	3.881	5.629
Measured density, g/cm ³	3.865 (5)	
w <i>R</i> _p , %	2.04	2.17
<i>R</i> _p , %	1.56	1.58
χ^2	4.02	1.975
<i>R</i> (<i>F</i> ²), %	2.50	2.57

TABLE III. Atomic coordinates and isotropic displacement parameters ($U_{\text{iso}} \times 100, \text{\AA}^2$) for $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ and $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$.

Atom	X	Y	z	$U_{\text{iso}} \times 100$
<i>Ca₂Zn₂(V₄O₁₄)</i>				
Zn(1)	-0.0089 (9)	0.25215 (29)	0.24720 (43)	4.01 (10)
Zn(2)	0.3428 (6)	0.17318 (28)	0.42497 (35)	4.01 (10)
Ca(1)	0.6571 (9)	0.1315 (5)	0.0201 (5)	4.9 (2)
Ca(2)	0.9461 (8)	0.0053 (5)	0.7552 (5)	4.9 (2)
V(1)	0.4870 (9)	0.2099 (4)	0.7063 (5)	3.27 (7)
V(2)	0.4297 (8)	0.0171 (4)	0.6888 (5)	3.27 (7)
V(3)	0.1397 (9)	-0.1347 (4)	0.5203 (6)	3.27 (7)
V(4)	0.1558 (9)	0.3765 (5)	0.5137 (5)	3.27 (7)
O(1)	0.5681 (20)	0.1095 (12)	0.7928 (12)	2.27 (13)
O(2)	0.2934 (28)	0.2615 (10)	0.7657 (15)	2.27 (13)
O(3)	0.3293 (26)	0.2937 (11)	0.5297 (16)	2.27 (13)
O(4)	0.6764 (28)	0.2754 (11)	0.7040 (14)	2.27 (13)
O(5)	0.3925 (21)	0.1137 (12)	0.5951 (13)	2.27 (13)
O(6)	0.6135 (22)	-0.0458 (11)	0.6799 (14)	2.27 (13)
O(7)	0.2467 (22)	-0.0209 (12)	0.5481 (13)	2.27 (13)
O(8)	0.2945 (25)	-0.0097 (12)	0.7964 (14)	2.27 (13)
O(9)	-0.0348 (24)	-0.1596 (11)	0.6241 (15)	2.27 (13)
O(10)	0.0433 (22)	-0.1270 (12)	0.3721 (16)	2.27 (13)
O(11)	0.3384 (25)	-0.2128 (10)	0.5510 (15)	2.27 (13)
O(12)	0.0000 (26)	0.3713 (13)	0.3686 (14)	2.27 (13)
O(13)	-0.0041 (25)	0.3572 (12)	0.6169 (15)	2.27 (13)
O(14)	0.2589 (24)	0.4809 (13)	0.5298 (14)	2.27 (13)
<i>Pb₂Cd₂(V₃O₁₀)(VO₄)</i>				
Pb(1)	0.38527 (19)	0.15779 (10)	0.39246 (19)	2.78 (13)
Pb(2)	0.68426 (20)	0.40938 (11)	0.14207 (19)	3.42 (13)
Cd(1)	0.13147 (31)	0.38557 (17)	0.49405 (30)	1.15 (14)
Cd(2)	0.29542 (31)	0.85660 (16)	0.12174 (31)	2.09 (14)
V(1)	0.8514 (8)	0.1271 (5)	0.3866 (8)	3.33 (23)
V(2)	0.8023 (8)	0.9146 (4)	0.1311 (8)	2.70 (23)
V(3)	0.1452 (7)	0.3175 (4)	0.9992 (8)	3.54 (21)
V(4)	0.6417 (7)	0.3891 (4)	0.6537 (8)	2.30 (22)
O(1)	0.9293 (21)	0.0097 (15)	0.2764 (22)	2.85 (17) ^a
O(2)	0.9516 (22)	0.8143 (13)	0.0749 (21)	2.85 (17) ^a
O(3)	0.2810 (20)	0.9044 (11)	0.4338 (24)	2.85 (17) ^a
O(4)	0.7112 (21)	0.1813 (11)	0.2063 (22)	2.85 (17) ^a
O(5)	0.0568 (22)	0.2043 (11)	0.4654 (20)	2.85 (17) ^a
O(6)	0.6232 (22)	0.8650 (12)	0.2328 (23)	2.85 (17) ^a
O(7)	0.7200 (21)	0.9781 (12)	0.9449 (24)	2.85 (17) ^a
O(8)	0.1697 (21)	0.4023 (12)	0.8182 (22)	2.85 (17) ^a
O(9)	0.3510 (21)	0.2843 (11)	0.1006 (21)	2.85 (17) ^a
O(10)	0.0387 (22)	0.3667 (12)	0.1799 (24)	2.85 (17) ^a
O(11)	0.7462 (23)	0.3052 (12)	0.8085 (21)	2.85 (17) ^a
O(12)	0.4360 (25)	0.3357 (12)	0.5068 (23)	2.85 (17) ^a
O(13)	0.8135 (20)	0.4379 (12)	0.4978 (22)	2.85 (17) ^a
O(14)	0.5817 (21)	0.4849 (11)	0.7821 (21)	2.85 (17) ^a

^aAtomic displacement parameters of all oxygen atoms were constrained as single variable.

diffractometer with transmission geometry, using $\text{CuK}\alpha_1$ radiation and a linear mini-PSD detector in a 2θ range of $5\text{--}120^\circ$ with a step of 0.02° . To obtain high-quality diffraction data, following the recommendations given by Stoe, very thin layers of powdered high absorbing materials were fixed on acetate foils by Elmers White Glue. The thickness of the layer was adjusted to get the transmission factor, I_0/I , equal to approximately 2–3, where I_0 is the flux of the primary beam, and I is the flux passing through the specimen. Polycrystalline silicon [$a = 5.43075(5) \text{\AA}$] was used as an external standard. Possible impurity phases were checked by comparing their XRPD patterns with those in the PDF2 database (ICDD, 2016). The only impurity found was 1.5 mass% of $\text{Cd}_2\text{V}_2\text{O}_7$ in $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$. The XRPD pattern of $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ was indexed using the TREOR program (Werner *et al.*, 1985) and compared with an analogous monoclinic unit cell of CaCoV_2O_7 (Murashova

et al., 1993). The crystal structure refinement of the new compounds was carried out employing Rietveld analysis (Rietveld, 1969) with the GSAS program suite using the XRPD data (Toby, 2001; Larson and Von Dreele, 2004). The peak profiles were fitted with a pseudo-Voigt function, $I(2\theta) = x \times L(2\theta) + (1-x) \times G(2\theta)$ (where L and G are the Lorentzian and Gaussian parts, respectively). The angular dependence of the peak width was described by the relation $(\text{FWHM})^2 = U \tan^2\theta + V \tan\theta + W$, where FWHM is the full line width at half maximum. The background level was described by a combination of 15-order Chebyshev polynomials. Since the background of XRPD pattern of $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ was difficult to fit, it was removed before the refinement. The absorption correction function for a flat plate sample in transmission geometry was applied. Since both models being refined have a large number of atomic positions, and correlations

TABLE IV. Selected interatomic distances d (Å) and angles ($^\circ$) for $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ and $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$.

(a) $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$							
Interatomic distances		Interatomic distances		Interatomic distances		Interatomic distances	
Zn(1)–O(2)	2.042 (18)	Zn(2)–O(2)	2.002 (16)	Ca(1)–O(1)	2.545 (13)	Ca(2)–O(6)	2.396 (15)
Zn(1)–O(4)	2.152 (19)	Zn(2)–O(3)	2.116 (16)	Ca(1)–O(3)	2.498 (17)	Ca(2)–O(8)	2.348 (17)
Zn(1)–O(9)	1.958 (15)	Zn(2)–O(5)	2.072 (15)	Ca(1)–O(4)	2.452 (16)	Ca(2)–O(9)	2.820 (17)
Zn(1)–O(10)	2.194 (20)	Zn(2)–O(6)	2.237 (17)	Ca(1)–O(8)	2.692 (16)	Ca(2)–O(10)	2.280 (18)
Zn(1)–O(12)	2.195 (18)	Zn(2)–O(9)	2.085 (16)	Ca(1)–O(11)	2.395 (17)	Ca(2)–O(12)	2.191 (19)
Zn(1)–O(13)	2.161 (16)	Zn(2)–O(11)	2.216 (17)	Ca(1)–O(13)	2.384 (18)	Ca(2)–O(13)	2.575 (18)
Zn–O	2.117	Zn–O	2.121	Ca–O	2.473	Ca–O	2.435
<i>Expected^a</i>	<i>2.100</i>	<i>Expected^a</i>	<i>2.100</i>	<i>Expected^a</i>	<i>2.420</i>	<i>Expected^a</i>	<i>2.420</i>
V(1)–O(1)	1.785 (15)	V(2)–O(1)	1.918 (15)	V(3)–O(7)	1.809 (17)	V(4)–O(3)	1.671 (16)
V(1)–O(2)	1.742 (16)	V(2)–O(5)	1.745 (16)	V(3)–O(9)	1.834 (16)	V(4)–O(12)	1.792 (15)
V(1)–O(3)	2.418 (18)	V(2)–O(6)	1.563 (15)	V(3)–O(10)	1.688 (14)	V(4)–O(13)	1.740 (14)
V(1)–O(4)	1.604 (16)	V(2)–O(7)	1.921 (15)	V(3)–O(11)	1.752 (16)	V(4)–O(14)	1.665 (17)
V(1)–O(5)	1.909 (16)	V(2)–O(8)	1.682 (16)				
V–O	1.892	V–O	1.766	V–O	1.771	V–O	1.717
<i>Expected^a</i>	<i>1.820</i>	<i>Expected^a</i>	<i>1.820</i>	<i>Expected^a</i>	<i>1.715</i>	<i>Expected^a</i>	<i>1.715</i>
Angles		Angles		Angles		Angles	
O(1)V(1)O(2)	109.0 (8)	O(1)V(2)O(5)	79.3 (6)	O(7)V(3)O(9)	110.7 (8)	O(3)V(4)O(12)	111.6 (10)
O(1)V(1)O(3)	155.6 (7)	O(1)V(2)O(6)	97.4 (8)	O(7)V(3)O(10)	100.9 (9)	O(3)V(4)O(13)	108.8 (9)
O(1)V(1)O(4)	108.3 (8)	O(1)V(2)O(7)	152.3 (8)	O(7)V(3)O(11)	106.2 (7)	O(3)V(4)O(14)	111.3 (8)
O(1)V(1)O(5)	78.5 (7)	O(1)V(2)O(8)	89.7 (8)	O(9)V(3)O(10)	117.0 (8)	O(12)V(4)O(13)	105.0 (7)
O(2)V(1)O(3)	80.7 (7)	O(5)V(2)O(6)	117.7 (8)	O(9)V(3)O(11)	108.0 (8)	O(12)V(4)O(14)	108.1 (9)
O(2)V(1)O(4)	114.4 (8)	O(5)V(2)O(7)	74.0 (7)	O(10)V(3)O(11)	113.3 (8)	O(13)V(4)O(14)	111.9 (9)
O(2)V(1)O(5)	111.8 (7)	O(5)V(2)O(8)	125.2 (8)				
O(3)V(1)O(4)	86.4 (7)	O(6)V(2)O(7)	101.3 (7)				
O(3)V(1)O(5)	77.0 (6)	O(6)V(2)O(8)	116.8 (9)				
O(4)V(1)O(5)	127.2 (8)	O(7)V(2)O(8)	99.7 (8)				
(b) $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$							
Interatomic distances		Interatomic distances		Interatomic distances		Interatomic distances	
Pb(1)–O(3)	2.712 (14)	Pb(2)–O(4)	3.003 (15)	Cd(1)–O(5)	2.355 (15)	Cd(2)–O(2)	2.419 (15)
Pb(1)–O(4)	2.758 (13)	Pb(2)–O(8)	2.555 (16)	Cd(1)–O(8)	2.261 (15)	Cd(2)–O(3)	2.278 (16)
Pb(1)–O(5)	2.542 (14)	Pb(2)–O(9)	2.715 (15)	Cd(1)–O(10)	2.227 (17)	Cd(2)–O(4)	2.336 (14)
Pb(1)–O(6)	2.650 (15)	Pb(2)–O(10)	2.587 (15)	Cd(1)–O(12)	2.284 (15)	Cd(2)–O(6)	2.344 (15)
Pb(1)–O(7)	2.912 (15)	Pb(2)–O(11)	2.775 (14)	Cd(1)–O(13)	2.396 (14)	Cd(2)–O(7)	2.200 (15)
Pb(1)–O(9)	2.635 (14)	Pb(2)–O(13)	2.565 (15)	Cd(1)–O(13)	2.277 (15)	Cd(2)–O(11)	2.153 (15)
Pb(1)–O(12)	2.406 (15)	Pb(2)–O(14)	2.757 (14)				
		Pb(2)–O(14)	2.508(15)				
Pb–O	2.659	Pb–O	2.683	Cd–O	2.3	Cd–O	2.288
<i>Expected^a</i>	<i>2.59</i>	<i>Expected^a</i>	<i>2.65</i>	<i>Expected^a</i>	<i>2.31</i>	<i>Expected^a</i>	<i>2.31</i>
V(1)–O(1)	1.844 (16)	V(2)–O(1)	1.707 (16)	V(3)–O(2)	1.824 (15)	V(4)–O(11)	1.697 (15)
V(1)–O(3)	1.680 (14)	V(2)–O(2)	1.803 (15)	V(3)–O(8)	1.698 (14)	V(4)–O(12)	1.763 (18)
V(1)–O(4)	1.709 (15)	V(2)–O(6)	1.606 (14)	V(3)–O(9)	1.634 (13)	V(4)–O(13)	1.796 (15)
V(1)–O(5)	1.717 (15)	V(2)–O(7)	1.627 (16)	V(3)–O(10)	1.685 (15)	V(4)–O(14)	1.632 (14)
V–O	1.738	V–O	1.686	V–O	1.71	V–O	1.722
<i>Expected^a</i>	<i>1.715</i>	<i>Expected^a</i>	<i>1.715</i>	<i>Expected^a</i>	<i>1.715</i>	<i>Expected^a</i>	<i>1.715</i>
Angles		Angles		Angles		Angles	
O(1)V(1)O(3)	110.9 (7)	O(1)V(2)O(2)	111.3 (8)	O(2)V(3)O(8)	115.6 (8)	O(11)V(4)O(12)	115.1 (8)
O(1)V(1)O(4)	105.0 (7)	O(1)V(2)O(6)	110.0 (8)	O(2)V(3)O(9)	95.6 (8)	O(11)V(4)O(13)	108.8 (7)
O(1)V(1)O(5)	106.3 (8)	O(1)V(2)O(7)	103.2 (8)	O(2)V(3)O(10)	113.3 (8)	O(11)V(4)O(14)	107.3 (8)
O(3)V(1)O(4)	109.1 (8)	O(2)V(2)O(6)	109.9 (7)	O(8)V(3)O(9)	112.8 (8)	O(12)V(4)O(13)	107.5 (7)
O(3)V(1)O(5)	112.1 (8)	O(2)V(2)O(7)	113.8 (8)	O(8)V(3)O(10)	112.9 (8)	O(12)V(4)O(14)	108.6 (7)
O(4)V(1)O(5)	113.1 (7)	O(6)V(2)O(7)	108.3 (8)	O(9)V(3)O(10)	104.9 (8)	O(13)V(4)O(14)	109.5 (8)
V(1)O(1)V(2)	130.6 (9)	V(2)O(2)V(3)	122.9 (9)				

The average values are indicated by boldface type.

^aThe sum of the crystal radii according to [Shannon R.D. Acta Crystallogr. A 32 (1976) 751]: Pb^{+2} VII – 1.37 Å, Pb^{+2} VIII – 1.43 Å, Cd^{+2} VI – 1.09 Å, V^{+5} IV – 0.495 Å, O^{-2} III – 1.22 Å.

between a large number of variables are probable, the atomic displacement parameters of all oxygen atoms were constrained as single variable. The crystallographic data, atomic coordinates, atomic displacement parameters, and selected interatomic distances are given in Tables II–IV. Experimental, calculated, and difference XRPD patterns are shown in Figure 1.

Density measurements were carried out on an AccuPyc II 1340 Gas Displacement Pycnometry System (Micromeritics Instrument Corporation, Norcross, Georgia, USA) with a sample chamber of 1 cm³. About 50–60% of the chamber volume was filled by the powder sample; 15 measurements were performed on the sample.

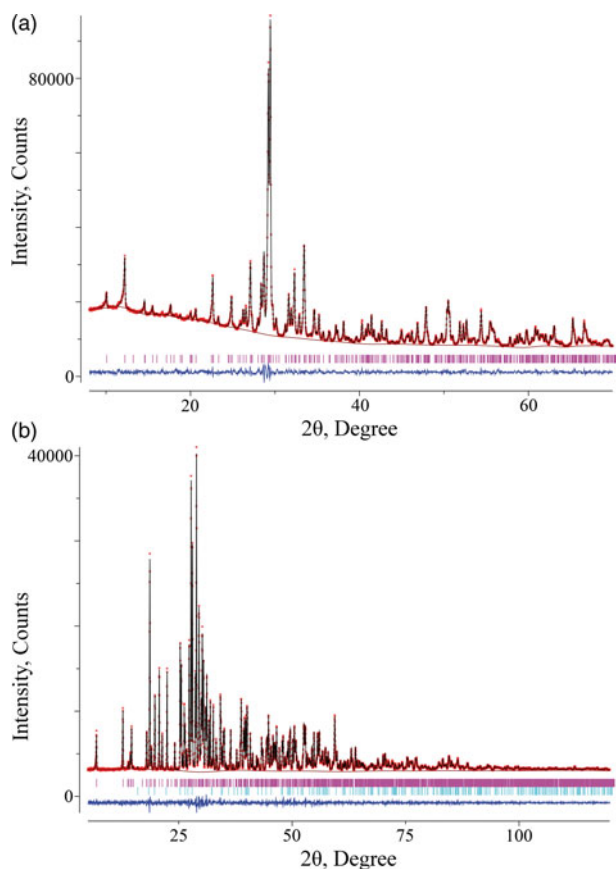


Figure 1. (Color online) Experimental (crosses), calculated (solid line), and difference (bottom line) XRPD patterns of (a) $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ and (b) $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$. The tick marks correspond to the Bragg reflections.

III. DISCUSSION

The XRPD pattern of $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ was indexed in the monoclinic system with unit-cell parameters $a = 6.8044(1) \text{ \AA}$, $b = 14.4876(3) \text{ \AA}$, $c = 11.2367(2) \text{ \AA}$, $\beta = 99.647(1)^\circ$ [space group $P2_1/c$ (14), $Z = 4$]. The most representative double vanadates belong to group I consisting of 10 compounds having an isotype structure that crystallizes in monoclinic system with space group $P2_1/c$. Their nominal anions $\text{V}_2\text{O}_7^{4-}$ either condense into $\text{V}_4\text{O}_{14}^{8-}$ tetramers when the oxygen coordination of the vanadium atoms increases to five [Figures 2(a) and 2(b)], or they form a pair of $\text{V}_3\text{O}_{10}^{5-}$ trimer and orthovanadate ion VO_4^{3-} [Figure 2(c)]. This division into the isotype series is rather arbitrary since the increased V–O distance varies from 2.24 Å in $\text{Pb}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ to 2.75 Å in the trimer–orthovanadate–ion chain in $\text{Pb}_2\text{Mg}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$. This compound is represented as $\text{Ca}_2\text{Zn}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ (Babaryk *et al.*, 2015). Crystal structure of $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ consists of layers containing $\text{V}_4\text{O}_{14}^{8-}$ tetramers alternating along (102) direction with the layers of edge-sharing zinc–oxygen octahedra, Ca(1) and Ca(2) atoms fill empty sites in the latter with coordination numbers 7 and 6, respectively. $\text{V}_4\text{O}_{14}^{8-}$ group consists of two highly distorted edge-sharing vanadium–oxygen polyhedra with CN = 5, which share corners with two terminal vanadium–oxygen tetrahedra [Figures 2(b)], wherein V(1)–O(3) distance, 2.418 Å, is much longer than others. This confirms the separation of the orthovanadate ion VO_4^{3-} from $\text{V}_3\text{O}_{10}^{5-}$ trimer, proposed by Babaryk *et al.* (2015). At the same time, the average metal–oxygen distances are in good

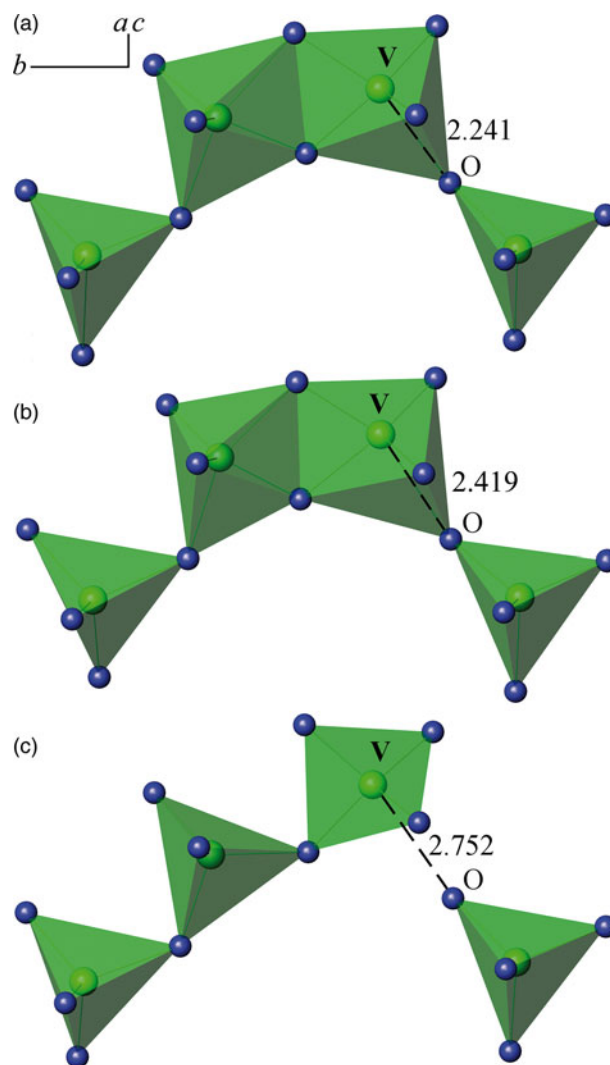


Figure 2. (Color online) The connection of anionic groups in vanadates $\text{Pb}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ (a), $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ (b), $\text{Pb}_2\text{Mg}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ (d).

agreement with the sums of the crystal radii according to Shannon (1976).

The XRPD pattern of the obtained $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ was found to be in good agreement with the data presented by Shpanchenko and Antipov in PDF2 (Entry 00-058-0617) for PbCdV_2O_7 and it was indexed with triclinic unit-cell parameters $a = 7.03813(6) \text{ \AA}$, $b = 12.9085(1) \text{ \AA}$, $c = 6.99961(5) \text{ \AA}$, $\alpha = 90.7265(5)^\circ$, $\beta = 96.3789(5)^\circ$, $\gamma = 94.9530(6)^\circ$, $V = 629.470(8) \text{ \AA}^3$ (space group $P\bar{1}$, No. 2, $Z = 2$), the reduced cell is $a = 6.99961(5) \text{ \AA}$, $b = 7.03813(6) \text{ \AA}$, $c = 12.9085(1) \text{ \AA}$, $\alpha = 94.9530(6)^\circ$, $\beta = 90.7265(5)^\circ$, $\gamma = 96.3789(5)^\circ$. Such unit-cell parameters may be indicative of a similarity of the structure to the B-type rare-earth disilicates $\text{RE}_2\text{Si}_2\text{O}_7$ (Felsche, 1970). The crystal structure of PbCdV_2O_7 has been solved space group $P\bar{1}$ using the EXPO2013 program suite (Altomare *et al.*, 2013) assuming two formula units per unit cell. The resulting model shown in Figure 3, similarly to the structure of $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$, consists of layers containing $\text{V}_4\text{O}_{14}^{8-}$ groups alternating along the (111) direction with the layers of two edge-sharing Cd(1)–oxygen octahedra and separate Cd(2) O_6 octahedra, Pb(1) and Pb(2) atoms fill empty sites in the latter with coordination numbers 7 and 8, respectively, forming a finite chain of four edge-sharing

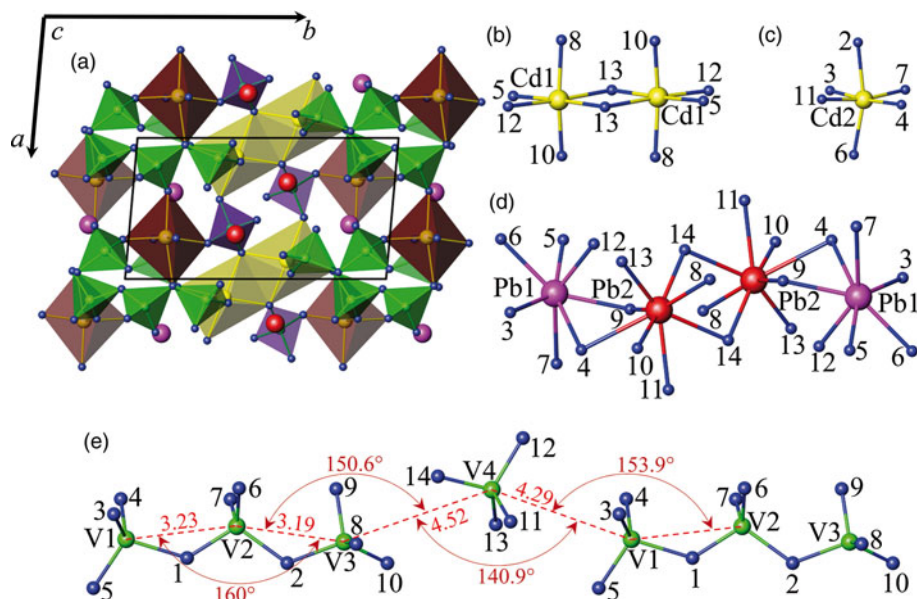


Figure 3. (Color online) Schematic drawing: (a) polyhedral view of the $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ structure, (b) and (c) stick and ball representation of the edge-sharing and isolated $\text{Cd}(1)\text{O}_6$ and $\text{Cd}(2)\text{O}_6$ octahedra, respectively, (d) isolated unit built of four edge-sharing $\text{Pb}(1)\text{O}_7$ and $\text{Pb}(2)\text{O}_8$ polyhedra, (e) broken chain, consisting of alternating single orthovanadate (VO_4) $^{3-}$ and linear trivanadate (V_3O_{10}) $^{5-}$ group. Green and purple tetrahedra indicate tri- and orthovanadates, yellow and brown colour indicate edge-sharing and single cadmium–oxygen octahedra. Blue, purple, red, yellow, and green spheres indicate oxygen, $\text{Pb}(1)$, $\text{Pb}(2)$, cadmium, and vanadium sites, respectively.

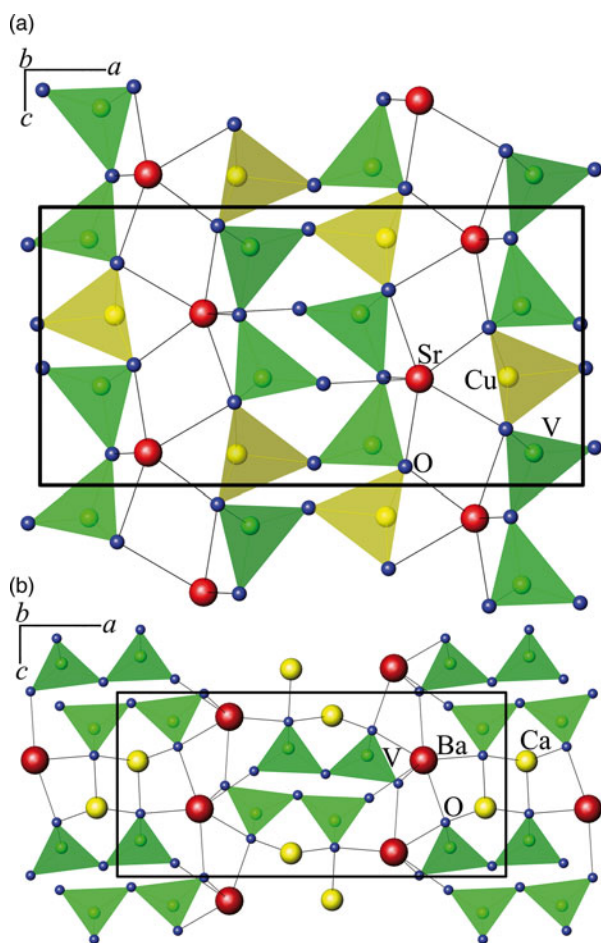


Figure 4. (Color online) The projection along the b -axis of the structure of (a) SrCuV_2O_7 (Velikodnyi and Murashova, 1992) and (b) BaCaV_2O_7 (Murashova *et al.*, 1989).

polyhedra. In $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$, $\text{V}_4\text{O}_{14}^{8-}$ group contains broken chains unusual for the vanadates consisting of single orthovanadate [$\text{V}(4)\text{O}_4$] $^{3-}$ and linear trivanadate (V_3O_{10}) $^{5-}$, formed of three sufficiently regular corner-sharing tetrahedra, alternating along (011) [Figure 3(e)]. The average metal–oxygen distances are in good agreement with the sums of the crystal radii according to Shannon (Shannon, 1976). Such a combination of triple tetrahedra (Si_3O_{10}) $^{8-}$ and single tetrahedra (SiO_4) $^{4-}$ groups has been reported for $\text{Ho}_2\text{Si}_2\text{O}_7$ (Felsche, 1972). Owing to the decrease in the unit-cell symmetry in Table I, the compound constitutes a separate group V. The compound $\text{Ba}_3\text{PbV}_4\text{O}_{14}$ (Sivakumar *et al.*, 2007) is also referred to this group, although this contradicts the study of phase equilibria in the $\text{Ba}_2\text{V}_2\text{O}_7$ – $\text{Pb}_2\text{V}_2\text{O}_7$ system. Primary solid solutions based on barium pyrovanadate were found to contain 0–30 mol% $\text{Pb}_2\text{V}_2\text{O}_7$ (Zhuravlev and Velikodnyi, 1997).

The authors also investigated the possibility of formation of $\text{Pb}_{1.5}\text{Cd}_{0.5}(\text{V}_3\text{O}_{10})(\text{VO}_4)$ and $\text{Pb}_{0.5}\text{Cd}_{1.5}(\text{V}_3\text{O}_{10})(\text{VO}_4)$ compounds. It was found that both compositions contain two phases: $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ and $\text{Pb}_2\text{V}_2\text{O}_7$ or $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ and $\text{Cd}_2\text{V}_2\text{O}_7$.

In group II of Table I, there are six compounds that crystallize in the orthorhombic system with space group $Pnma$. However, according to the $\text{V}_2\text{O}_7^{4-}$ anion packing, four compounds isotopic with SrCuV_2O_7 (Vogt and Muller-Buschbaum, 1991b) can be identified, with $\text{V}_2\text{O}_7^{4-}$ dimers elongated along the a -axis [Figure 4(a)], while in the other two double pyrovanadates, BaCaV_2O_7 and α - BaZnV_2O_7 (high-temperature modification), $\text{V}_2\text{O}_7^{4-}$ dimers are elongated along the c -axis [Figure 4(b)] (Murashova *et al.*, 1989).

Three double vanadates in group III form compounds with monoclinic symmetry and space group $P2_1/n$. Figure 5 displays a typical structure of β - BaZnV_2O_7 (Murashova

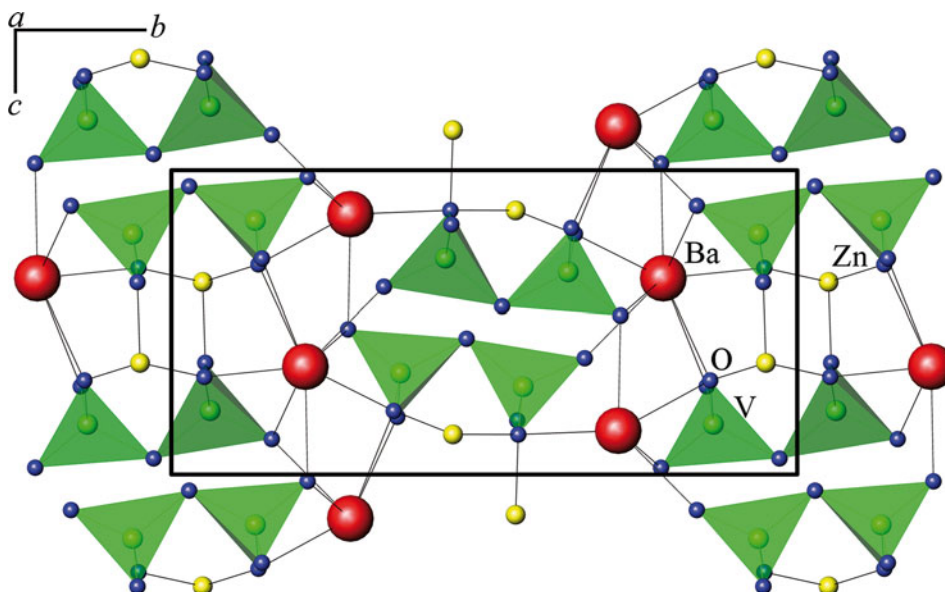


Figure 5. (Color online) Crystal structure of β -BaZnV₂O₇ (Murashova *et al.*, 1989).

et al., 1989). In group III, the vanadate SrZnV₂O₇ (Velikodnyi *et al.*, 1989) is also included, assuming the possibility of a different setting when indicating the parameters, namely: $a' = c/2 = 5.9885 \text{ \AA}$, $b' = 2a = 14.85 \text{ \AA}$, $c' = b = 6.697 \text{ \AA}$.

The double vanadate CaCuV₂O₇ (Figure 6) stands apart, since its V₂O₇⁴⁻ chains are directed along the *ac* vector (Vogt and Muller-Buschbaum, 1991a; b)

The compound CaCdV₂O₇ (Krasnenko *et al.*, 1990) is not shown in Table I because, in the authors' opinion, it

comprises a part of the solid solution based on cadmium pyrovanadates. The limiting composition of the homogeneity region is restricted by the sample Ca_{1.22}Cd_{0.78}V₂O₇ (Murashova *et al.*, 1994).

In the binary systems of vanadates of bivalent metals Sr₂V₂O₇-M'₂V₂O₇ (M' = Mn, Ca, Cd) (Velikodnyi and Murashova, 1992; Zhuravlev *et al.*, 1993; Zhuravlev *et al.*, 1994), compounds with cation ratio Sr:M' = 3:1, crystallizing in tetragonal symmetry with space group P4₁2₁2 in Sr₃Mn

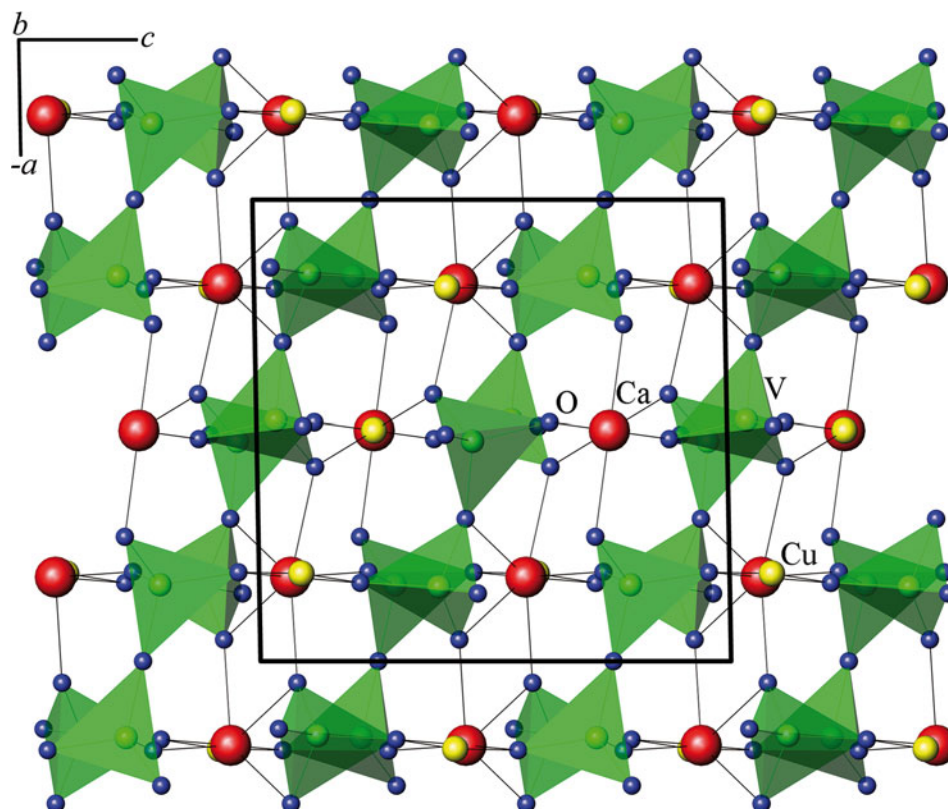


Figure 6. (Color online) Orientation of groups V₂O₇⁴⁻ in CaCuV₂O₇ (Vogt and Muller-Buschbaum, 1991b).

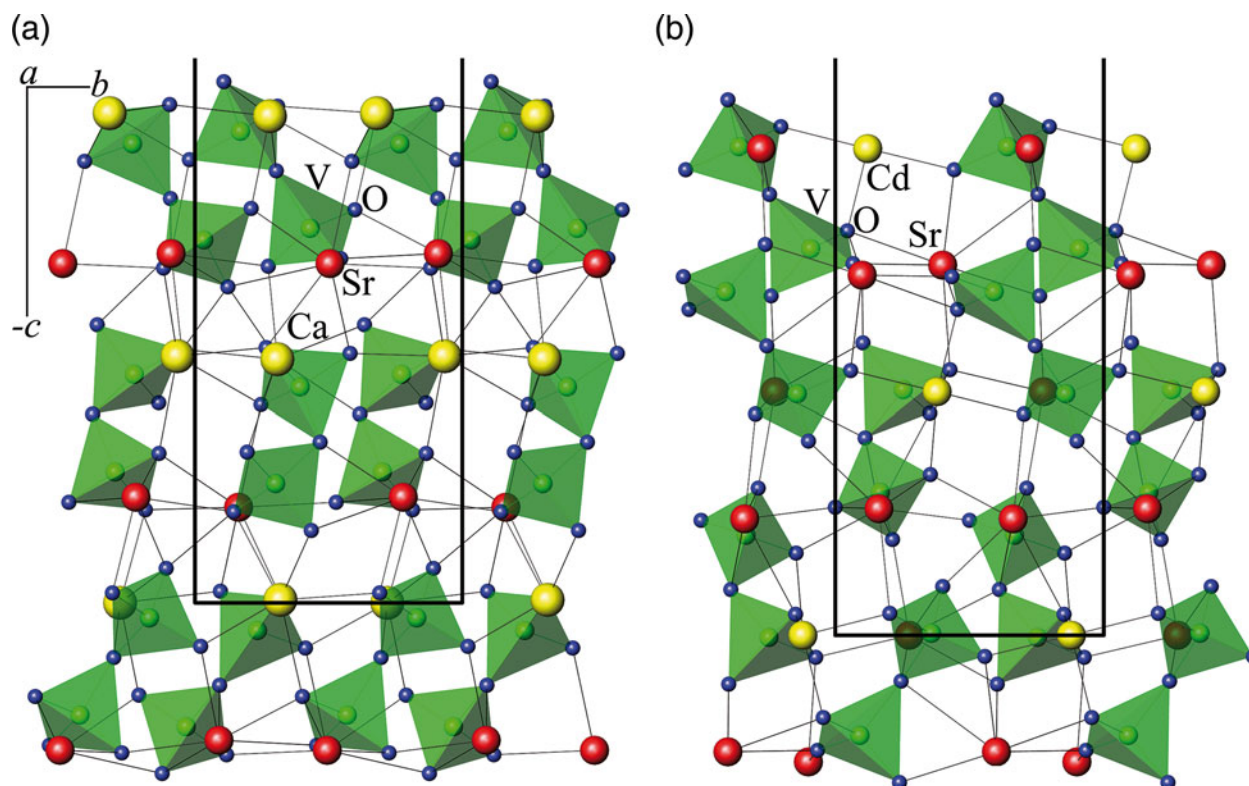


Figure 7. (Color online) The projection of fragments of the structure of (a) $\text{Sr}_3\text{Ca}(\text{V}_2\text{O}_7)_2$ and (b) $\text{Sr}_3\text{Cd}(\text{V}_2\text{O}_7)_2$ along the a -axis.

$(\text{V}_2\text{O}_7)_2$ and $\text{Sr}_3\text{Cd}(\text{V}_2\text{O}_7)_2$, and also $\text{Sr}_3\text{Ca}(\text{V}_2\text{O}_7)_2$ with space group $P4_1$ (Figure 7) are identified.

Proceeding from the arrangement (configuration) of oxygen polyhedrons in vanadium crystal lattices of double vanadates $MM'_2\text{V}_2\text{O}_7$, $M_3M'(\text{V}_2\text{O}_7)_2$, $MM'_2(\text{V}_4\text{O}_{14})$, $M_3M'(\text{V}_3\text{O}_{10})(\text{VO}_4)$, they can be considered as derivatives of pyrovanadate $M_2\text{V}_2\text{O}_7$ of the type of potassium dichromate ($M_2\text{V}_2\text{O}_7$, $M = \text{Ba}, \text{Sr}, \text{Co}, \text{Ni}, \text{Pb}$) or calcium pyrovanadate $\text{Ca}_2\text{V}_2\text{O}_7$. The variety of crystal structures inside these two families is because of the arrangement of two types of bivalent cations and rotation of vanadium–oxygen polyhedrons. For pyrovanadates $M_2\text{V}_2\text{O}_7$ having a thortveitite structure, the formation of broad primary solid solutions in their binary systems is more typical. Both in the pyrovanadates $M_2\text{V}_2\text{O}_7$ and in the double vanadates of divalent metals, structural transformations associated with the evolution of “soft” metal–oxygen polyhedra can take place when the temperature or the composition are changed (Krasnenko *et al.*, 2017; Rotermel and Krasnenko 2017).

IV. CONCLUSIONS

Two new double vanadates $\text{Ca}_2\text{Zn}_2(\text{V}_4\text{O}_{14})$ (I) and $\text{Pb}_2\text{Cd}_2(\text{V}_3\text{O}_{10})(\text{VO}_4)$ (II) have been synthesized, and their crystal structures have been described. The double vanadates of divalent metals known to date can be classified in six different groups according to the proximity of their crystal structures to the structure of vanadium–oxygen anions. The crystal lattices of double vanadates of divalent metals can be regarded as being derived from two types of pyrovanadates $M_2\text{V}_2\text{O}_7$ with the structure of potassium dichromate or calcium pyrovanadate.

SUPPLEMENTARY MATERIAL

The supplementary material for this article can be found at <https://doi.org/10.1017/S0885715618000441>.

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