

# Mechanisms of dynamic near-wake modulation of a utility-scale wind turbine

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(Received 10 March 2021; revised 27 June 2021; accepted 15 August 2021)

The current study uses large eddy simulations to investigate the transient response of a utility-scale wind turbine wake to dynamic changes in atmospheric and operational conditions, as observed in previous field-scale measurements. Most wind turbine wake investigations assume quasi-steady conditions, but real wind turbines operate in a highly stochastic atmosphere, and their operation (e.g. blade pitch, yaw angle) changes constantly in response. Furthermore, dynamic control strategies have been recently proposed to optimize wind farm power generation and longevity. Therefore, improved understanding of dynamic wake behaviours is essential. First, changes in blade pitch are investigated and the wake expansion response is found to display hysteresis as a result of flow inertia. The time scales of the wake response to different pitch rates are quantified. Next, changes in wind direction with different time scales are explored. Under short time scales, the wake deflection is in the opposite direction of that observed under quasi-steady conditions. Finally, yaw changes are implemented at different rates, and the maximum inverse wake deflection and time scale are quantified, showing a clear dependence on yaw rate. To gain further physical understanding of the mechanism behind the inverse wake deflection, the streamwise vorticity in different parts of the wake is quantified. The results of this study provide guidance for the design of advanced wake flow control algorithms. The lag in wake response observed for both blade pitch and yaw changes shows that proposed dynamic control strategies must implement turbine operational changes with a time scale of the order of the rotor time scale or slower.

**Key words:** flow-structure interactions, vortex dynamics, wakes

## 1. Introduction

Utility-scale wind turbines operate in highly stochastic atmospheric conditions and are subject to constant changes in wind speed, direction and turbulence. Simplified models of

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these conditions can be developed, but they cannot be fully replicated in the laboratory or in simulations. Moreover, turbine operation (e.g. blade pitch, rotor speed, yaw angle) is constantly adapting to these changes, further increasing the complexity of the fluid–structure interactions that wind turbines experience. Improved understanding of these dynamic interactions is essential for continued increases in turbine size and efficiency (Stevens & Meneveau 2017; Porté-Agel, Bastankhah & Shamsoddin 2018; Veers 2019).

Dasari *et al.* (2019) first explored the effect of changes in blade pitch on the wake of a 2.5 MW wind turbine in the field, finding significant impact on wake expansion and blade tip vortex behaviour. Another recent field-scale study investigated the effect of dynamic conditions, including wind direction, blade pitch and tip speed ratio (ratio of the speed of the blade tips to the incoming wind speed), on the wake of the same 2.5 MW turbine (Abraham & Hong 2020). Using super-large-scale flow visualization with natural snowfall, this investigation revealed the significant impact of changes in atmospheric and operational conditions on wake deflection and expansion, termed dynamic wake modulation. Changes in blade pitch and tip speed ratio were shown to cause fluctuations in the wake expansion angle and, remarkably, dynamic changes in wind direction were found to deflect the wake in the opposite direction of that observed under steady conditions. Furthermore, these dynamic wake behaviours were shown to enhance mixing up to 20 %, accelerating wake recovery. While these findings provided many useful insights into wake behaviours in the field, the underlying mechanisms causing these behaviours were not clear due to the inherent limitations of field studies, including the limited field of view and the lack of control over wind conditions.

Laboratory-scale experiments allow for greater control over flow conditions, enabling direct observation of the transient wake response to dynamic conditions. Yu *et al.* (2017) used an actuator disk in a wind tunnel to investigate the effects of step changes in the thrust coefficient on the loading and wake. They observed an overshoot or undershoot of the wake velocity response, depending on the direction of the thrust coefficient change, attributed to passage of the vorticity shed from the disk edge. With a similar set-up, Macrí *et al.* (2021) studied step changes in yaw angle. They found a lag in wake deflection and thrust coefficient response of the order of the yaw manoeuvre duration. To investigate the effect of dynamic inflow on turbine blade loading, Schepers (2007) implemented step changes in blade pitch on a 2-bladed, 10 m diameter turbine in the NASA-Ames wind tunnel. In this experiment, load overshoots were observed before a gradual approach to the new equilibrium. Berger & Kühn (2018) conducted a similar study to investigate the impact of fast changes in blade pitch on a scaled turbine model and its wake. They also recorded overshoot and undershoot of turbine loading in addition to a decaying wake velocity response attributed to flow inertia. Although these experimental studies successfully isolated individual parameters to determine their effect on the wake, the mechanisms causing the wake changes are still not clear due to their inability to directly observe all variables (e.g. vorticity) at all locations around the rotor. Furthermore, the scalability of wind tunnel experiments is limited by constraints on the physical scale and mechanical characteristics of model turbines and the challenge of replicating the complexity of atmospheric flow.

Simulations have the potential to elucidate these mechanisms, as flow and turbine parameters can be easily controlled and modified, and all variables can be extracted from the domain. A few simulation studies have investigated the effect of dynamic conditions on wind turbine performance and wake behaviour. Leishman (2002) reviewed the challenges involved in modelling the unsteady aerodynamics of wind turbines, and used dynamic inflow theory to estimate the time constant for flow development through a rotor as

1–1.5 rotor revolutions. This study also showed a qualitative picture of the wake response to a 30° step change in yaw angle using the vortex wake model, demonstrating that it took approximately 9 rotor revolutions for the wake to fully stabilize. Ebrahimi & Sekandari (2018) simulated the effect of step changes in both wind speed and yaw angle on power production and blade loading, finding the time scale for stabilization to be 4–5 s. Finally, Andersen & Sørensen (2018) used large eddy simulations (LES) to investigate the power output response to changes in wind speed and direction. They found a lag between peaks in thrust force and peaks in power that they attributed to generator inertia and the time scale of the controller. Further, they observed that the correlations between the turbine loads and the wake position were low, highlighting the highly dynamic behaviour of the wake.

In addition to gaining insight into wake behaviours occurring during normal utility-scale wind turbine operation, improved understanding of the dynamic wake is crucial for the design of recently proposed advanced wind farm control algorithms, including thrust optimization (Goit & Meyers 2015; Munters & Meyers 2017; Shapiro *et al.* 2017; Munters & Meyers 2018*b*; Yılmaz & Meyers 2018), yaw angle modification (Gebraad, Fleming & van Wingerden 2015; Raach *et al.* 2017, 2018; Fleming *et al.* 2019; Howland *et al.* 2020) and combinations of the two (Kanev, Savenije & Engels 2018; Munters & Meyers 2018*a*). For example, Raach *et al.* (2017, 2018) used simulations to investigate the effectiveness of a lidar-based closed-loop control framework, and observed a period of inverse wake deflection in response to a 5° step change in yaw angle. Yılmaz & Meyers (2018) and Munters & Meyers (2018*b*) took advantage of changes in wake width induced by periodic blade pitch changes to induce successive vortex rings in the wake of a simulated turbine, thereby re-energizing the wake through their interactions. The wind farm optimization conducted by Munters & Meyers (2018*a*) yielded similar behaviours for thrust and analogous yaw oscillations that induced wake meandering. The current study employs LES to explore the underlying physical mechanisms behind these dynamic wake behaviours.

The current study focuses on developing the understanding of dynamic wake behaviours, both those occurring during normal utility-scale turbine operation and those that result from the implementation of adaptive control algorithms. The investigation uses LES to model changes in blade pitch, wind direction and rotor yaw occurring at different rates. The time scales and mechanisms of the wake response are then described. Section 2 describes the simulation methodology and the turbine model, § 3 presents the results and § 4 provides the discussion of the results and conclusions.

## 2. Methodology

### 2.1. Large eddy simulations

LES were performed using Nalu-Wind, a wind-focused fork of the incompressible flow solver developed by Sandia National Laboratories, Nalu (Sprague *et al.* 2020). Nalu-Wind solves the filtered Navier–Stokes equations using an unstructured finite-volume formulation that is second-order accurate in space and time. The deviatoric part of the resolved Reynolds stress tensor was represented using a Smagorinsky model with a Smagorinsky coefficient of  $C_S = 0.08$ , based on the average of the values computed by the Lagrangian scale-dependent Smagorinsky model. Martínez-Tossas *et al.* (2018) show that, when using  $C_S = 0.08$ , the turbulence characteristics (e.g. resolved Reynolds stresses) agree well with the results from the more realistic Lagrangian-scale-dependent model. The timestep of the simulations was chosen to be 0.025 s such that the Courant–Friedrichs–Lewy number based on the tip velocity remained below 1. The simulations were conducted using uniform laminar inflow with an incoming wind speed of

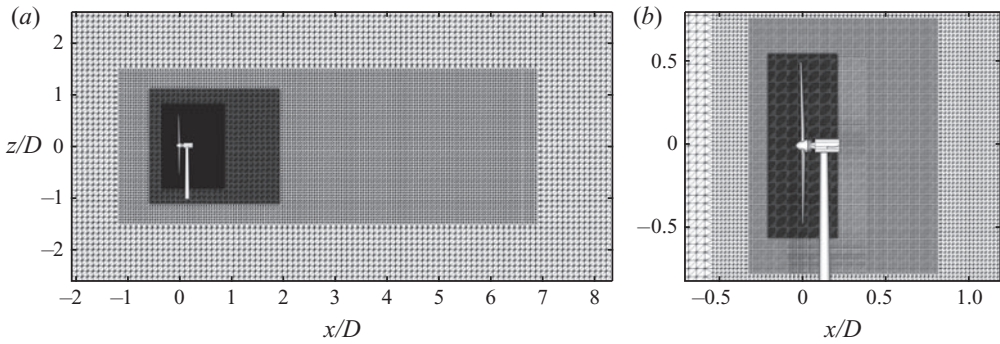


Figure 1. (a) The entire simulation domain, showing the grid refinement and the position of the turbine. (b) A smaller portion of the simulation domain highlighting the refined region around the rotor. Note that the simulated turbine is represented using actuator lines. The model included here is shown for visualization purposes. In the current study, wake behaviours are analysed at  $x/D = 0.18$  and  $x/D = 5$ .

$U_\infty = 10 \text{ m s}^{-1}$ . Uniform inflow was selected to isolate the changes in turbine operation and their effect on the near wake. Previous simulation studies have frequently used uniform laminar inflow to separate deterministic wake behaviours from the effects of turbulent stochasticity (Tsalicoglou *et al.* 2014; Troldborg *et al.* 2015; Howland *et al.* 2016; Kim *et al.* 2016; Rahimi *et al.* 2018). In addition, the near wake (the focus of the current study) is dominated by coherent structures shed from the turbine rather than random turbulence (Sørensen 2011). Previous field-scale studies using high-resolution flow visualization also exhibit the dominance of coherent structures in the near wake (Hong *et al.* 2014; Yang *et al.* 2016; Abraham, Dasari & Hong 2019; Dasari *et al.* 2019; Abraham & Hong 2020). Most importantly, the results of the recent field study investigating the dynamic wake modulation phenomena explored in the current study show that these large-scale near-wake behaviours dominate above atmospheric turbulence (Abraham & Hong 2020). The size of the simulation domain was  $1000 \text{ m} \times 500 \text{ m} \times 500 \text{ m}$  ( $10.4D \times 5.2D \times 5.2D$ , where  $D = 96 \text{ m}$  is the turbine rotor diameter), and the top, bottom and sides of the domain had symmetry boundary conditions imposed. No ground surface was modelled in order to maintain uniform inflow. The resolution farthest from the rotor was  $10 \text{ m}$ , and the mesh was refined progressively to  $0.625 \text{ m}$  directly around the rotor, producing a grid with a total of 5.6 million nodes (figure 1). This resolution is typical of or finer than similar large-scale simulations in the literature (Martínez-Tossas *et al.* 2018; Blaylock *et al.* 2019; Nielson & Bhanagar 2019).

## 2.2. Wind turbine model

The simulated wind turbine was modelled after the University of Minnesota Eolos wind turbine, described in previous studies (Hong *et al.* 2014; Chamorro *et al.* 2015; Abraham *et al.* 2019; Dasari *et al.* 2019; Abraham & Hong 2020). It is a 2.5 MW Clipper Liberty C96 three-bladed, horizontal-axis, pitch-regulated, variable speed machine with a  $96 \text{ m}$  rotor diameter ( $D$ ) and  $80 \text{ m}$  hub height ( $H_{hub}$ ). The turbine model was implemented in OpenFAST (Sprague *et al.* 2020), and the controller was tuned to match the real power curve as closely as possible. The model was then incorporated into the LES using an actuator line model, where the blades were represented by a force distribution along a line extending from the hub to each blade tip. The actuator line for each blade was discretized into 100 points, and the forces from the blades were then projected onto the

flow using a Gaussian function (Sørensen & Shen 2002; Martínez-Tossas, Churchfield & Leonardi 2014). The blade forces were calculated using lift and drag coefficient look-up tables determined by the specifications of the Eolos turbine used for the field studies. The nacelle and tower were included in the model as additional body forces, as these structural components have been shown to significantly impact the near wake (Abraham *et al.* 2019). The tower was modelled as a drag force discretized into 50 points to allow for variation in cross-sectional diameter along the height. As with the blades, the forces were projected onto the flow using a Gaussian function. The nacelle was modelled as a Gaussian drag body force with a frontal area of  $A_n = 20 \text{ m}^2$  and a drag coefficient of  $C_{D,n} = 0.5$ . The width of the Gaussian kernel was determined as a function of  $A_n$  and  $C_{D,n}$  to ensure the appropriate momentum thickness of the generated wake (Martínez-Tossas 2017):  $\epsilon_D = \sqrt{2C_{D,n}A_n/\pi}$ . Previous studies have shown that the actuator line model can successfully reproduce the flow features that dictate the large-scale near-wake behaviours investigated in the current study, i.e. near-wake flow fields and coherent structures (Lu & Porté-Agel 2011; Sanderse, van der Pijl & Koren 2011; Kang, Yang & Sotiropoulos 2014; Martínez-Tossas *et al.* 2014; Nilsson *et al.* 2015). Tip loss corrections have not been included in the current study. Sarlak *et al.* (2016) showed that the wake of a turbine modelled using actuator lines is not significantly modified by the use of tip loss corrections for low to intermediate tip speed ratios, such as those used in the current study.

### 2.3. Wake detection and fitting

The current study focuses on the near wake ( $0.18D$  downstream, selected to enable comparison with field-scale experimental results from Abraham & Hong 2020) where the turbine-induced flow modulation originates. To quantify the centreline and width of the wake, the velocity at the cross-section is fit with a two-dimensional Gaussian function,

$$u(y, z) = A * \exp\left(-\frac{(y - y_c)^2 + (z - z_c)^2}{2\sigma^2}\right) + U_\infty, \quad (2.1)$$

where  $(y_c, z_c)$  is the centre of the Gaussian,  $\sigma^2$  is the variance and  $A$  is a fitting coefficient (Bastankhah & Porté-Agel 2014; Quon, Doubrawa & Debnath 2020). The Gaussian wake model is used because it minimizes the number of fitting coefficients, whereas other wake models, particularly those designed for the near wake, require many additional fitting parameters (e.g. Keane *et al.* 2016; Ishihara & Qian 2018; Cathelain *et al.* 2020). The centre of the wake cross-section is taken to be the centre of the Gaussian fit, which is used to determine the wake deflection angle,  $\xi$  (figure 2a). Often the far-wake width is defined as the 95 % confidence interval of the Gaussian velocity deficit profile (Aitken *et al.* 2014; Doubrawa *et al.* 2017). However, the near-wake velocity deficit has steeper edges than in the far wake, so the 95 % confidence interval would severely overestimate the near-wake width. By comparing the fitted Gaussian with the near-wake velocity deficit obtained from the LES, we found that the 91 % confidence interval provides a more accurate definition of the near-wake width. The justification of this selection is described in more detail in Appendix A. The wake width is then converted to the wake expansion angle, shown in figure 2(b), using the following relation:

$$\varphi = \arctan\left(\frac{1.7\sigma - \frac{D}{2}}{0.18D}\right), \quad (2.2)$$



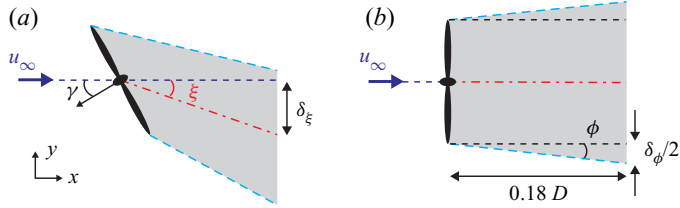


Figure 2. (a) Schematic of the turbine wake showing the definition of the yaw misalignment angle,  $\gamma$ , the wake deflection angle,  $\xi$ , and the wake deflection magnitude,  $\delta_\xi$ , from the top (positive- $z$ ) view. Coordinate axes are also shown. (b) Schematic of the turbine wake showing the definition of the wake expansion angle,  $\phi$ , and the wake expansion magnitude,  $\delta_\phi$ . The incoming wind is indicated by  $u_\infty$  and the measurement plane is located  $0.18D$  downstream of the rotor.

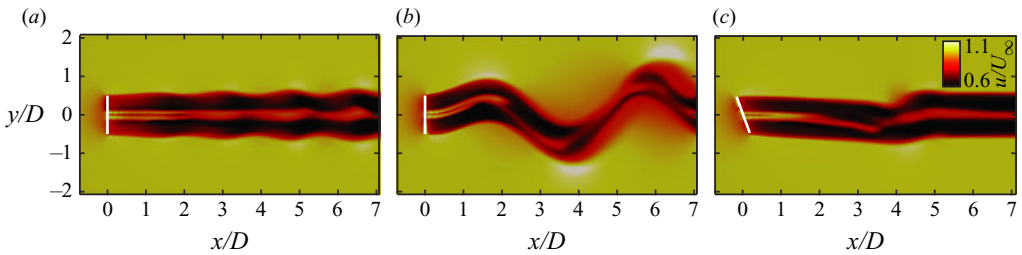


Figure 3. Sample timesteps of the wake streamwise velocity at hub height from the top (positive- $z$ ) view during the simulations modelling changes in (a) blade pitch, (b) wind direction and (c) rotor yaw. White lines indicate the position and orientation of the rotor.

where the factor of 1.7 corresponds to the 91% confidence interval and  $0.18D$  is the downstream distance of the measurement plane.

### 3. Results

We now present results for the turbine wake response to three types of operational changes: (i) variations in expansion caused by blade pitch, (ii) redirection from wind direction changes and (iii) wake deflection due to rotor yaw. Sample images of the wake velocity during each of these scenarios are shown in [figure 3](#).

#### 3.1. Blade pitch

First, the effect of changes in blade pitch ( $\beta$ ) on the near wake is investigated. Most utility-scale wind turbine controllers increase the pitch of the blades when the incoming wind is above the rated wind speed to reduce the angle of attack of the airfoils and decrease the thrust force of the rotor as a way to regulate the structural loading. To examine the effect of this process on the wake, a time series of pitch changes at different rates, similar to those observed for a utility-scale turbine, is implemented in the OpenFAST turbine controller. The pitch first increases at each rate for 10 s, then decreases at the same rate for 10 s, as shown in [figure 4\(a\)](#) along with the resulting changes in wake expansion angle. The wake expansion varies inversely with changes in blade pitch due to the aforementioned reduction in thrust caused by lowering the angle of attack. The same relationship is observed in the field experiment from Abraham & Hong (2020). Interestingly, the correlation is not linear, rather some hysteresis occurs in the wake response. This hysteresis can also be observed in the field data, as evidenced by the fact that there are multiple different values of wake

expansion for a given blade pitch angle during a sample sequence of 800 s (figure 4b). The same characteristic looping behaviour is observed in the relationship between blade pitch and wake expansion from the field data as that observed in the simulation results, although the loops are not as regular as those from the simulations due to the many different factors influencing wake behaviour in the field. Because individual variables are difficult to isolate in the field, the cause of this observation could not be confirmed with certainty. In the simulation, the cause of such hysteretic response becomes clear when comparing the wake expansion with the tip speed ratio,  $\lambda = \omega D/2u_\infty$  where  $\omega$  is the angular velocity of the rotor, which changes in response to changes in blade pitch. Figure 4(c) shows the strong correlation between  $\lambda$  and  $\varphi$ , which suggests that the wake is actually responding to the change in rotor speed rather than the change in blade pitch itself. A similar trend is observed in the experimental data, conditionally sampled for periods where the wind is above the rated speed and the blade pitch is changing, although with a wider range of  $\lambda$  due to larger changes in  $u_\infty$  and much more variability due to the dynamic atmospheric wind speed and direction (figure 4d). Note that the results of the simulation are repeatable because of the use of uniform inflow, while the experimental data are not deterministic due to the multitude of uncontrolled stochastic variables in the field. Still, the trends observed in the experimental data are robust, as described in more detail in Abraham & Hong (2020). The relationship between  $\lambda$  and  $\varphi$  is stronger than that between  $\beta$  and  $\varphi$  because the reduction in lift force on the blades due to the increase in pitch causes the rotor to slow down, which causes the wake expansion to decrease. This reduction in rotor speed lags slightly behind the increase in blade pitch due to the inertia of the flow. Schepers (2007) described the effect of flow inertia to explain the observed lag in turbine response to a step increase in blade pitch. He attributed the lag to the time it takes to accelerate the flow after a decrease in axial induction. Ebrahimi & Sekandari (2018) observed a similar delay in thrust change after a step change in wind speed. A linear regression fit is applied to the relationship between  $\lambda$  and  $\varphi$  from the experiment, revealing a shallower slope than that of the simulation data (figure 4d). This difference in slope is attributed to the smoothing applied to the experimental wake boundary data to account for turbulent fluctuations, which tends to obscure more extreme values. The experimental data also include many additional sources of uncertainty, including concurrent changes in multiple parameters that may interact, and the measurement of incoming velocity at the turbine nacelle, which is within the induction zone of the turbine (Li *et al.* 2020). However, it is remarkable that the overall trends from the experiment and simulations still match well in spite of these discrepancies, indicating that the large-scale wake behaviours dominate over the effects of smaller-scale turbulence.

To quantify the time scale of the wake expansion response, changes in blade pitch angle at different rates ( $\beta'$ ) are simulated. Blade pitch is varied from  $1^\circ$  (the default pitch angle of the Eolos turbine when operating below the rated wind speed) to  $7^\circ$  at several different rates between  $0.1^\circ$  and  $4^\circ \text{ s}^{-1}$ , and from  $7^\circ$  to  $1^\circ$  at rates between  $-0.1^\circ$  and  $-4^\circ \text{ s}^{-1}$ . Such step changes are used to replicate the blade pitching behaviour of an operational turbine, which cannot change the blade pitch instantaneously. Figure 5(a) shows a sample time sequence of the change in wake expansion in response to an increase of blade pitch at a constant rate. The wake begins expanding when the pitch begins changing, then asymptotically approaches its maximum change in expansion,  $\varphi_{max}$ . To facilitate physical interpretation of the results, values are normalized using the time scale  $\tau_0 = D/U_\infty$  and angles are converted from degrees to radians. Figure 5(b) shows that  $\varphi_{max}$  is independent of pitch rate, and that with a  $6^\circ$  (0.10 rad) change in blade pitch, the wake expansion always changes by  $\sim 16^\circ$  (0.28 rad). On the other hand, the duration of the wake expansion change is strongly dependent on pitch rate. To quantify this effect, a

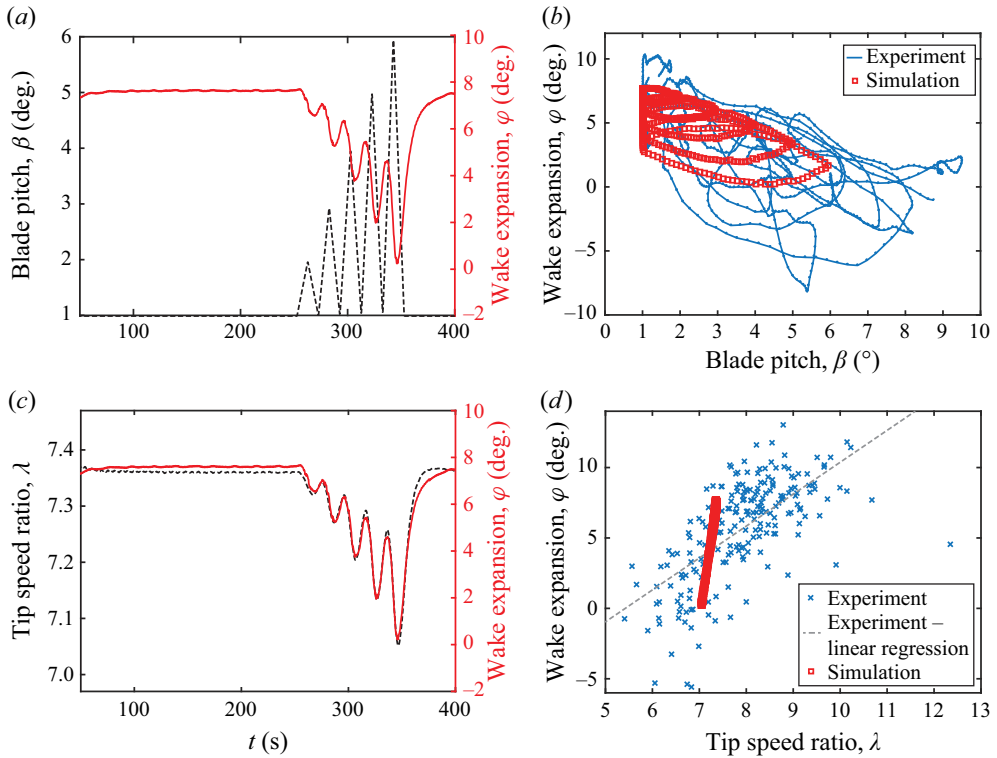


Figure 4. (a) Prescribed changes in blade pitch (dashed black line) and the resulting changes in wake expansion (solid red line). (b) Instantaneous wake expansion angle vs blade pitch from the simulation (red squares) and a sample sequence of 800 s from the experiment from Abraham & Hong (2020) (blue line). (c) Time series of tip speed ratio changes (dashed black line) caused by changes in blade pitch and resulting wake expansion (solid red line). (d) Instantaneous wake expansion angle vs tip speed ratio from the simulation (red squares) and from periods of the experimental dataset from Abraham & Hong (2020) where the wind is above the rated speed and the blade pitch is changing (blue crosses). A linear regression fit to the experimental data is included to facilitate comparison with the simulation data.

wake expansion time scale ( $\tau_\varphi$ ) is defined as in exponential decay, i.e. as the time for the change in wake expansion to reach  $\varphi_\tau = (1 - 1/e)\varphi_{max}$ . Berger & Kühn (2018) similarly observed exponential decay of wake velocity in response to a step change in rotor thrust. Figure 5(c) shows that  $\tau_\varphi$  is significantly higher at slow pitch rates ( $\tau_\varphi/\tau_0 \sim 5$ ) compared with fast pitch rates ( $\tau_\varphi/\tau_0 \sim 1$ ). Figure 5(d) further elucidates this trend by scaling the wake expansion time scale by the pitch manoeuvre duration ( $t_{end} - t_{start}$ ). This scaling reveals that  $\tau_\varphi/(t_{end} - t_{start})$  is linearly dependent on  $\beta'\tau_0$ , highlighting that as the pitch rate increases, the lag in wake response increases, indicating an increased deviation from quasi-steady behaviour. Some asymmetry is observed between an increasing and decreasing blade pitch, where the time scales tend to be larger for increasing pitch. This trend is consistent with the explanation provided by Schepers (2007) for the difference between an upward and downward pitching step: for an increase in blade pitch, the axial induction is initially large, leading to lower wake velocity and advection time than for a decrease in blade pitch, where the wake velocity is initially higher. To provide a sense of the typical blade pitch rate of a utility-scale wind turbine operating in the field, the mean pitch rate implemented by the Eolos turbine during the experiment described in Abraham & Hong (2020) was  $0.4^\circ \text{ s}^{-1}$  ( $\beta'\tau_0 = 0.04$ ), with a maximum and minimum rate of



## Dynamic near-wake modulation

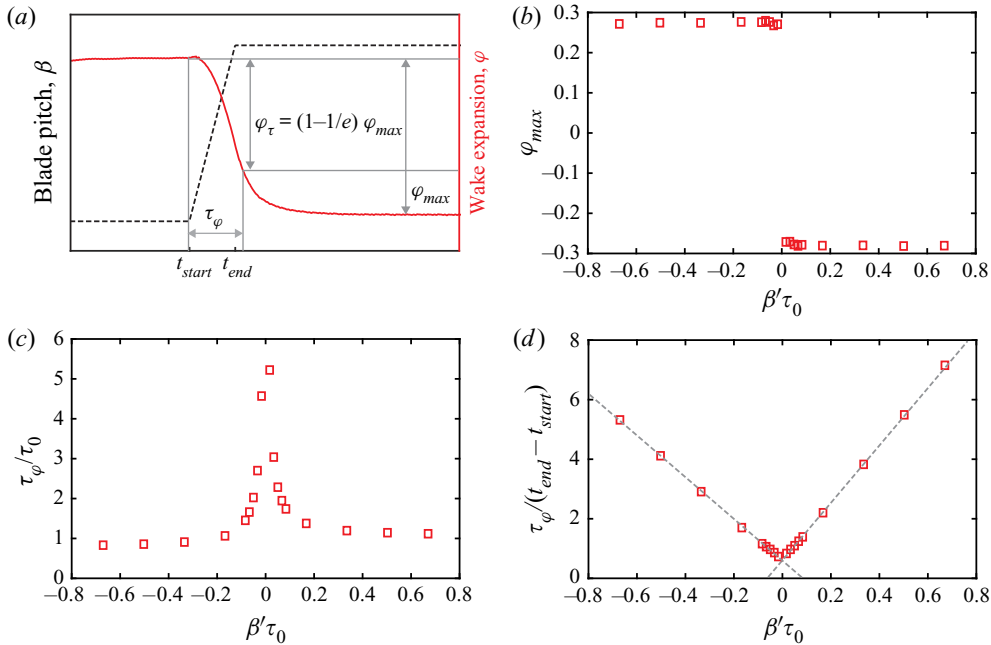


Figure 5. (a) Sample change in blade pitch angle at a constant rate (dashed black line) and the resulting wake expansion response (solid red line). The wake expansion time scale,  $\tau_\varphi$ , and maximum change in wake expansion,  $\varphi_{max}$ , are defined in grey. (b) Relationship between normalized blade pitch rate and maximum wake expansion change. (c) Relationship between normalized pitch rate and normalized wake expansion time scale. (d) Relationship between normalized pitch rate and wake expansion time scale normalized by the duration of the blade pitch manoeuvre. The grey dashed lines show linear regression fits to the data for  $\beta'\tau_0 < 0$  and  $\beta'\tau_0 > 0$ .

$2.4^\circ \text{ s}^{-1}$  ( $\beta'\tau_0 = 0.26$ ) and  $0.2^\circ \text{ s}^{-1}$  ( $\beta'\tau_0 = 0.02$ ), respectively. These findings have important implications for the design of advanced wind farm control algorithms that use blade pitch to regulate turbine axial induction (e.g. Yılmaz & Meyers 2018), which cannot expect the wake to react immediately to changes in blade pitch.

### 3.2. Wind direction

In Abraham & Hong (2020), a clear correlation was observed between instantaneous incoming wind direction and spanwise wake deflection, although it was in the opposite direction of that described in several previous studies conducted under steady conditions (e.g. Jiménez, Crespo & Migoya 2010; Bastankhah & Porté-Agel 2016; Shapiro, Gayme & Meneveau 2018). Here, the mechanism behind such conflicting results is investigated in more detail. First, the spanwise component of the wind is varied sinusoidally with a 20 s period while the rotor direction is held constant, providing the turbine with dynamic yaw misalignment ( $\gamma$ ) similar to the conditions experienced in the field due to the stochasticity of the atmospheric flow (figure 6(a) and supplementary movie 1 available at <https://doi.org/10.1017/jfm.2021.737>). The resulting instantaneous wake deflection is shown to follow the trend observed in the field (figure 6(b)). Note that, as in the wake expansion case, the slope of the wake deflection response to yaw misalignment angle is shallower for the experimental data than the simulation data. Once again this discrepancy is attributed to the turbulence and uncertainties of the experimental data. Additionally, as will be described

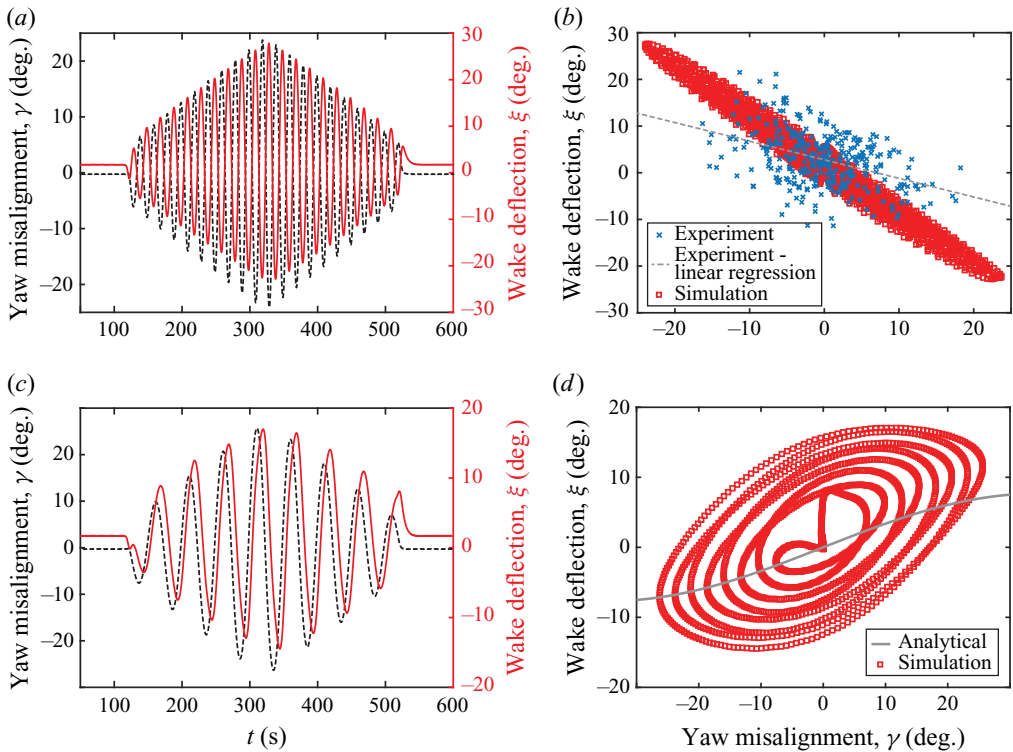


Figure 6. (a) Prescribed changes in wind direction with a 20 s period (dashed black line) and the resulting changes in spanwise wake deflection (solid red line). (b) Instantaneous wake deflection angle vs wind direction for the experiment from Abraham & Hong (2020) (blue crosses) and the simulation (red squares). A linear regression fit to the experimental data is included to facilitate comparison with the simulation data. (c) Prescribed changes in wind direction with a 50 s period (dashed black line) and the resulting changes in spanwise wake deflection (solid red line). (d) Analytical solution for the steady wake deflection angle from Jiménez *et al.* (2010) (grey line) compared with the instantaneous wake deflection vs wind direction from the simulation (red squares).

in more detail in the following sentences, the wake deflection response is dependent on the time scale of wind direction changes. Atmospheric wind experienced by turbines in the field fluctuates across a range of time scales, whereas the simulated wind direction changes with a constant period.

The period of wind direction changes is increased to 50 s, and a different trend is observed compared with the 20 s period (figure 6(c) and supplementary movie 2). With these slower wind direction changes, the wake deflection more closely follows the analytical relationship defined in Jiménez *et al.* (2010) for steady yaw error, although with some hysteresis (figure 6(d)). This hysteresis is caused by a lag in the wake response to changes in yaw error. These results suggest the existence of a characteristic wake response time scale during which the wake deflection transitions from the transient opposite deflection response to the steady analytical response. The dependencies of this time scale will be explored in the following section using step changes in  $\gamma$  at different rates. Note that the wake deflection response is asymmetrical, with a larger deflection on the positive side than the negative side, likely caused by wake rotation (Bastankhah & Porté-Agel 2016). The turbine modelled in the current study rotates in the counterclockwise direction.

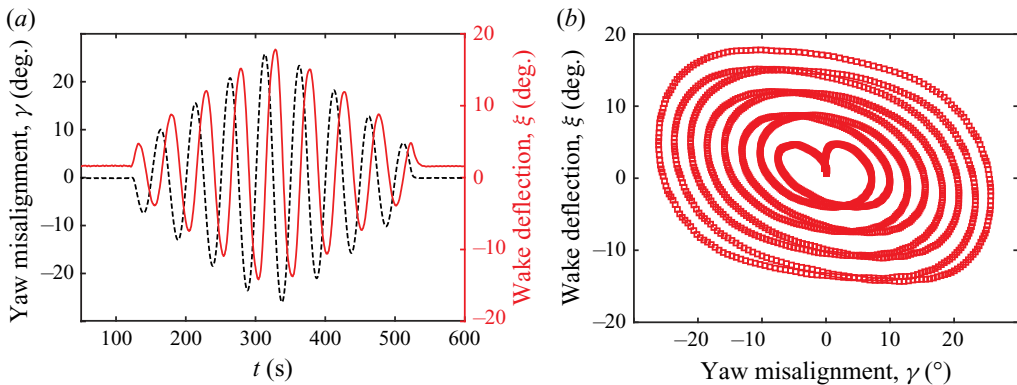


Figure 7. (a) Prescribed sinusoidal changes in rotor yaw angle with a period of 50 s, matching the changes in wind direction shown in figure 6(c), (dashed black line) and the resulting changes in spanwise wake deflection (solid red line). (b) Instantaneous wake deflection angle vs yaw misalignment angle.

For a clockwise rotating turbine, the negative deflection may be larger than the positive deflection.

### 3.3. Rotor yaw

Using changing wind direction to investigate yaw error includes the coupling of two effects: yaw misalignment induced wake deflection and changes in the direction of wake advection by the surrounding flow. Although this coupling is representative of the wake response in the field under stochastic atmospheric flow, these effects must be separated to gain further insight into the flow modulation caused by the turbine. Therefore, the same yaw misalignment sequence as that shown in figure 6(c) is implemented by changing the rotor yaw angle while keeping the wind direction constant (figure 7a). In this scenario, the lag in wake response is longer than previously observed for the changing wind direction scenario with the same period (50 s). This discrepancy is attributed to the fact that, when the wind direction changes, the surrounding flow advects the wake in the spanwise direction, pushing it towards the steady yaw response. Additionally, the streamwise velocity must be kept constant to ensure constant mass flow through the simulation domain, so spanwise velocity is varied in the wind direction simulation. This increase in spanwise velocity causes the wind velocity magnitude to increase. Jiménez *et al.* (2010) showed that the spanwise force exerted by the turbine on the wake is dependent on the square of the inflow velocity magnitude under steady conditions. Because the velocity magnitude is larger in the wind direction simulation during periods of yaw misalignment than in the rotor yaw simulation, the force pushing the wake towards steady-state deflection is stronger in the wind direction simulation. Therefore, the dynamic wake deflection approaches steady-state behaviour more quickly than in the rotor yaw simulation. Although the time scales of the wake response in the two cases are different, the general trends observed are consistent, including the magnitude of the inverse wake deflection. To isolate the effect of dynamic wake modulation from that of wake advection by ambient wind, and to facilitate the extension of these findings to wake control applications, the following analysis uses rotor yaw angle changes to investigate dynamic spanwise wake deflection in more detail.

To quantify the inverse wake deflection magnitude and time scale more precisely, changes in rotor direction with constant yaw rates are investigated. The yaw angle is

varied from  $0^\circ$  to  $20^\circ$  at several different rates ( $\gamma'$ ) between  $0.1^\circ$  and  $4^\circ \text{ s}^{-1}$ , and from  $20^\circ$  to  $0^\circ$  at rates between  $-0.1^\circ$  and  $-4^\circ \text{ s}^{-1}$ . As with blade pitch, step changes are used to replicate the yawing behaviour of an operational turbine, which cannot change the rotor angle instantaneously. Figure 8(a) shows a sample time sequence of wake deflection with a constant yaw rate. Under this condition, the wake first deflects in the direction opposite of the yaw change, then deflects in the same direction as the yaw change for the remaining duration of the rotor motion, consistent with the results of previous studies (Leishman 2002; Raach *et al.* 2017, 2018). Results are once again normalized by  $\tau_0$  and angles are converted to radians. Figure 8(b) quantifies the magnitude of the maximum inverse wake deflection,  $\xi_{max}$ , showing a clear dependence on yaw rate. This deflection is not insignificant; at the largest yaw rates, it reaches 75 % of the rotor misalignment angle. However, the duration of this deflection decreases with increasing yaw rate magnitude. The inverse wake deflection time scale ( $\tau_\xi$ ) is defined in the same way as the wake expansion time scale, i.e. as the time for the wake deflection to reach  $\xi_\tau = (1 - 1/e)\xi_{max}$ . The value of  $\tau_\xi/\tau_0$  generally increases with decreasing yaw rate magnitude, although the peak occurs at a normalized yaw rate  $\gamma'\tau_0 > 0$ . This asymmetry is also likely caused by wake rotation, and may be reversed in the case of a clockwise rotating turbine. Note that  $\tau_\xi$  ranges from  $0.23\tau_0$  to  $0.54\tau_0$  for the yaw rates investigated here, and a yaw rate of  $0.5^\circ \text{ s}^{-1}$  ( $\gamma'\tau_0 = 0.08$ , typical of e.g. the Eolos turbine) results in  $\tau_\xi = 0.53\tau_0$  when the yaw is increasing and  $\tau_\xi = 0.35\tau_0$  when it is decreasing. These values show that the wake takes a significant amount of time to stabilize in response to changes in yaw angle, which has important implications for the design of yaw-based wind farm optimization algorithms. This crucial point will be discussed further in § 4. When an inverse wake deflection rate is defined as  $\xi_{max}\tau_0/\tau_\xi$ , another interesting trend is revealed. This quantity is linearly dependent on  $\gamma'\tau_0$ , with a nearly one-to-one relationship (the linear regression slope is  $-1.2$  and intersects the ordinate axis at  $\xi_{max}\tau_0/\tau_\xi = 0.01$ ). This relationship clearly demonstrates the tradeoff between inverse wake deflection magnitude and duration under different yaw rates. The physical explanation for this relationship will be further elucidated in § 3.4. Note that these yaw changes are implemented under turbine operational conditions that are otherwise optimized by the turbine controller (i.e. blade pitch is set to the value determined to maximize power based on the wind speed, as it would be for an operational utility-scale turbine). The effect of yaw changes under sub-optimal operating conditions has not been investigated. However, we expect a reduction in thrust coefficient to increase the inverse wake deflection time scale, as Jiménez *et al.* (2010) showed that the steady wake deflection response weakens with reduced thrust coefficient.

### 3.4. Vorticity analysis during dynamic yaw misalignment

Further insight into the mechanism behind these wake behaviours can be gained by looking at the vorticity in the wake. Previous studies have shown that streamwise vorticity plays an important role in the behaviour of the yawed wake, leading to wake deflection and the curled wake shape that develops downstream (Bastankhah & Porté-Agel 2016; Howland *et al.* 2016; Shapiro *et al.* 2018; Martínez-Tossas *et al.* 2019; Zong & Porté-Agel 2020). When streamwise vortices with opposing signs form on the top and bottom halves of the wake, they induce a spanwise velocity. Based on these studies, the following analysis focuses on the streamwise component of the vorticity vector. In the current study, after the turbine yaws, negative streamwise vorticity ( $\omega_x$ ) is observed in the top half of the wake and positive streamwise vorticity is observed in the bottom half (see supplementary movie 3 – stills in Appendix B), consistent with the steady yawed wake behaviour

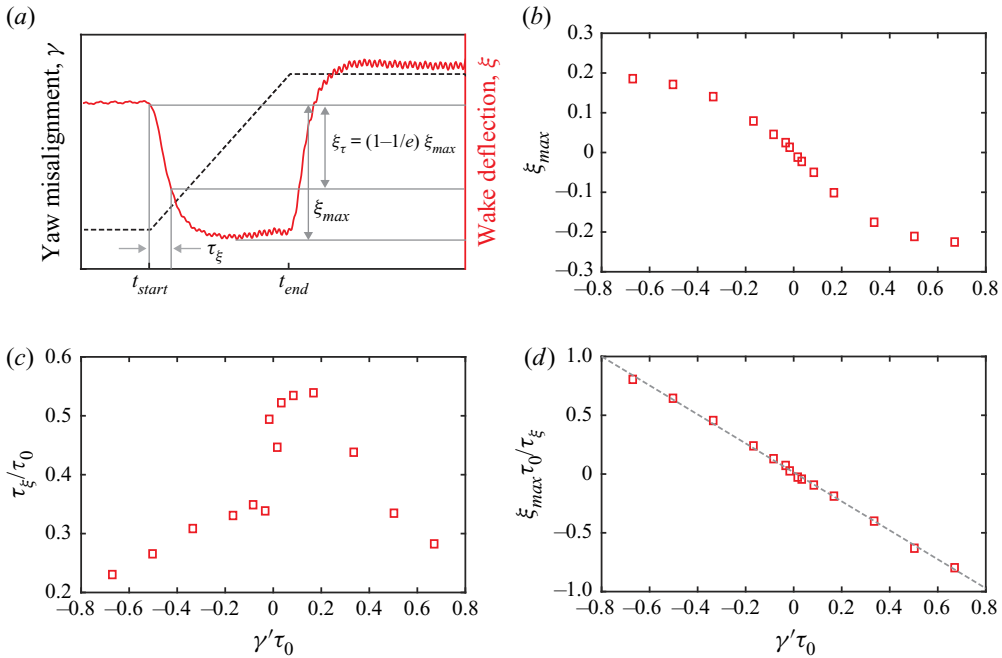


Figure 8. (a) Sample change in yaw angle at a constant rate (dashed black line) and the resulting wake deflection response (solid red line). The wake deflection time scale,  $\tau_\xi$ , and maximum inverse wake deflection,  $\xi_{max}$ , are defined in grey. (b) Relationship between normalized yaw rate and maximum inverse wake deflection. (c) Relationship between normalized yaw rate and normalized inverse wake deflection time scale. (d) Relationship between yaw rate and  $\xi_{max}\tau_0/\tau_\xi$ . The dashed grey line shows the linear regression fit to the data.

described in Zong & Porté-Agel (2020). More interestingly, during the positive yaw manoeuvre, a short period of increased vorticity is observed in the top-left quadrant (I) of the wake and a period of decreased vorticity is observed in the bottom-right quadrant (IV) of the wake (figure 9(a) and supplementary movie 3 – stills in Appendix B). The maximum streamwise vorticity in sections of each of the four quadrants of the wake located at  $z = \pm 0.3D$ ,  $0.2D < y < 0.5D$  or  $-0.5D < y < -0.2D$ , and  $0.5D < x < 0.6D$  compared with the theoretical vorticity trend excluding the transient effect is plotted over time in figure 9(b), demonstrating the observed vorticity changes. Without the transient effect, the streamwise vorticity would be expected to transition smoothly from its initial value to the reduced value in the top half of the wake (quadrants I and II) and the increased value in the bottom half (quadrants III and IV). However, the transient effect shifts the vorticity in the opposite directions in quadrants I and IV. This transient vorticity shift can be explained by the angle of the vortices shed from the turbine blade tips during the yaw manoeuvre, where one side of the rotor is moving upstream and the other is moving downstream. As explained in Zong & Porté-Agel (2020), the angle of the blade tip vortex trajectory determines the streamwise component of the vorticity, which dictates the deflection direction of the wake. When the rotor is turning, the side moving upstream (the left side in figure 9) is experiencing a larger streamwise velocity relative to the flow, increasing the streamwise component of the vorticity on that side (supplementary movie 3). On the side moving downstream, the relative velocity is reduced, along with the streamwise vorticity component. As the yaw angle increases, the steady yaw angle effect described in Zong & Porté-Agel (2020) dominates over the transient effect, leading to



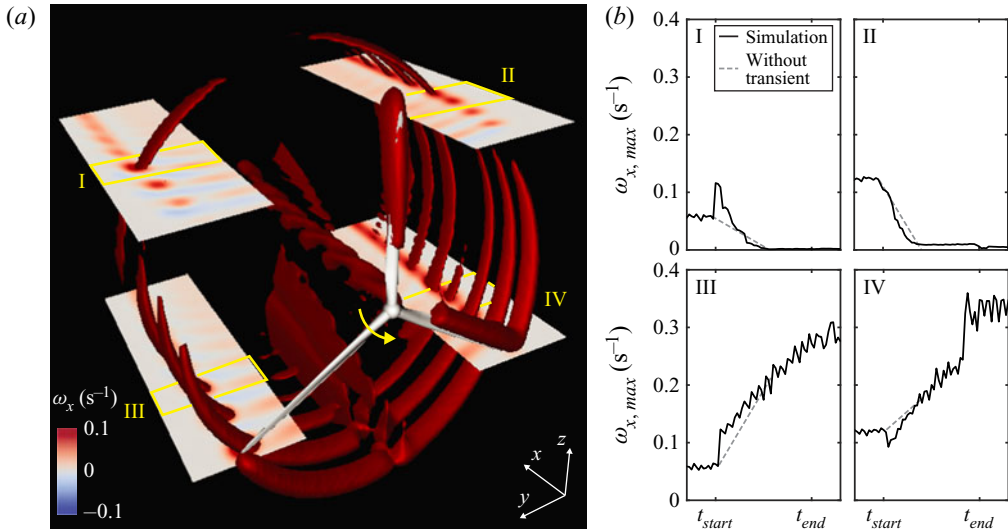


Figure 9. (a) Isocontour of streamwise vorticity with cut planes in each quadrant. The isocontour value is  $\omega_x = 0.1 \text{ s}^{-1}$ . Note that the turbine tower and nacelle are included in the simulated turbine model, although only the rotor is shown here for clarity. The yellow arrow near the hub indicates the direction of the yaw. The yellow boxes labelled with roman numerals indicate the regions plotted in (b), which shows the maximum streamwise vorticity component within each region over time compared with the theoretical vorticity trend excluding the transient effect. The plotted regions are located at  $z = \pm 0.3D$ ,  $0.2D < y < 0.5D$  or  $-0.5D < y < -0.2D$ , and  $0.5D < x < 0.6D$ .

the expected steady-state vorticity distribution. In quadrants I and IV the transient effect is in the opposite direction of the steady effect, while the two effects are in the same direction in quadrants II and III. Therefore quadrants I and IV contribute to the opposite wake deflection while II and III do not. When the yawing manoeuvre ends and the two sides of the rotor experience the same relative streamwise velocity, the transient effect disappears altogether.

Although the value of the streamwise vorticity remains positive in all four quadrants during the transient wake response, the difference in vorticity between the top and bottom of the wake is enough to induce a positive spanwise velocity and corresponding inverse wake deflection. Both the spatially averaged spanwise velocity ( $v_{avg}$ , figure 10a) and the maximum spanwise velocity ( $v_{max}$ , figure 10b) within the rotor area at a  $y$ - $z$  plane located  $0.5D$  downstream show a peak just after the yawing manoeuvre begins, indicating a transient inverse wake deflection response. Subsequently, the spanwise velocity decreases due to the steady yaw response. As the streamwise vorticity is responsible for the negative spanwise velocity and wake deflection during the steady yaw response (Zong & Porté-Agel 2020), so our results indicate the opposite streamwise vorticity shift shown in figure 9 causes the positive spanwise velocity and wake deflection that are characteristic of the transient inverse wake deflection response. Note that the magnitude of the transient spanwise velocity peak increases with downstream distance, as does the inverse vorticity shift. The values at  $x = 0.5D$  are presented to highlight the velocity and vorticity trends that develop directly after the flow passes through the rotor.

The magnitude of the transient vorticity shift is directly dependent on yaw rate, as shown in figure 11. This linear relationship sheds light on the clear dependence of the inverse wake deflection rate,  $\xi_{max}\tau_0/\tau_\xi$ , on yaw rate shown in figure 8. The inverse wake deflection time scale  $\tau_\xi$  depends on yaw rate because higher yaw rates execute a yawing manoeuvre

## Dynamic near-wake modulation

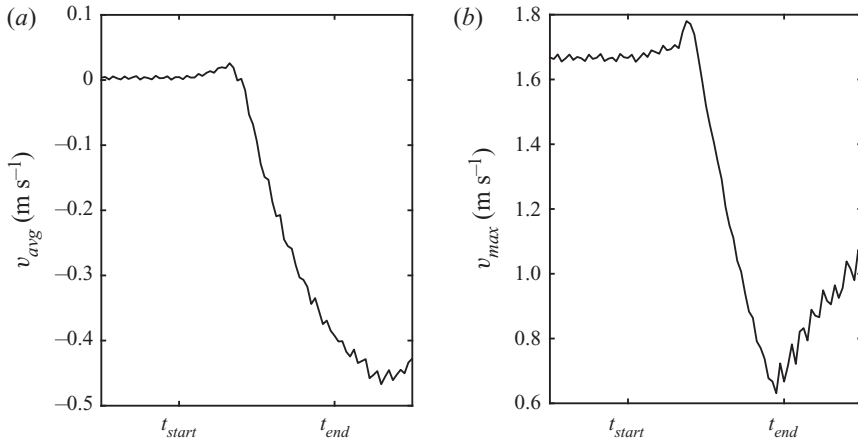


Figure 10. (a) Spatially averaged and (b), maximum spanwise velocity ( $v$ ) over the rotor area in the  $y$ - $z$  plane  $0.5D$  downstream of the turbine during a yawing manoeuvre.

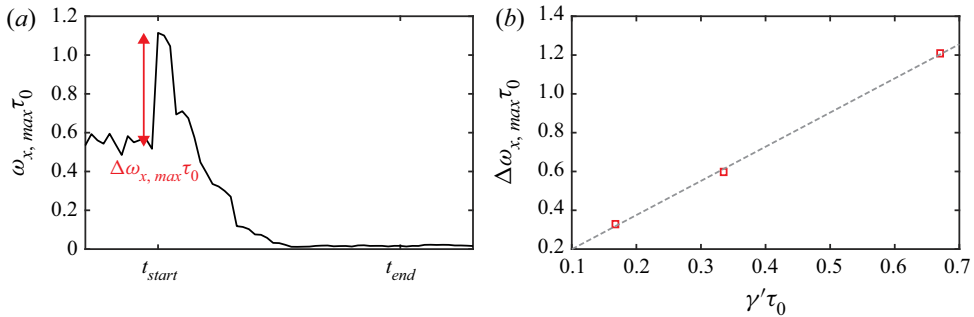


Figure 11. Transient vorticity shift dependence on yaw rate, including (a) the definition of the normalized vorticity shift magnitude,  $\Delta\omega_{x,max}\tau_0$ , and (b) a plot of  $\Delta\omega_{x,max}\tau_0$  vs normalized yaw rate,  $\gamma'\tau_0$ . The dashed grey trendline shows the linear regression of the data in (b). Note that fewer yaw rates are shown here than in [figure 8](#) because higher temporal frequency outputs were required from the simulations to fully resolve the vorticity peak.

of the same magnitude more quickly, but the magnitude of the inverse wake deflection  $\xi_{max}$  is also affected by yaw rate because the strength of the vorticity generated at the rotor is determined by yaw rate. This trend is in contrast to that observed for blade pitch in [figure 5](#), because the magnitude of the maximum wake expansion change  $\varphi_{max}$  is unaffected by pitch rate. The transient wake expansion response to dynamic blade pitch changes is simply a slow approach to steady-state behaviour, whereas the wake deflection response to yaw changes occurs in the opposite direction of the steady-state behaviour.

The vertical component of vorticity also changes when the rotor is yawing, with the left side producing stronger vorticity than the right side, as with the streamwise component. This imbalance in vertical vorticity may also induce a positive spanwise velocity, contributing to the observed spanwise wake deflection, although it would likely be much smaller than that generated by the streamwise component of vorticity (Lewke, Le Dizès & Williamson 2016). Previous field-scale flow visualization studies show strong, clear tip vortices within the near wake of utility-scale wind turbines (Hong *et al.* 2014; Yang *et al.* 2016; Abraham *et al.* 2019; Dasari *et al.* 2019; Abraham & Hong 2020), so turbulence and shear are not expected to significantly inhibit the aforementioned

mechanism in the field. Indeed, the same inverse wake deflection described above was observed in the field data from Abraham & Hong (2020). That being said, figure 6 shows that the magnitude of the resulting wake deflection is damped by the increased mixing caused by these atmospheric effects.

Based on the analysis of the spanwise wake deflection, one might expect a similar trend in the vertical direction due to the differences in streamwise vorticity between the left and right sides of the wake. However, no significant transient vertical wake shift is observed during the yawing manoeuvre. This lack of vertical deflection is attributed to the large number of competing effects acting on the wake in the vertical direction. First, the interaction between wake rotation and the ground has been shown to substantially influence the vertical displacement of the wake centre during yaw (Bastankhah & Porté-Agel 2016). Furthermore, Kleusberg, Schlatter & Henningson (2020) showed that the angle of attack of the blades varies between the top and bottom of the rotor when the turbine is yawed, introducing an additional source of vertical asymmetry. Finally, differences in spanwise vorticity between the top and bottom of the rotor may contribute to changes in the vertical velocity field of the wake. The combination of these effects, along with the spanwise asymmetry in streamwise vorticity observed in figure 9, balance such that no significant transient vertical wake deflection is observed.

### 3.5. Downstream propagation

In order to apply the findings of the current study to the development of control strategies, the extension of these near-wake time scales to the far wake must be investigated. Qualitatively, it is clear that these dynamic wake modulation behaviours persist downstream. In the wake expansion case, an interesting phenomenon is observed as the wake advects downstream after a change in blade pitch. When the blade pitch increases, the velocity deficit decreases due to a reduction in lift on the blades, so the upstream part of the wake moves faster than the downstream part, leading to a bulge at the point of blade pitch change (figure 12a). When the blade pitch decreases, the opposite occurs and the wake pinches off (figure 12b). These same wake width changes have been exploited to enhance wake mixing in previous studies investigating dynamic induction control of wind farms (Munters & Meyers 2018a,b; Yilmaz & Meyers 2018; Frederik *et al.* 2020). When the rotor yaw changes, the disturbance due to inverse wake deflection is also observed to persist and strengthen as it moves into the far wake (figure 12c,d).

Quantitative investigation of dynamic wake modulation propagation downstream is also provided, although we note the limitations of this analysis. In the far wake, coherent structures have broken down and atmospheric turbulence is much more dominant than in the near wake (Zhan, Letizia & Iungo 2020). Turbulence is not included in the current study to facilitate the observation of deterministic near-wake modulation, as described in § 2.1. The downside of this simplification is that it limits the ability to draw realistic conclusions about far-wake propagation. Therefore, the following analysis adds primarily theoretical value for idealized conditions. First, the wake expansion response to changes in blade pitch is calculated at  $5D$  downstream of the rotor and compared with that observed at  $0.18D$ . The  $5D$  distance is chosen because it is well within the far wake (typically considered to begin at  $2 - 4D$  downstream, Göçmen *et al.* 2016), but still within the higher-resolution portion of the simulation mesh (figure 1a). Furthermore, Santhanagopalan, Rotea & Iungo (2018) found  $5D$  to be the optimal spacing between the first and second row of turbines under most conditions. To facilitate this far-wake comparison,  $\delta\varphi_{max}/D$ , where  $\delta\varphi$  is the deviation of the wake diameter from  $D$ , is used to represent the amount of wake expansion rather than  $\varphi_{max}$ . This metric is selected because

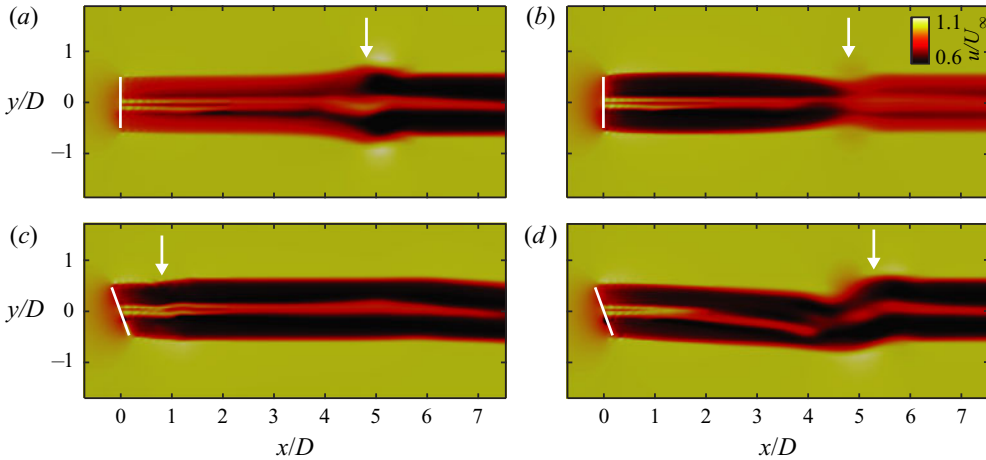


Figure 12. Sample timesteps of the wake streamwise velocity at hub height from the top (positive- $z$ ) view 50 s after (a) an increase and (b) a decrease in blade pitch. The resulting changes in wake expansion have advected several times the rotor diameter downstream, indicated by the white arrows. Sample timesteps of the same quantity (c) 10 s and (d) 60 s after a change in rotor yaw. The position and orientation of the turbine rotor is marked by white lines and the location of the resulting inverse wake deflection at each timestep is indicated by white arrows.

its calculation does not depend on the downstream distance, unlike  $\varphi$  (see figure 2), and therefore demonstrates how the magnitude of a perturbation changes as it propagates downstream. As shown in figure 13(a), the maximum wake expansion does not change significantly between  $0.18D$  and  $5D$ . The maximum inverse wake deflection, on the other hand, decreases in magnitude as the perturbation is advected downstream (figure 13b). The wake deflection metric used,  $\delta_{\xi, \max}/D$ , is defined using the spanwise deviation of the wake centre (figure 2), with the wake centre location determined by a Gaussian fit to the streamwise wake velocity profile as described in § 2.3. Although figure 13(b) shows a significant reduction in inverse wake deflection at  $5D$ , figure 12(d) clearly shows qualitatively that it does, in fact, persist into the far wake. This discrepancy between the qualitative and quantitative observations is attributed to the significant distortion of the wake cross-section in the far wake during periods of yaw misalignment (Bastankhah & Porté-Agel 2016; Howland *et al.* 2016; Shapiro *et al.* 2018; Martínez-Tossas *et al.* 2019; Zong & Porté-Agel 2020).

Wake expansion and deflection time scales are also calculated at  $5D$  downstream and compared with those at  $0.18D$ , after accounting for the time it takes for the wake to be advected this distance by the ambient air. Figure 13(c) shows that the wake expansion time scale increases significantly as the perturbation caused by changing blade pitch propagates downstream. This increase in time scale is caused by the phenomenon depicted in figures 12(a) and 12(b). When the blade pitch increases, the maximum reduction in wake diameter occurs after the bulge caused by the velocity differences in the upwind and downwind portions of the wake passes. This bulge increases the time between the start of the pitch change manoeuvre and  $\delta_{\varphi, \tau}$ , the point used to determine  $\tau_{\varphi}$  (figure 14). When the blade pitch decreases, the narrowing of the wake causes the same lag in wake expansion time scale. On the other hand, the deflection time scale at  $5D$  downstream does not change significantly from that at  $0.18D$  downstream (figure 13d). Some increased scatter is observed, especially at the lower yaw rates, attributed to the relatively small inverse wake deflection at these yaw rates and the significant wake distortion discussed

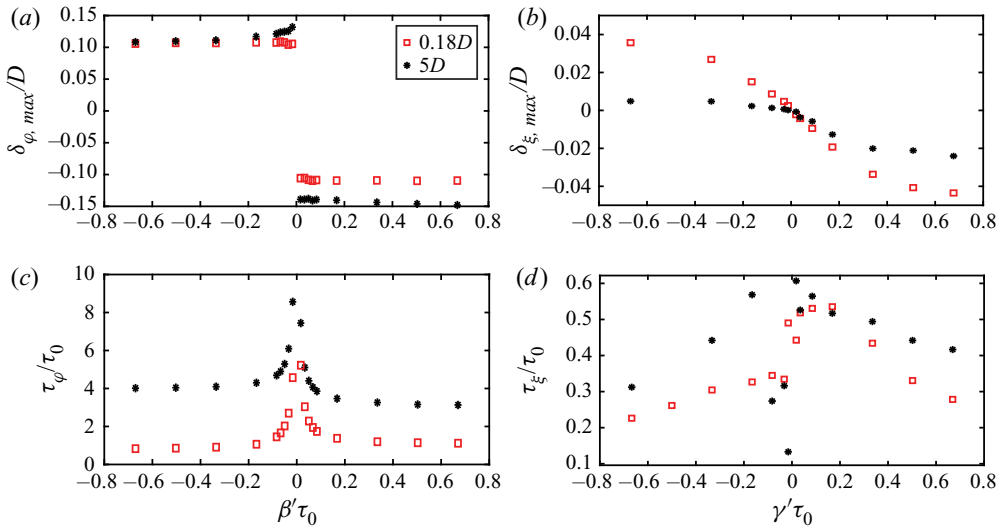


Figure 13. (a) Relationship between blade pitch rate and maximum wake expansion change at 0.18D and 5D downstream of the turbine. (b) Relationship between yaw rate and maximum inverse wake deflection at 0.18D and 5D downstream. (c) The effect of pitch rate on the wake expansion time scale at 0.18D and 5D downstream. (d) The effect of yaw rate on the inverse wake deflection time scale at 0.18D and 5D downstream.

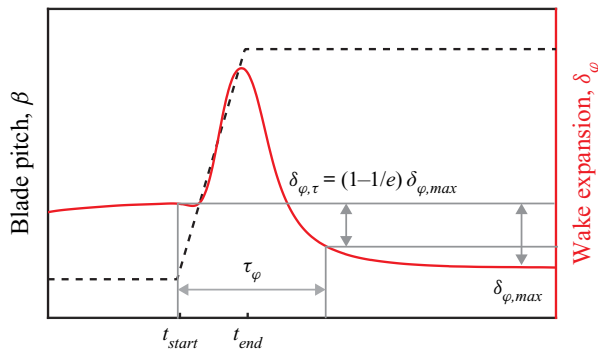


Figure 14. Sample change in blade pitch angle at a constant rate (dashed black line) and the resulting wake expansion response at 5D downstream (solid red line), with the wake expansion time scale,  $\tau_\varphi$ , and maximum change in wake expansion,  $\delta_{\varphi,\tau}$ , defined in grey.

above, both of which lead to increased uncertainty in the definition of the wake deflection time scale.

#### 4. Conclusions and discussion

The current study uses LES to model transient behaviours in the wake of a wind turbine in response to changes in blade pitch, incoming wind direction and yaw angle. Changes in blade pitch result in changes in wake expansion that are consistent with the results from the field study from Abraham & Hong (2020). The wake response to blade pitch changes displays hysteresis as a result of flow inertia, which causes a lag between changes in blade pitch and changes in tip speed ratio. The relationship between wake expansion and tip speed ratio exhibits the strongest dependence of the tested parameters, suggesting tip



speed ratio is most responsible for changes in wake expansion. The lag between blade pitch and wake expansion changes is quantified for different pitch rates, showing that, although the maximum change in wake expansion depends on the magnitude of the pitch change, the time for the wake to stabilize varies significantly with pitch rate. Changes in wind direction are investigated to further elucidate the relationship between wake deflection and dynamic yaw misalignment observed in Abraham & Hong (2020), which was opposite of the steady yaw misalignment response reported in previous studies (e.g. Jiménez *et al.* 2010; Bastankhah & Porté-Agel 2016; Shapiro *et al.* 2018). This behaviour is shown to depend strongly on the time scale of wind direction changes, with short-period changes (20 s) resulting in opposite wake deflection and long-period changes (50 s) demonstrating the steady wake deflection response. To separate the effects of turbine-modulated wake deflection from wake advection by the ambient flow, changes in rotor angle with a constant wind direction are investigated. The wake takes longer to reach the steady yaw response when the rotor angle is changed as a result of the removal of the wake advection effect. When the yaw rate is changed, a tradeoff is observed between inverse wake deflection time and magnitude. The mechanism behind the transient inverse wake deflection is elucidated by quantifying changes in streamwise vorticity in different parts of the wake. In the top-left quadrant, the vorticity increases during the yaw manoeuvre, while it decreases in the bottom-right quadrant, inducing a period of positive spanwise velocity. These behaviours are caused by changes in the relative velocities of each part of the rotor and the resulting change in projection angle of the blade tip vortices. Finally, these near-wake behaviours are shown to propagate downstream to the far wake. The wake expansion time scale increases as the perturbation induced by the blade pitch change is advected downstream, while the wake deflection time scale remains largely unchanged.

The results of the current study provide insight into the wake behaviour of utility-scale wind turbines operating under atmospheric conditions, enabling more accurate modelling and prediction of the real-world wake. They explain phenomena previously observed in high-resolution field-scale wake data. Furthermore, they have significant implications for recently proposed dynamic flow control strategies. One such strategy is the regulation of the thrust coefficient of each turbine in a wind farm, e.g. by modifying the blade pitch, to optimize the overall farm power generation (Goit & Meyers 2015; Munters & Meyers 2017; Yilmaz & Meyers 2018). This method can also be applied for power tracking, allowing wind farms to provide additional grid services (Shapiro *et al.* 2017). Another strategy for wind farm optimization is adaptive yawing to dynamically deflect wind turbine wakes away from downstream turbines (Gebraad *et al.* 2015; Raach *et al.* 2017, 2018). Munters & Meyers (2018a) proposed combining these two strategies to fully optimize wind farm power output, and Kanev *et al.* (2018) included fatigue loading considerations to maximize overall wind farm lifetime. However, the aforementioned studies did not provide detailed analyses of the time scales of the proposed dynamic wake changes. In order to effectively implement these novel wake control strategies by dynamically varying parameters such as blade pitch and rotor yaw, the transient wake response must be included in the models used to develop such algorithms. The current study shows that the wake consistently takes time of the order of  $D/U_\infty$  ( $\sim 10$  s for the set-up presented here) to reach a steady response. Therefore, wake changes with time scales shorter than this cannot be implemented effectively. This limitation is determined by the physical time scales of the vorticity in the wake and the inertia of the flow.

Dynamic wake modulation is expected to enhance wake recovery downstream due to the fluctuations of the near-wake boundary by an average 11 % increase in energy flux into the wake, as discussed in Abraham & Hong (2020) and Abraham, Martínez-Tossas

& Hong (2020). Although turbulence still dominates wake recovery, dynamic wake modulation provides a significant contribution. Munters & Meyers (2018b), Yılmaz & Meyers (2018) and Frederik *et al.* (2020) exploited dynamic wake behaviours to further enhance wake breakdown and accelerate recovery. Brown *et al.* (2021) also showed that dynamically varying the blade pitch and rotor speed excites unstable blade tip vortex modes, accelerating breakdown. The results of the current study additionally suggest that these dynamic wake modulations persist into the far wake where they can further impact on wake mixing. Furthermore, when the rotor misalignment angle changes, the resulting asymmetry of the blade tip vortices is expected to accelerate tip vortex breakdown. Tip vortex breakdown is typically induced by the development of instabilities in the vortex helix, particularly by the mutual inductance (vortex pairing) instability (Ivanell *et al.* 2010; Felli, Camussi & Di Felice 2011; Sørensen 2011; Sarmast *et al.* 2014; Lignarolo *et al.* 2015). The fundamental study of Ortega, Bristol & Savaş (2003) and the modal decomposition investigation of Sarmast *et al.* (2014) show that asymmetric vortex configurations destabilize faster than symmetric configurations. As tip vortex breakdown is the first step of wake recovery, the tip vortex asymmetry due to rotor misalignment will contribute to the enhanced wake recovery caused by dynamic wake modulation.

The asymmetric wake response to changes in rotor misalignment is also expected to contribute to wake meandering. Currently, two mechanisms have been proposed in the literature to understand wake meandering: the dynamic wake meandering model which considers the wake to be a passive tracer advected by large-scale atmospheric motions, and the idea that the rotor acts like a bluff body shedding vortices (Yang & Sotiropoulos 2019). Both of these frameworks treat the turbine as a passive structure, but our results show that the wake deflection is actively modulated by the turbine. In the field, the yaw misalignment between the rotor and wind is constantly changing due to the constant changes in wind direction, which leads to continual changes in wake deflection. These turbine-modulated wake deflections will be superimposed on any meandering caused by advection or bluff body vortex shedding.

The findings of the current study also have implications for turbines undergoing tilt angle changes. These tilt changes can be induced either by the rocking motion of ocean waves for offshore floating turbines (Rockel *et al.* 2014) or by active wake control (Annoni *et al.* 2017; Su & Bliss 2020). Previous studies have shown that the magnitude of wake deflection in the vertical direction during rotor tilt is comparable to spanwise wake deflection during yaw (Bossuyt *et al.* 2021), and that the counter-rotating vortex mechanism responsible for inducing steady-state spanwise wake deflection is also responsible for tilt-induced vertical wake deflection (Su & Bliss 2020). These similarities in steady-state behaviours suggest analogous dynamic wake behaviours would result from dynamic tilt changes. For floating offshore turbines, all tilt changes are dynamic, as wave-induced motions are inherently oscillatory. Alternatively, dynamic tilt-based control algorithms could be proposed with the addition of the necessary mechanical components. Future studies may investigate whether the potential benefits of such a control method outweigh the added cost of implementation. Note that the factors affecting vertical wake deflection under yawed conditions discussed at the end of § 3.4 will likely influence the vertical deflection induced by rotor tilt as well, and must be considered in such future investigations.

Finally, we acknowledge that the current study investigates the wake of a single example turbine. We expect the qualitative trends described here to hold true regardless of turbine design, but we caution the reader that the quantitative measures may not translate directly to other turbines. Future work can investigate the potential impact of turbine

size, geometry, rotation direction and siting on the observed phenomena. Additionally, the wake behaviour was studied under uniform inflow in order to isolate the effects of each parameter changed individually. However, the effect of such atmospheric phenomena as wind shear and veer can be investigated in future studies. More significantly, turbulence has not been included in the current study. Although the near wake is dominated by the coherent structures shed from the turbine, atmospheric turbulence dominates far-wake behaviour in the field (Zhan *et al.* 2020). Therefore, the direct applicability of the downstream dynamic wake modulation propagation analysis to wind turbines operating under real-world conditions is limited. As discussed in § 3.5, this far-wake analysis adds primarily theoretical value for idealized conditions.

**Supplementary movies.** Supplementary movies are available at <https://doi.org/10.1017/jfm.2021.737>.

**Acknowledgements.** The authors also thank N. Hamilton, S. Ananthan, G. Vijayakumar and M. Sprague from NREL for fruitful discussions and assistance with the simulations.

**Funding.** The research was performed using computational resources sponsored by the Department of Energy's Office of Energy Efficiency and Renewable Energy and located at the National Renewable Energy Laboratory. Funding was provided by the National Science Foundation INTERN funding opportunity as a supplement to NSF CAREER award NSF-CBET-1454259.

**Declaration of interests.** The authors report no conflict of interest.

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## Appendix A

The need for the selection of the 91 % confidence interval to define the wake width in the near wake rather than the 95 % interval typically used for the far wake becomes clear by looking closely at the Gaussian fit for a sample timestep. In the near wake, the velocity deficit drops more sharply at the wake edges than the Gaussian function. A cross-section of the wake velocity profile and Gaussian fit at hub height is shown in [figure 15\(a\)](#), along with lines indicating the location of the 95 % confidence interval ( $1.96\sigma$ ) and the 91 % confidence interval ( $1.7\sigma$ ). The 95 % interval intersects the velocity profile outside of the region of the velocity deficit that defines the wake. On the other hand, the 91 % interval intersects the velocity profile at the point of maximum velocity gradient, which demarcates the wake boundary. The specific value of 91 % was selected by finding the point of maximum velocity gradient at multiple timesteps. The need for the shift in definition of the wake boundary is further clarified in [figure 15\(b\)](#), which shows the near-wake velocity cross-section with both confidence intervals superimposed. The outer is the 95 % interval, which clearly overshoots the wake boundary, while the inner circle (91 % interval) captures the wake edge much more accurately.

## Appendix B

[Figure 16](#) shows streamwise vorticity in the near wake of the turbine during key points of the rotor yawing manoeuvre. The beginning of the yawing manoeuvre and the resulting increase in streamwise vorticity in the top-left quadrant of the wake are shown in the top two frames. The decrease in streamwise vorticity in the top-left quadrant of the wake due to the steady wake response and the end of the yawing manoeuvre are shown in panels (c,d).

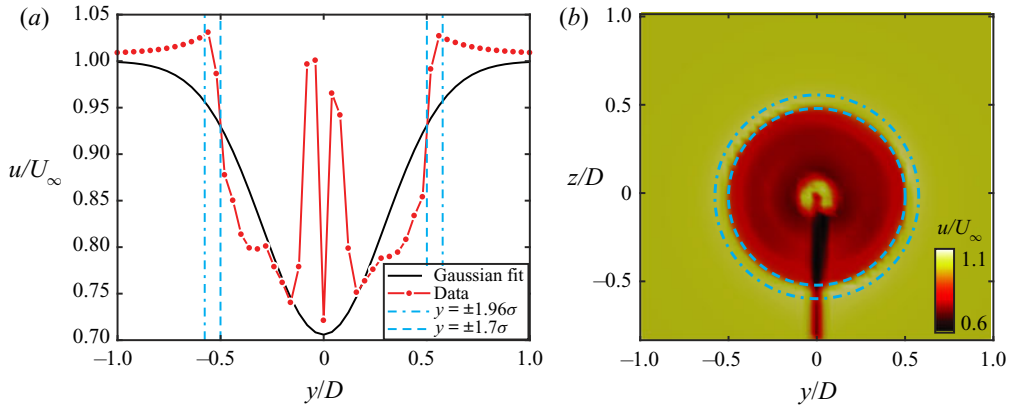


Figure 15. (a) Cross-section at hub height of the wake velocity field for a sample simulation time step compared with the corresponding Gaussian fit. Note that the sharp velocity peaks in the middle are characteristic of flow acceleration around the turbine nacelle. The width of the 95 % ( $y = \pm 1.96\sigma$ ) and 91 % ( $y = \pm 1.7\sigma$ ) confidence intervals are also indicated as vertical lines. (b) Wake velocity field with 95 % (dot-dashed circle) and 91 % (dashed circle) confidence intervals superimposed.

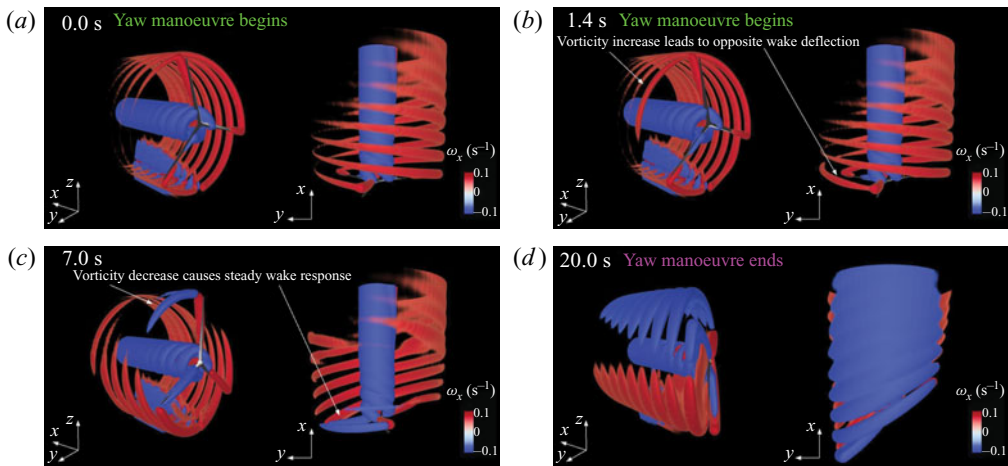


Figure 16. Stills of key points in supplementary movie 3 showing isocontours of streamwise vorticity in the wake during a rotor yawing manoeuvre. The values of the isocontours are  $\omega_x = 0.1 \text{ s}^{-1}$  and  $\omega_x = -0.1 \text{ s}^{-1}$  for the positive (red) and negative (blue) isocontours, respectively.

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