plaining social interactions is not entirely convincing. The spirit behind this attempt should be praised, yet psychological game theory as defined and exemplified by Colman does not offer a truly viable solution. The key problem is that the suggested solutions are theoretically under-specified, quite limited in scope, and lead to a second-order indeterminacy.

To illustrate my point I will focus on the concept of "team reasoning." What is so special about team reasoning that cannot be said about other ways of reasoning? For example, one might define "altruistic reasoning," "individualistic reasoning," "fairness reasoning," "reciprocity reasoning," and so on, in the same kind of holistic way as the definition is offered for "team reasoning." It is easy to find examples of games that can be solved using some of these concepts; although they can be solved promptly also via "team reasoning," the intuition is that it would not necessarily be the best solution concept. By best solution concept I mean a concept that is intuitively compelling and likely to be empirically supported with actual behavioral data.

I will present two examples of games. For the first example, let's consider all modified coordination games for two players with asymmetrical payoffs. Let's consider this asymmetric coordination game with the following payoffs and choices (Fig. 1):

As for every coordination game, a standard analysis would show two Nash equilibria (H, H and L, L), and the issue would be how to select one of the two. Applying a team reasoning would single out H, H as the best equilibrium. Would this be a compelling solution? I doubt it. If I were Player I, I would think twice before choosing H. By applying "fairness reasoning" or "Reciprocity reasoning," I could anticipate that Player II would like L, L much more than H, H (or, put differently, dislike much more the inequality of payoffs resulting from H, H). I would therefore anticipate that the other player would play L, and as a consequence I would decide to play L. On the other hand, if I were to apply "altruistic reasoning" or "individualistic reasoning," for opposite reasons I should come to the conclusion that Player II will play H, and hence so would I. The problem is threefold: First, we can list a series of reasoning concepts besides "team reasoning"; second, psychological game theory, as defined by Colman, would offer no tools to select among these different reasoning concepts; and third, the solution concept which would be the best for a player, depends on his expectations about the other player's type.

The second example is perhaps even more intriguing.<sup>1</sup> The Ultimatum Game (UG) is a well-known paradigm that has been the subject of several studies in experimental economics and in social psychology. The UG is a very simple game whereby two players bargain over a given monetary endowment. The first player proposes a division of the endowment and the second player can either accept or refuse it. If she refuses it, both players end up with nothing. Orthodox game theory predicts that the first player will propose a small amount for the second player (e.g., 99% for self vs. 1% for other) and the second player will accept the proposal. However, several experimental studies have found systematic deviations from these predictions (e.g., Guth 1995; Thaler 1988). It is well established that a consistent portion of second players would reject low offers (e.g., 25% or lower) even though this means that both players end up with nothing. What about team reasoning? A team-reasoning second player should never reject any offer, because from the perspective of a second player the strategy that maximizes the joint payoff is to accept any offer. In

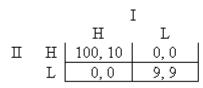


Figure 1 (Perugini). Example of a coordination game with asymmetric payoffs.

fact, for every offer, the alternative would be to reject it, which is always dominated in terms of joint payoffs, given that it implies no payoff for both players. Therefore, a team reasoning second player would be equally likely to accept a 1/99 or a 50/50 split. The intriguing conclusion is that a team-reasoning player often will behave exactly as dictated by orthodox game theory, even in those situations where our intuition would suggest we do otherwise.

Equally problematic are those cases where team reasoning offers different predictions from orthodox game theory. Take social dilemmas. Of course, social dilemmas can be solved by using team reasoning, but this is equally true for several of the nonstandard solution concepts that I have sketched previously. I wonder how well a team reasoning concept would fare when compared with other nonstandard solution concepts across a comprehensive range of social dilemmas. To sum up, I am not convinced that team reasoning can be a good solution to much more than the specific example of the Hi-Lo matching game with symmetrical payoffs illustrated by Colman. But then, why should it not be named "matching reasoning" instead?

These examples illustrate my main problem with Colman's suggestions: Concepts such as team reasoning must be defined more precisely, which ultimately means that it will be necessary to specify the payoffs involved, how they are transformed, and under which conditions each solution concept primarily applies. The preceding examples have made clear that an important parameter is the symmetry of the payoffs for the players: Everything else being equal, the more asymmetrical the payoffs, the less likely is that team reasoning can offer a compelling solution for all players. But this implies that the team reasoning concept should specify what level of asymmetry is acceptable to the players, which ultimately means to specify some function of weighting the payoffs involved. Only in this way can the solution concepts pass more stringent theoretical and empirical tests. The alternative would be to have a storage bin full of loose ad-hoc reasoning concepts that can be used post-hoc for different situations, but without any rule that specifies when and why they should be adopted. In other words, ironically, the lack of a reason for choosing, which was the main point behind many of Colman's sharp criticisms on the indeterminacy of orthodox game theory, will strike back with a vengeance. Without specifying the concepts more precisely – given that they can explain or predict only some interactions and not others, and that alternative nonstandard concepts can be compellingly applied in several circumstances - we will be left without any reason why to apply a given nonstandard psychological solution concept in the first place.

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#### NOTE

1. I owe this example to Tim Rakow.

# Chance, utility, rationality, strategy, equilibrium

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**Abstract:** Almost anyone seriously interested in decision theory will name John von Neumann's (1928) Minimax Theorem as its foundation, whereas Utility and Rationality are imagined to be the twin towers on which the theory rests. Yet, experimental results and real-life observations seldom support that expectation. Over two centuries ago, Hume (1739–40/1978) put his finger on the discrepancy. "Reason," he wrote "is, and ought to be the slave of passions, and can never pretend to any other office than to serve and obey them." In other words, effective means to reach specific goals can be prescribed, but not the goals. A wide range of experimental results and daily life behavior support this dictum. In November 1945, a conference of mathematicians was held at the Museum of Science and Industry in Chicago. A robot was displayed in the entrance hall, inviting the visitors to play a game of tic-tac-toe. Needless to say, regardless of who made the first move, every game ended either in a draw or in a win for the robot. Many were impressed. Today, an exhibit of this sort would be unthinkable, except, possibly in a children's section.

The term "game," in the context of interacting actors with usually different goals, was introduced by von Neumann and Morgenstern (1944) in their seminal treatise *Theory of Games and Economic Behavior*. It will surprise many that von Neumann did not recognize chess as a "game" in the sense that he used the term.

"Chess is not a game," von Neumann told Jacob Bronowski, who worked with him during World War II (Poundstone 1992, p. 6). He meant that there is a "correct" way to play the game – although no one presently knows what it is – and that the game should therefore be trivial, in much the same sense as tic-tac-toe is trivial to players aware of a "correct" strategy.

It turned out that the inspiration for game theory was not chess or any parlor game, which can be shown to have one or more "correct" ways to play it, but poker instead, where it is not possible to guess with certainty the choice of strategy of one's opponent(s).

According to Luce and von Winterfeldt (1994), "[M]ost people in real situations attempt to behave in accord with the most basic (conventional) rationality principles, although they are likely to fail in more complex situations." The "situations" are not mentioned, but one can surmise that "utility" is (perhaps tacitly) represented in them by a linear function of some "good" (money, survivors), and that expected utilities are either given (EU) or subjectively assumed (SEU).

This observation tends to imply that normative (prescriptive) decision theory has a positive role to play along with recent empirical descriptive approaches, which seek to gain understanding of how people actually make decisions in a great variety of situations. Yet, already in the late eighteenth century, maximization of expected utility was shown to lead to absurd results in the socalled Petersburg Paradox. A fair coin is thrown. The gambler wins  $n2^{n-1}$  rubles if "heads" appears n times before the first "tails." The gambler's expected gain is infinite. Daniel Bernoulli (1738/1954), to whom the invention of the game is attributed, modified the rule, whereby expected utility increased logarithmically rather than linearly with n. This still made the expected gain, and thus a "rational" maximum stake, enormous, and hence unacceptable to any "rational" player. Indeed, as long as expected gain increases monotonically with *n*, a rule can be devised to make the expected gain enormous. No "rational" gambler can be expected to pay anywhere near it for the privilege of playing the game once.

Passing from gambling to two-or-more-person games, we encounter similar difficulties with prescriptive decision theory. Especially impressive are paradoxes resulting from backward induction. Consider the Prisoner's Dilemma game played a large known number of times. In a single play, defection by both players is a minimax outcome, which, according to von Neumann, is the only rational one. In a long sequence of plays, however, one might suppose that repeated cooperation (CC) might emerge, as each player forestalls the other's "revenge" for defection. Nevertheless, the last "rational" outcome ought to be double defection (DD), because no retaliation can follow. Given this conclusion, the next to the last play also ought to be (DD), and so on down to the first play.

When Flood and Dresher, discoverers of the Prisoner's Dilemma game (Poundstone 1992), reported to von Neumann that in a long sequence of plays of the game, the outcome was not at all a solid string of DD's, as predicted by the minimax theorem, the great mathematician did not take the result of the admittedly informal experiment seriously. Subsequent experiments, however, showed that, especially in long repeated plays, substantial runs of CC are a rule rather than an exception. Even in single plays by total strangers, frequent CC outcomes have been observed (Rapoport 1988).

Colman cites backward induction in "Centipede," a weirdly designed multi-move game in which both players could win fabulous sums if they tacitly agreed to cooperate after the first play. Nevertheless, backward induction would dictate stopping after the first play, whereby both would receive zero. In contrast, backward induction in R. Selten's "Chain Store" game prescribes CC throughout. The inventor of the game writes that, in the role of the chain store, he would not play as prescribed and presumably would get more money (Selten 1978). Luce and Raiffa (1957) also preferred to violate the backward induction prescription in finitely repeated Prisoner's Dilemma, thus avoiding the only minimax equilibrium of this game.

It turns out that these frequent failures of rational choice theory to prescribe acceptable actions in gambling or game-like situations can be traced to two often tacitly implied assumptions, namely, rejection of so called "evidential" decision theory (Joyce 1999) and independence of decisions of individual players.

Suppose a believer in predestination (Calvinist, Presbyterian) is asked why, if his ultimate abode is fixed, he leads a sober and chaste life. Why doesn't he drink, gamble, chase women, and so on while he can? He might answer, "Since God is just, I can assume that I am among the saved, because I live as I live." He considers his frugal and chaste life as "evidence" that he has been saved and he cherishes this feeling (Joyce 1999).

Asked why he bothers to vote in a general election, seeing that his vote can't possibly make a difference in the result, Herr Kant replies, "I vote, because I would like everyone to vote and because it makes me feel that I have done my duty as a citizen." In the wilderness, Dr. Z has one dose of a life-saving medicine. If given to Mr. X, it will save his life with a probability of 0.9; if given to Mr. Y it has a probability of 0.95. Maximization of expected utility demands that she give the medicine to Mr. Y. But Dr. Z tosses a fair coin to decide. She doesn't want to "play God."

The concept of rationality in classical prescriptive decision theory has three weak spots: individualism, decision independence, and the minimax equilibrium dogma. "Individualism" in this context means "egoism." To avoid the pejorative connotation, Wicksteed (1933) called it "non-tuism." Decision independence is dropped in evidential decision theory. "However I decide, so will my co-players, since there is no reason to suppose that they think not as I do." This perspective dethrones the Nash equilibrium from its role as a *sine qua non* condition of rational choice.

In spite of his generous appreciation of game-theoretic contributions to decision theory, Colman effectively pronounces the end of prescriptive theory founded on the orthodox paradigm, and discusses the promising dawn of inductive experimental-psychological approaches.

## Why not go all the way

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**Abstract:** "Psychology Game Theory" grafts social-process explanations onto classical game theory to explain deviations from instrumental rationality caused by the social properties of cooperation. This leads to confusion between cooperation as a social or individual behavior, and between *ultimate* and *proximate* explanations. If game theory models explain the existence of cooperation, different models are needed for understanding the proximate social processes that underlie cooperation in the real world.

Colman's provocative paper reminds me of a familiar scenario in science. A popular doctrine is under stress but refuses to die. Instead, it is amended again and again in a vain attempt to forge an accommodation with a new reality. A good example is the assumption that individual self-interest, which can explain the evolution of cooperation, must also underlie the *behavior* of cooperating in the real world. Colman characterizes this assumption (from Hume) as "instrumental rationality." The stress comes from