# Annual flooding, survival and recruitment in a rodent population from the Niger River plain in Mali

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**Abstract:** Multimammate rats of the genus *Mastomys* are among the most widespread pest species in Africa. Previous studies of *Mastomys* population dynamics have generally reported variation in abundance but few have investigated the demographic parameters underlying this variation, and in particular recruitment. Capture-mark-recapture data were collected for *Mastomys erythroleucus* several times a year from 2000 to 2004 at a site annually flooded by the Niger River in Mali. Closed-population models were used to estimate population abundance. Both seniority (a parameter inversely linked to recruitment) and survival probabilities were estimated by capture-mark-recapture models. The impacts of water level, population abundance and cumulative rainfall were assessed for each demographic parameter. Survival probabilities (local survival) were negatively correlated with water level, suggesting that rodents emigrated out of the study zone during flooding. As for seniority probabilities, 86% of temporal variation was explained by a model with season, abundance, water level and the interaction between abundance and water level. This suggests that density-dependence in recruitment was mediated by intraspecific competition for food or refuge from floodwaters, or by predation. The flood of the Niger River greatly impacts *Mastomys erythroleucus* population dynamics, affecting both survival and seniority probabilities.

Key Words: abundance, capture recapture, density-dependence, *Mastomys erythroleucus*, recruitment, seniority, small mammal, survival, trap-happiness, West Africa

### INTRODUCTION

The population dynamics of any living organism are shaped by both intrinsic (e.g. density) and extrinsic (e.g. climate) factors (Berryman 1999). Density-dependence seems to vary greatly among the taxa in which it has been reported. While rare in birds (Croxall & Rothery 1991), it seems especially common in mammals (Erb et al. 2001). Small mammals in particular have proved ideal subjects for investigating density-dependence by various methods (time series: Stenseth 1999; enclosure experiments: Aars & Ims 2002; analysis of demographic parameters estimated from capture-recapture data: Julliard et al. 1999, Lima et al. 2003, Prévôt-Julliard et al. 1999). Many extrinsic factors have also been put forward to account for the population dynamics of small mammals, including predation (Ims & Andreassen 2000), parasitism (Telfer et al. 2002), climate (Lima et al. 2001) and food resources (Boutin 1990). While

most studies have focused on a single factor, some have recently demonstrated that population dynamics is best understood in a framework combining multiple factors, particularly because of interactions between extrinsic and intrinsic factors (Leirs et al. 1997. Lima et al. 2001, Stenseth 1999). Environmental disturbances such as fires, clear-cutting or flooding are known to have tremendous impacts on small-mammal population dynamics (Brown et al. 2001, Halvorson 1982, Yunger 2002). The effects of floods on small-mammal population dynamics have been closely studied in various smallmammal communities (Chamberlain & Leopold 2003, Fournier-Chambrillon et al. 2000, Granjon et al. 2005, Haferkorn 1994, Jacob 2003, but see Batzli 1977). Most studies have reported variation in abundance for various species and have investigated the effects of flooding on the composition of small-mammal communities (e.g. by allowing certain previously rare species to proliferate) or the order in which species recolonize areas after flooding (Anderson & Shapiro 1957, Klinger 2006, Zhang et al. 2007). This paper focuses instead on demographic

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parameters – survival and recruitment – within a single species, the multimammate rat *Mastomys erythroleucus* (Temminck, 1853).

Multimammate rats of the genus *Mastomys* are among the most widespread pest species in West Africa where they may severely damage crops especially during outbreaks (Leirs 2003). Worse still, several Mastomys species are substantial reservoirs of human pathogens (Gratz 1997). Primarily to alleviate the burden Mastomys imposes on human populations, certain Mastomys species have come in for close study (see Leirs in press for a synthesis) as regards their physiology (Granjon et al. 1994), ecology (Hubert & Adam 1981, Hubert et al. 1978, Leirs 1995) and evolutionary biology (Granjon & Duplantier 1993, Leirs et al. 1994). In the realm of population dynamics, studies have been conducted on *M. erythroleucus* (Hubert 1982, Granjon 1987) and *M.* huberti (Granjon et al. 1994, 2005) in West Africa. In East African populations of M. natalensis, a few studies have reported that abundance of individuals impacts survival in wild populations (Julliard et al. 1999, Leirs et al. 1997, Lima et al. 2003, Sluydts et al. 2007).

In this paper, we use 4 y of capture-recapture data collected year round at a site in Mali flooded annually by the Niger River to describe the pattern in survival and recruitment in a wild population of *M. erythroleucus*. We use recent capture-recapture methods to analyse population size (Karanth & Nichols 1998), survival (Lebreton *et al.* 1992) and seniority (Nichols *et al.* 2000). More specifically, these analyses allow us to investigate the impact of the flood of the River Niger on survival and seniority probabilities, by combining one intrinsic (abundance) and two extrinsic (cumulative rainfall, taken as a surrogate of primary production, and water level of the River Niger) factors.

## METHODS

## Study site

Djoliba is located 40 km south-west of Bamako (Mali 8°12 W 12°32 N). The climate is Sahelian to Sudanian with a single rainfall season of about 5 mo (June–October). The dry season is traditionally split into a first period, from November to February, where daily and especially night-time temperatures are relatively cool, and a second period, from March to May, where daily temperatures are hotter. There was much variation among years in the amount of rainfall and the number of rainy days. The year 2000 had 717 mm of rainfall over 80 d; 2001: 722 mm over 60 d; 2002: 720 mm over 55 d; 2003: 1108 mm over 82 d (data from the National Meteorological Service, Bamako). The River Niger floods once a year starting

around May–June and reaching its maximum in late September and its minimum in March–April. The flood is thus a slow, continuous phenomenon rather than a quick and catastrophic event (Batzli 1977). However, as the slope of the plain of the River Niger is generally gentle, vast areas are simultaneously exposed to flooding by changes in river level (Granjon *et al.* 2005). During the study, there were four flooding events of variable intensity; the maximum water levels were 540 cm in 2000, 684 cm in 2001, 494 cm in 2002 and 606 cm in 2003 (data from the National Meteorological Service, Bamako).

Djoliba is situated on the River Niger's alluvial plain. The study zone sloped gently from a dyke built to contain the floodwaters of the River Niger, but now largely eroded, down to the river bank. There were two main vegetation types in the study zone: a shrub savanna characterised by several tree species, e.g. Ficus gnaphalocarpa (Miq.) A. Rich., Guiera senegalensis J.F. Gmel., Acacia macrostachya Reichenb. and Combretum lecardii Engl. and a riverine forest dominated by Combretum lecardii associated with Dichrostachys glomerata (Forssk.) Chiov., Mitragyna inermis (Willd.) Kuntze, Piliostigma reticulatum (DC.) Hochst. and Guiera senegalensis. Vetiveria nigritana (Benth.) Stapf was the commonest grass species. There were many termite colonies throughout the study area. Traps were laid in a U-shaped pattern, each arm of the U (TS1 and TS2, about 250 m apart, Figure 1) being made up of two groups (80 m apart) of two trapping lines (20 m apart) of 25 traps (L1-L2 and L3-L4). An extra trapping line of 50 traps (D) joined both arms of the U and was actually set up over the dyke referred to above (about 250 m from the River Niger's main watercourse). All traps were 10 m apart and each trap position was recorded via a global positioning system (GPS, with a displayed maximum accuracy of 5 m). In the course of the study, 27 individuals were recorded travelling between the separate components (D, TS1 and TS2) of the trapping pattern; for this reason, all capturerecapture data were analysed together.

#### **Trapping schedule**

Twenty-one primary trapping sessions (PTSs) were carried out from July 2000 to January 2004. The average time between two consecutive PTSs was 64 d (range: 27–119). To deal with the unequal time intervals between PTSs, all survival and seniority probabilities were standardised to 7 d. Each PTS lasted from 4 to 7 d. Traps were baited with groundnut paste, set in the late afternoon and checked every morning. In this work, we focus on *Mastomys erythroleucus* (Temminck, 1853) which represented more than 90% of all captures but six other rodent species were also captured at the site: *Taterillus gracilis* (Thomas, 1892), *Mus* (*Nannomys*)



**Figure 1.** Trapping site. The study site was situated 40 km south-west of Bamako in the alluvial plain of the River Niger (Mali  $8^{\circ}12 \text{ W} 12^{\circ}32 \text{ N}$ , see (a). The trapping design was formed of several sets of trapping lines, roughly perpendicular to the shore and connected by an extra trapping line set up on the dyke (see (b) and text for further details). There was a gentle slope from the dyke to the river (see (c)).

musculoides Temminck, 1853, Cricetomys gambianus Waterhouse, 1840, Dasymys rufulus Miller, 1900, Rattus rattus (Linnaeus, 1758) and Arvicanthis ansorgei Thomas, 1910. Small mammals were treated in a humane manner. and in compliance with Malian Centre National de la Recherche Scientifique et Technique authorisations and guidelines of the American Society of Mammalogists (Animal Care and Use Committee 1998). Individuals were sexed, weighed and individually marked by toe-clipping before being released at their capture point. Unfortunately reproductive activity of individuals was not assessed from the first to the twelfth PTS included. Although we are aware that the relationship between age and body weight is not simple in many rodent species (Leirs 1995), it was assumed, as a first approximation, that specimens weighing 20 g or less were young individuals (Granjon

*et al.* 2005). Duplantier (1988), carrying out laboratory crosses, showed that a body weight of 20 g corresponds roughly to an age of 2 mo for both an insular and a continental population of *M. erytholeucus*. By identifying young individuals among the data, we were able to infer the dates of the breeding seasons for each year.

#### Capture-recapture modelling

Capture-recapture data were initially collected under a Pollock's robust design (Pollock 1982) but data were sparse for several trapping sessions. Sparseness of data is known to jeopardize the correct estimation of population size when using closed population models; in particular, with sparse data, the model selection routine in the CAPTURE program becomes unreliable (Hammond & Anthony 2006, Menkins & Anderson 1988). We decided, then, to estimate population sizes at each trapping session without making a model selection. Our a priori expectation was that model M<sub>h</sub> would provide a reasonable model for capture probability since Sluydts et al. (2007) have applied it successfully to a population of *M. natalensis* in Tanzania. We used the jack-knife estimator because it is robust to deviations from underlying models and has performed well in simulations (Boulanger & Krebs 1996) as well as in many case studies (Hammond & Anthony 2006, Karanth & Nichols 1998). Although we favour much the use of population-size estimates from closed-population models to estimate abundance, for comparative purposes we also calculated the Minimum Numbers Known Alive (MNKA, Krebs 1966) given that MNKA have been frequently used in the past in the small mammal literature. For the other demographic parameters (survival and seniority probability), we used an open model approach, focusing only on whether or not an animal had been captured at least once at each of the 21 PTSs (Nichols et al. 2000). Statistical analyses were thus carried out following Lebreton *et al.* (1992) with the joint estimation of a demographic parameter, survival or seniority probability (denoted respectively  $\phi$  and  $\gamma$ ), and a detection probability (denoted respectively in survival and seniority analysis p and r). Specifically, seniority probabilities, which are demographic parameters inversely linked to recruitment, were estimated from reverse-time capturerecapture analysis as detailed in Nichols et al. (2000). For both demographic parameters, the fit of a general model was assessed and found satisfactory and then a model selection was carried out from this general model. Goodness-of-fit (GOF) tests were carried out using UCARE (programme freely downloadable at http://www.cefe.cnrs.fr/BIOM/logiciels.htm). We mainly considered two components of the tests provided by UCARE: test 2.CT and test 3.SR. Test 2.CT detects trap-dependence, i.e. whether or not the probability of recapture of an individual depends upon its previous capture history. Test 3.SR focuses on transience, i.e. the fact that some individuals will pass once through the sampling design and thus never be recaptured (Pradel et al. 2005). Because GOF tests revealed trap-happiness in the data, we used as a general model a model including traphappiness with full-time variation in survival or seniority probability and in the two probabilities of recapture (Gimenez et al. 2003). Because this kind of model, with full-time variation, is known to be beset by serious identifiability problems (Pradel 1993), we attempted first to reduce the full-time variation in recapture probabilities either to simpler models with seasonal and annual variation or no temporal variation at all. In a second step, we ran four models of temporal variation in survival or

seniority (a two-way interaction model between season and year, a model with additive seasonal and annual variation, a model with seasonal variation only and a model with annual variation only) crossed with five recapture models (same temporal variation as for survival probability plus an additive trap-happiness effect). To sum up, the set of candidate models had 28 models for each analysis and they are listed in Appendix 1. Following Burnham & Anderson (1998), all models were ranked by Akaike's Information Criterion corrected for small sample size  $(AIC_c)$ : the better the model, the smaller the criterion. As recommended by Burnham & Anderson (1998), for each model we calculated the difference in AIC<sub>c</sub> from the model with the lowest AIC<sub>c</sub> score (noted  $\Delta AIC_c$ ), the Akaike weights (noted AIC<sub>c</sub> weights) and considered all models with  $\Delta AIC_c \ge 10$  as essentially not supported by the data. Further, as a rule of thumb, two models with  $\Delta AIC_c < 2$  are not distinguishable on statistical grounds. In this case, for the sake of parsimony, we considered best the model with the fewest parameters. We used analyses of deviance to test for the effects of external covariates (ANODEV, Skalski et al. 1993). All models were fitted in Mark 4.2 (White & Burnham 1999). All estimates of demographic parameters come with 95% confidence interval support limits between parentheses.

#### **Biological covariates**

Because we wanted to investigate the impact of the annual flood of the River Niger on the demography of *M. erythroleucus*, we considered the variable year as starting just around the maximum of the flood (usually in late September). Additionally, we divided the year into a dry season and a rainy season.

Two extrinsic covariates representing different hypotheses about the functioning of the Mastomys population were used. First, in arid and semi-arid environments, rainfall has typically been used as a surrogate measurement for primary production generally thought to be connected with both food and shelter availability for small mammals (Brown & Singleton 1999, Holmgren et al. 2006, Hubert 1982). Rainfall is known to have a marked effect on Mastomys reproduction for several species and countries (Leirs 1995, p. 73) and Julliard et al. (1999) have recently reported a close connection between survival and rainfall for M. natalensis in Tanzania. Thus we used the cumulative rainfall measured in a given time interval between two trapping sessions (cumr) to explain the temporal variation in both survival and seniority probabilities. We expected a positive relationship between survival and rainfall and a negative relationship between seniority and rainfall (the more rainfall, the greater recruitment). Monthly rainfall data were recorded at Bamako (40 km from



Figure 2. Variation of monthly water level (1999–2005) at Koulikoro (a) and rainfall at Bamako (2000–2003) (b). Numbers and bars on top of each bar display respectively the mean and the upper confidence limit at 95%.

our study site). Second, we used the daily water level of the River Niger (wl) recorded at Koulikoro (70 km downstream from our study site) averaged over time intervals separating two consecutive PTSs to assess the impact of the flood on demographic parameters (Figure 2). We expected an inverse relationship between survival and water level (higher water levels mean lower survival because of flooding) and a direct relationship between seniority and water level (higher water levels mean lower recruitment). Finally, given the importance of density-dependence relationships previously described in small mammals in general and *Mastomys* in particular, we used the estimates of abundance from closed-population models (abund) to explore the relationships between abundance and seniority or survival. We had no a priori expectations about the relationship between abundance and survival because both direct and inverse relationships have been reported in *Mastomys*, depending for instance on functional categories (Julliard *et al.* 1999), but we

**Table 1.** Trapping schedule and estimates of abundance at each primary trapping session. PTS = primary trapping session; # : no recapture at this PTS; p = probability of capture estimated from closed population models; N = population size estimated from closed population models (M<sub>h</sub> with the jack-knife estimator) and the associated standard error; MNKA = Minimum Number Known Alive. Column labelled 'Weight' gives the average weight and associated standard error in grams of all individuals caught at the PTS. Column labelled ' $\leq$  20 g' gives the number of individuals whose weight was inferior or equal to 20 g at each PTS (- = means no capture of this kind of individual). The trapping session the closest to the maximum of the flooding is indicated in bold for each year.

PTS	Dates of PTS	Р	N (mean $\pm$ SE)	MNKA	Weight (g) (mean $\pm$ SE)	$\leq 20 \text{ g}$
1	15–21 July 2000	0.25	$46 \pm 6.2$	35	$54.2 \pm 2.6$	1
2	24-30 September 2000	0.14	$4 \pm 3.2 \#$	6	$65.8 \pm 16.7$	_
3	5–11 November 2000	0.11	$13 \pm 4.1$	9	$38.6 \pm 4.1$	_
4	15–19 December 2000	0.19	$221\pm20.4$	123	$35.6 \pm 1.5$	29
5	21–27 February 2001	0.23	$149\pm8.7$	116	$30.9 \pm 1.0$	10
6	23–29 May 2001	0.21	$49 \pm 5.6$	44	$39.7 \pm 1.5$	_
7	6–12 July 2001	0.18	$61 \pm 11.3$	36	$42.4 \pm 1.2$	_
8	14-20 October 2001	0.13	$10 \pm 3.3$	8	$46.3 \pm 7.8$	_
9	19–24 November 2001	0.18	$16\pm4.09$	12	$49.5\pm2.4$	_
10	22–27 December 2001	0.21	$48 \pm 5.3$	37	$43.9\pm2.1$	1
11	22–27 January 2002	0.10	$163\pm21.5$	70	$29.6 \pm 1.4$	15
12	3-8 April 2002	0.17	$26 \pm 5.81$	23	$32.2 \pm 2.6$	_
13	6–11 June 2002	0.25	$25 \pm 3.9$	23	$45.3\pm2.1$	_
14	4-9 September 2002	0.18	$39 \pm 7.6$	25	$76.2 \pm 3.2$	_
15	16-21 November 2002	0.06	$37 \pm 9.8$	12	$54.9 \pm 5.6$	_
16	29 January–3 February 2003	0.13	$416 \pm 34.9$	209	$29.8 \pm 0.7$	35
17	9–14 April 2003	0.10	$137 \pm 19.3$	64	$30.7 \pm 1.0$	4
18	6–11 August 2003	0.32	$53 \pm 4.8$	44	$58.4 \pm 2.3$	-
19	18-23 October 2003	0.17	$3 \pm 2.1 \#$	3	$54.0 \pm 2.0$	_
20	14-19 November 2003	0.08	$34 \pm 9.0$	12	$48.3\pm4.4$	1
21	14–19 January 2004	0.09	$543 \pm 39.4$	223	$30.7\pm0.8$	46

expected rather a direct relationship in seniority as parameters linked to recruitment like maturation rates of females were indeed shown to decrease with density (Julliard *et al.* 1999, Leirs 1995, Sluydts *et al.* 2007). We refrained from performing a test of delayed density dependence because unfortunately we could not come up with any clear working hypothesis in our system. All covariates were standardized to help convergence (White & Burnham 1999).

# RESULTS

## Basics

Out of 915 individuals marked (496 males), 155 individuals were caught in at least two different PTSs (2 PTSs: 129, 3 PTSs: 20, 4 PTSs: 5 and 5 PTSs: 1). Fifty-three per cent of individuals were never recaptured (i.e. even within a given PTS). The effective sample size, i.e. the number of captures and recaptures minus the number of captures at the last PTS, was 873 in the data set used for the survival analysis and 1068 in the data set used for the seniority analysis.

Even if average capture probabilities estimated from model  $M_h$  were relatively low (mean = 0.16, 95% CI = 0.13-0.19), estimates of population size were correct on the whole as shown by the reasonably small associated

standard errors (Table 1, Figure 3). PTSs 2 and 19, where there was no recapture at all, are the two exceptions to this pattern. Population sizes varied greatly between years and within a given year (Figure 3). However, maximum numbers were generally reached in December–January (i.e. during the first part of the dry season) and minimum numbers in September–October (i.e. at the end of the rainy season). The average individual weight of the population displayed similar seasonal variations with a low around January and a high around September. Except for one individual captured in July 2000 and four individuals captured in April 2003, young individuals appeared only at trapping sessions from November to February, with most individuals found in January.

#### GOF tests and the general model

For both survival and seniority analyses, test 2.CT was the only significant component, indicating traphappiness: the probability of recapture was higher if the individual had already been captured at the previous trapping session than if it had not been (test 2.CT: z = -1.99, P = 0.046). Thus we used as a starting point for model selection a general model including traphappiness (denoted  $\phi_{(t)}$  or  $\gamma_{(t)} p_{(m \times t)}$ , Appendix 1). The model fitted the data satisfactorily ( $\chi^2 = 9.5$ , df = 10, P = 0.48).



**Figure 3.** Estimate of abundance (a), survival (b) and seniority probabilities (c) with their 95% confidence limits (ticks). Abundance was estimated from model  $M_h$ . Survival and seniority probability estimates are from the best models and standardized to 7 d. A few points are on the boundary of the parameter space (i.e. equal to 0 and 1) and consequently no confidence intervals are displayed since standard likelihood theory cannot provide sensible estimates of standard errors for parameter estimates lying on a boundary. Vertical dashed bars represent for each year the maximum intensity of the flooding events measured at Koulikoro, a site 70 km downstream from our study site.

**Table 2.** Models in survival probabilities ranked by AIC<sub>c</sub>. Only the first five models run are displayed; however other models run were essentially not supported by the data ( $\Delta AIC_c \ge 10$ , Burnham & Anderson 1998). Best model is shown in bold. AIC<sub>c</sub> = Akaike's Information Criterion;  $\Delta AIC_c$  = difference in AICc with the score of best model; AIC<sub>c</sub> Weight = Akaike's weight; DEV = deviance; np = number of identifiable parameters; m = trap-happiness effect; t = full-time variation; s = seasonal variation; y = annual variation.

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Survival	Recapture	AIC <sub>c</sub> Weight	AIC <sub>c</sub>	$\Delta AIC_{c}$	np	DEV
t	m	0.53	1015.36	0.00	22	63.75
t	m + s	0.27	1016.74	1.38	23	63.02
t	m + y	0.12	1018.39	3.03	25	60.44
t	m + s + y	0.07	1019.26	3.90	26	59.19
t	$m+s\times y$	0.00	1025.38	10.02	29	58.90

**Table 3.** Models in seniority probabilities ranked by AIC<sub>c</sub>. Only the first five models run are displayed; however other models run were essentially not supported by the data ( $\Delta AIC_c \ge 10$ , see Burnham & Anderson 1998). Best model is shown in bold. AIC<sub>c</sub> = Akaike's Information Criterion;  $\Delta AIC_c$  = difference in AICc with the score of best model; AIC<sub>c</sub> Weight = Akaike's weight; DEV = deviance; np = number of identifiable parameters; m = trap-happiness effect; t = full-time variation; s = seasonal variation; y = annual variation.

Seniority	Recapture	AIC <sub>c</sub> Weight	AIC <sub>c</sub>	$\Delta AIC_{c}$	np	DEV
t	m	0.69	809.99	0.00	22	68.38
t	m + s	0.26	811.96	1.96	23	68.26
t	m + y	0.03	816.02	6.02	25	68.12
t	m + s + y	0.01	817.67	7.68	26	67.68
t	$\boldsymbol{m} + \boldsymbol{s} \times \boldsymbol{y}$	0.00	821.39	11.40	29	65.07

#### Model selection for capture-recapture data

Model selection was similar for both survival and seniority probability, and three points are worth commenting on: (1) Reducing the full-time variation in recapture probabilities considerably improved the fit of the model (from the general model, AIC<sub>c</sub> decreased by a minimum of 30 units, Appendix 1). However, there was some uncertainty about temporal variation in recapture probabilities as lowranked models differed only slightly by their recapture modelling (Tables 2 and 3). (2) Models including traphappiness reached significantly lower AIC<sub>c</sub> values than other models without trap-happiness ( $\Delta AIC_c = 2.2$  and 5.5, for seniority and survival analysis, respectively). In the survival analysis, the probability of recapture for the individuals trapped at the previous primary session was 0.427 (0.299–0.565) vs. 0.164 (0.057–0.389) for those individuals not trapped at the previous primary session. In the seniority analysis, the probabilities of recapture were 0.560 (0.465-0.652) vs. 0.342 (0.166-(0.574), respectively. (3) It was not possible to reduce the full-time variation in survival without altering the fit of the model significantly: the first model with reduced temporal variation, namely  $s \times y$ , for survival as well as for seniority, differed by more than 32 units from the lowest AIC<sub>c</sub> model. Thus both survival and seniority

probabilities varied greatly over the study, offering a unique opportunity to test for the effect of covariates (Figure 3).

Season and water level explained 51% of the temporal variation in survival probabilities ( $F_{(2, 17)} = 8.90$ , P = 0.0023). The slope of water level was negative, meaning that survival probabilities decreased when water level increased, as we expected  $(\beta(wl) = -0.72 \ (-1.00))$ -0.45). We interpret this inverse relationship in terms of the impact of the overall flooding of the area as it is hard to believe that day-to-day variation in water level can reduce local survival of rodents. Abundance was not confirmed as having a significant effect on survival probabilities (ANODEV P > 0.10). Conversely, 86% of the temporal variation in seniority probabilities was explained by a model with season, water level, abundance and their interaction  $(F_{(4, 15)} = 22.5, P = 3.4 \times 10^{-6})$ . The interaction was negative and significant, meaning that the seniority probabilities varied with both water level and abundance values ( $\beta$ (abund) = 0.74 (-1.03; 2.52);  $\beta$ (wl) = -1.73 (-2.82; -0.64);  $\beta$ (abund.wl) = -2.56 (-4.86; -0.27). Lastly, the effect of cumulative rainfall was not confirmed in either the survival or the seniority probabilities (ANODEV all P > 0.10).

## DISCUSSION

#### **Recapture probability**

Our results showed significant trap-happiness i.e. the probability of recapture varied with each individual's capture history (Pradel 1993). In terms of behaviour, one might argue that, because previously caught individuals have learned that traps contain food, they will actively seek to enter the traps again so raising their probability of recapture compared with individuals not having experienced trapping. This hypothesis has been suggested for two Chilean populations of the leaf-eared mouse Phyllotis darwini, which inhabits semi-arid environments (Crespin & Lima 2006, Lima et al. 2003), and there is some evidence indeed that food availability impacts trapping in small mammals (Adler & Lambert 1997). However, given that the time intervals between two consecutive PTSs can be several months long, a more extensive study is needed to confirm that this trap-happiness is the consequence of a behavioural shift of the individuals rather than a mere consequence of heterogeneity of capture (Kendall et al. 1995, Pradel 1993).

#### Survival and seniority probabilities

Although the trapping sessions were not regularly spaced in time in our study, our results indicate that the breeding

season of M. erythroleucus generally starts at the end of the wet season and extends into the beginning of the dry season, which is consistent with other studies of murine rodents in Senegal (Granjon 1987, Hubert 1982). This seasonality has far-reaching consequences for *M. erythroleucus* population dynamics as shown by the fluctuations in abundance observed each year in our data (Figure 3). However, the model selection failed to retain seasonality: for seniority and survival probabilities alike, the best models were indeed full-time dependent models while seasonal models were not supported by the data. This may be because the data encompass only 4 y and because, with three estimates out of seven equal to zero for both seniority and survival probabilities, the last 2 y did not yield much information about seasonality. We believe that, with data for many more years, a model with only seasonal and annual variation would have proved the best model.

Although the best model did not include seasonality formally, it showed that, within a year, survival probabilities tended to be low after the flooding event and to rise thereafter. For instance, survival fell from 0.83 (0.73; 0.90) to 0.69 (0.39; 0.88) after the second flood, and then increased up to 1. Then, survival fell from 0.77 (0.59; 0.88) to 0 after the third flood and then rose to 0.94 (0.90; 0.97). Similarly, survival increased from 0 to 0.83 (0.58; 0.95) after the fourth flood. Given that (1) the survival probabilities estimated here were for local survival (i.e. that permanent emigration out of the study zone is equivalent to death), that (2) M. erytholeucus can swim a little (Duplantier & Bâ 2001), that (3) the differences in survival, before and after the spate, were high, and that (4) local survival fell as a function of mean water level in our study, we believe that this drop in survival was mainly due to emigration out of the flooded areas. Even so, it is likely some rodents either drowned or starved to death (Anderson & Shapiro 1957, Batzli 1977, Jacob 2003), particularly when all habitats were flooded for a relatively long time, which sometimes happened at our study site, e.g. in September 2001. Finally, it is likely that the individuals recolonizing new habitats when the flood abated were old as suggested by the relatively high average individual weight at the trapping sessions close to the spate; this observation is consistent with the results of Hubert (1982) who, using lens-weight data, described a Senegalese population of M. *erythroleucus* as old on average at the end of the rainy season. Thus it is logical that, in our survey, survival tended to decline after the spate compared with before. The subsequent increase in survival is associated with the production of the new generation, accompanying the vegetation growth triggered by rainfall (representing food and shelter for rodents).

There was no relationship between survival or seniority and rainfall, contrary to our expectations. However, we

note that rainfall may have direct and delayed effects on survival in the same functional category of *M. natalensis* and further that these effects impact functional categories in a different way (Julliard *et al.* 1999). Lima *et al.* (2001) have shown that rainfall may produce opposing effects across different demographic parameters, e.g. maturation rate and recruitment rate of females for *Phyllotis darwini*, a small rodent inhabiting semi-arid environment in central Chile. Thus the occurrence of more complex relationships than the linear effect on pooled males and females we have tested may explain why we were unable to pick up a signal with rainfall in our 4-y study.

As for seniority probabilities, best model estimates displayed marked seasonal variation. Values of seniority probabilities reached a relatively brief low around November-December (in 2000 the low reached 0.59 (0.49; 0.68) and in 2001 0.63 (0.37; 0.83) as already noted by Hubert (1982) for same species in Senegal. Further, the temporal variation in seniority probabilities was largely explained by a model with season and a negative interaction between abundance and water level, suggesting, in terms of recruitment, that the number of new individuals in the rodent population (i.e. emigration + local reproduction) is indeed impacted by the River Niger but not directly as we first expected, but indirectly depending on both abundance and water-level values. Keeping in mind that water-level variation means that greater or lesser tracts of land are flooded, it is likely that the variation in recruitment in our study is mediated by intraspecific competition for food or refuge during the flood. Low recruitment values generally correspond to high abundance values and low water-level values (five cases out of seven with  $\gamma > 0.99$ ) whereas high recruitment values are attained for low abundance values and moderate water-level values (three cases out of four with  $\gamma < 0.66$ ). A simple interpretation of these features is that high abundances mean intense intraspecific competition (and so low recruitment) and that high water levels lead to a concentration of individuals on unflooded land (and so high recruitment). The negative interaction between abundance and water level is consistent with the recent work of Sluydts et al. (2007) which has shown that, in Tanzanian M. natalensis, female maturation, i.e. the recruitment of adults from the pool of subadult individuals, depends on negative interaction between abundance and rainfall. How can these similar density-dependent relationships be explained? Many authors have already reported that either recruitment or dispersal is impeded at high densities in small-mammal populations (Aars & Ims 2002, Desy et al. 1990, Ostfeld & Canham 1995). Further, Prevôt-Juliard et al. (1999), for a population of Finnish bank voles (Myodes glareolus), a species in which breeding females are known to defend a territory (Bondrup-Nielsen & Ims 1986), have reported that recruitment of new breeding females is negatively correlated with the density

of already established females and so is probably mediated by territorial competition among breeding females. However, as Mastomys does not seem territorial or even aggressive (Leirs 1995 but see Granjon & Duplantier 1993), it is still not clear what the behavioural mechanisms are behind the density-dependence observed in Mastomys. An alternative explanation is that, when water levels are high, small mammals may be concentrated in a few areas that attract predators (the 'pantry' effect, Batzli 1983, Meserve et al. 2001) and/or in which predators consume more individuals. The abundance of small mammals may thus be lowered much by predation, which may in turn favour a high recruitment of small mammals. Conversely, when water levels are moderate, rodents may have more space to escape from predators and so small mammals may be more abundant. Note that Julliard et al. (1999) reported a direct density-dependent relationship in survival of Mastomys natalensis that they interpreted as the outcome of predation. More generally, predation is thought to have a major impact on small-mammal population dynamics (Ims & Andreassen 2000, Lima et al. 2001, Madsen et al. 2006, Stenseth 1999). More work, especially manipulations and/or experiments, is needed to understand the factors shaping density-dependence in *Mastomys*.

#### CONCLUSION

Our results showed that demography of *M. erythroleucus* is strongly impacted by the River Niger, i.e. an extrinsic factor, as both survival and seniority probabilities were affected by its floods. Seniority probabilities also varied with the number of individuals in the population, i.e. an intrinsic factor. More broadly, our results are consistent with the functioning of population described for other rodent species in semi-arid habitats, e.g. M. natalensis in Tanzania (Julliard et al. 1999, Sluydts et al. 2007) or *Phyllotis darwini* in Chile (Lima *et al.* 2001) with a strong impact on demographic rates of both intrinsic and extrinsic factors, such as rainfall and/or predation (owls). More work over a longer period of population monitoring is now needed to better understand the interplay between these different factors, in order to anticipate the potential population changes due to climatic forcing, mediated by the impact of the River Niger.

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**Appendix 1.** Set of models run for the seniority ( $\gamma$ ) and the survival ( $\phi$ ) analysis. This appendix displays only the models not presented in Tables 2 and 3. Models are ranked by the Akaike Information Criterion. For both the seniority and the survival analysis, all models had an Akaike's weight equalling zero. Detection probabilities for each analysis were respectively denoted as *r* and *p*. AIC<sub>c</sub> = Akaike information criterion corrected for small sample sizes; np = number of identifiable parameters; DEV = deviance; m = trap-happiness effect; t = full-time variation; s = seasonal variation; y = annual variation; . = no variation (intercept-only model).

	AIC <sub>c</sub>	np	DEV
Seniority			
$\gamma(t) r(m \times t)$	851.33	59	29.66
$\gamma$ (s + y) r(m + s × y)	1084.80	14	359.76
$\gamma(\mathbf{y}) r(\mathbf{m} + \mathbf{s} \times \mathbf{y})$	1085.43	13	362.44
$\gamma$ (s x y) $r$ (m + s × y)	1087.24	17	356.01
$\gamma$ (s + y) r(m + s)	1093.74	8	380.96
$\gamma$ (s × y) r(m + s)	1094.45	11	375.56
$\gamma$ (s + y) r(m)	1095.61	7	384.86
$\gamma$ (s + y) r(m + s + y)	1096.16	11	377.27
$\gamma$ (s × y) $r$ (m)	1097.44	10	380.59
$\gamma$ (s × y) r(m + s + y)	1097.66	14	372.62
$\gamma$ (s + y) r(m + y)	1099.24	10	382.39
$\gamma(\mathbf{y}) r(\mathbf{m})$	1099.32	6	390.59
$\gamma(y) r(m+s)$	1100.27	7	389.52
$\gamma(\mathbf{y}) r(\mathbf{m} + \mathbf{s} + \mathbf{y})$	1101.24	10	384.39
$\gamma(\mathbf{y}) r(\mathbf{m} + \mathbf{y})$	1101.58	9	386.76
$\gamma$ (s × y) $r$ (m + y)	1101.99	13	379.00
$\gamma(s) r(m + s \times y)$	1125.94	11	407.04
$\gamma$ (s) $r(m + s + y)$	1148.58	8	435.80
$\gamma(s) r(m+y)$	1153.98	7	443.23
$\gamma(s) r(m+s)$	1183.32	5	476.62
$\gamma(s) r(m)$	1201.78	4	497.10
$\gamma(.) r(m)$	1205.07	3	502.41
Survival			
$\phi(\mathbf{s} \times \mathbf{y}) p(\mathbf{m} + \mathbf{s} + \mathbf{y})$	1050.48	14	115.57
$\phi(\mathbf{s} \times \mathbf{y}) p(\mathbf{m} + \mathbf{y})$	1051.35	13	118.52
$\phi(\mathbf{s} \times \mathbf{y}) p(\mathbf{m} + \mathbf{s} \times \mathbf{y})$	1052.33	17	111.20
$\phi(\mathbf{s} \times \mathbf{y}) p(\mathbf{m} + \mathbf{s})$	1060.89	11	132.17
$\phi(\mathbf{y}) p(\mathbf{m} + \mathbf{s} + \mathbf{y})$	1060.96	10	134.29
$\phi(\mathbf{y}) p(\mathbf{m} + \mathbf{s} \times \mathbf{y})$	1061.40	13	128.56
$\phi(\mathbf{y}) p(\mathbf{m} + \mathbf{s})$	1062.02	7	141.48
$\phi(\mathbf{s} \times \mathbf{y}) p(\mathbf{m})$	1062.19	10	135.52
$\phi(t) p(m \times t)$	1062.91	59	29.78
$\phi(s+y) p(m+s+y)$	1063.01	11	134.29
$\phi(s+y) p(m+s \times y)$	1063.28	14	128.38
$\phi(s+y) p(m+s)$	1064.02	8	141.44
$\phi(\mathbf{y}) p(\mathbf{m} + \mathbf{y})$	1064.79	9	140.16
$\phi(\mathbf{y}) p(\mathbf{m})$	1065.77	6	147.26
$\phi(s+y) p(m+y)$	1066.24	10	139.58
$\phi(s+y) p(m)$	1067.21	7	146.67
$\phi(s) p(m+s+y)$	1070.56	8	147.98
$\phi(s) p(m+y)$	1072.23	7	151.69
$\phi(\mathbf{s}) p(\mathbf{m} + \mathbf{s} \times \mathbf{y})$	1073.37	11	144.65
$\phi(\mathbf{s}) p(\mathbf{m})$	1074.20	4	159.74
$\phi(s) p(m+s)$	1074.32	5	157.84
$\phi(.) p(\mathbf{m})$	1075.46	3	163.02