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Author for correspondence:

Vitor E. Valenti, Autonomic Nervous System Center, Sao Paulo State University, UNESP, Av. Hygino Muzzi Filho, 737. Mirante, 17.525-900 – Marilia, Sao Paulo, Brazil. Tel: +55 14 3402–1300. E-mail: vitor.valenti@unesp.br

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HRV analysis: undependability of approximate entropy at locating optimum complexity in malnourished children

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David M. Garner¹, Gláucia S. Barreto², Vitor E. Valenti³⁽¹⁾, Franciele M. Vanderlei⁴⁽¹⁾, Andrey A. Porto³⁽¹⁾ and Luiz Carlos M. Vanderlei⁴

¹Cardiorespiratory Research Group, Department of Biological and Medical Sciences, Faculty of Health and Life Sciences, Oxford Brookes University, Headington Campus, Gipsy Lane, Oxford, OX3 0BP, UK; ²Faculdade de Tecnologia Intensiva. FATECI – Fortaleza, Ceará, Sao Paulo, Brazil; ³Autonomic Nervous System Center, Sao Paulo State University, UNESP, Marília, Sao Paulo, Brazil and ⁴Department of Physiotherapy, Sao Paulo State University, UNESP, Presidente Prudente, Sao Paulo, Brazil

Abstract

Introduction: Approximate Entropy is an extensively enforced metric to evaluate chaotic responses and irregularities of RR intervals sourced from an eletrocardiogram. However, to estimate their responses, it has one major problem - the accurate determination of tolerances and embedding dimensions. So, we aimed to overt this potential hazard by calculating numerous alternatives to detect their optimality in malnourished children. Materials and methods: We evaluated 70 subjects split equally: malnourished children and controls. To estimate autonomic modulation, the heart rate was measured lacking any physical, sensory or pharmacologic stimuli. In the time series attained, Approximate Entropy was computed for tolerance $(0.1 \rightarrow 0.5 \text{ in intervals of } 0.1)$ and embedding dimension $(1 \rightarrow 5 \text{ in intervals of } 1)$ and the statistical significances between the groups by their Cohen's d_s and Hedges's g_s were totalled. Results: The uppermost value of statistical significance accomplished for the effect sizes for any of the combinations was -0.2897 (Cohen's d_s) and -0.2865 (Hedges's g_s). This was achieved with embedding dimension = 5 and tolerance = 0.3. Conclusions: Approximate Entropy was able to identify a reduction in chaotic response via malnourished children. The best values of embedding dimension and tolerance of the Approximate Entropy to identify malnourished children were, respectively, embedding dimension = 5 and embedding tolerance = 0.3. Nevertheless, Approximate Entropy is still an unreliable mathematical marker to regulate this.

The RR intervals derived from an electrocardiographic trace fluctuate in an irregular and often chaotic manner.¹ Historically, time series assessments have stimulated academics to examine this niche.^{2,3} The assessment of RR intervals is called Heart Rate Variability, a method for measuring the autonomic nervous system and, hence, its autonomic dysfunction. As a technique, it is simple, dependable and cheap and an important technique for arbitrating physiologically healthy and/or pathological conditions.^{4–6} Other techniques such as the sympathetic Skin Response are an alternative but unresponsive.^{7,8} Quantitative Pupillography is complicated and expensive.⁹ Throughout medical dynamical systems, high chaotic values may designate healthy physiological status but losses could be pathological.^{10,11}

Heart rate variability can be computed by an algorithm described by Pincus (1991), hence, Approximate Entropy.^{12–15} The benefits of Approximate Entropy include low computer processor demand. It is reliable with small sample lengths (RR < 50). Similarly, it can accurately decipher statistics even with considerable signal noise. Nonetheless, this technique has a crucial shortcoming in that its accuracy is very reliant on the following parameter choices – tolerance, *r* and embedding dimension, *M*. Approximate Entropy is as such difficult to interpret.

In this study, we systematically applied different combinations of embedding tolerance, *r*, and embedding dimension, *M*, in normal subjects and compared them to malnourished children. The relationship between malnourishment and complexity metrics is useful in the risk assessment of dynamical diseases associated with the illness and can support the treatment of these children. The crucial purpose is to enforce embedding tolerance, *r*, and embedding dimension, *M*, groupings to acquire their optimum, hence, achieving the greatest statistical significances between the groups.

Materials and methods

Population and sample

The malnourished group entailed children not more than -2 in z-score in relative to the height for the age, according to the criteria for age and gender by the World Health Organization.¹⁶

Table 1. Description of the characteristics of the population by group, gender, age (years), weight (kg), height (cm) and z-score (mean ± SD)

Group	Gender	Age (years)	Weight (kg)	Height (cm)	z -score
Malnutrition	23 Girls	3.71 ± 0.75	13.02 ± 1.71	91.53 ± 5.47	-2.80 ± 0.59
Eutrophic	20 Girls	4.09 ± 0.85	17.89 ± 3.04	106.83 ± 8.15	0.191 ± 1.28

The eutrophic group consisted of children with z scores ≥ -2 and below +3, also consistent with World Health Organization standards. Excluded from this study was obese children (z-score > +3) or who presented with no less than one of the subsequent criteria: children who were taking medications that would influence autonomic activity of the heart, such as propranolol and atropine. Also omitted were children who presented with infections, metabolic diseases or cardiorespiratory system diseases, which affected their cardiac autonomic control.

The subjects and their parents/guardians were duly well-versed as to the procedures and objectives of the study. After agreeing to participate, the parents/guardians signed terms of informed consent. All procedures received approval from the ethics committee of the Institution (Process nº 275.310). Ethical Committee in Research from Sao Paulo State University (UNESP), Marilia, SP, Brazil.

Experimental protocol

Before starting experimental procedures, information was noted on age, gender, mass and height. The anthropometric measurements were undertaken following the recommendations of Lohman *et al.*¹⁷ Mass was measured using a digital scale (Filizzola PL 150, Filizzola Ltda., Brazil) with a precision of 0.1 kg, with the children barefoot and wearing only lightweight clothing. Height was measured via an infantometer with an accuracy of 0.1 cm. The data collection was achieved in a laboratory with temperature between 21°C and 23°C and relative humidity between 40% and 60%. Data sets were logged between 14:00 and 17:00 to minimise the circadian rhythm interference. After the initial evaluation, all procedures required for data collection were explained on an individual basis. Children were told to continue at rest and avoid talking during the data collection.

Next, the heart monitor belt was placed over the thorax, aligned with the distal third of the sternum. The Polar S810i heart rate receiver (Polar Electro, Finland) was located on the wrist.^{18–21} The equipment had been previously validated for monitoring beat-by-beat heart rate and the use of these data for Heart Rate Variability analysis in children and adults.²⁰ The children were positioned in the dorsal decubitus with a cushion and remained at rest with spontaneous breathing for 20 minutes. After data collection, the child was discharged. The Heart Rate Variability behaviour pattern was logged beat-by-beat throughout the monitoring process at a sampling rate of 1 kHz. After the digital and manual filtering for the elimination of premature ectopic beats and artefacts, 1000 uninterrupted RR intervals were required for data analysis. Only series with >95% sinus rhythm were included in this study.²²

Mathematical analysis

Approximate entropy

Techniques based on entropy are routinely used in medical signal and data analysis.^{14,23} Approximate Entropy^{13,15,24,25} is a process

that evaluates the level of regularity and the unpredictability of changes over time series. Approximate Entropy is the logarithmic ratio of component-wise matching sequences from the signal length, *N*. Other parameters include *r* tolerance and *M* the embedding dimension. For instance, with studies assessing Heart Rate Variability in obese children,¹⁴ *r* is set to 0.2 and this represents 0.2 or, 20% of the standard deviation of the data sets RR intervals. A value of zero for Approximate Entropy would indicate a totally foreseeable series. Approximate Entropy increases with increasing chaotic response and irregularities. Further information regarding Approximate Entropy and it computation is found in the Kubios HRV* Manual.²⁶

Statistical analysis

At this point, we enforced various effect sizes to study the implications of the data. We did not evaluate normality^{27–29} and so did not enforce the one-way analysis of variance,³⁰ or Kruskal–Wallis³¹ test as in previous studies. These two statistical tests are unable to discriminate adequately between the small changes in significance apparent here. Therefore, we examine the significances using their effect sizes.^{32–34}.

Cohen's d_s^{35} is the foremost subcategory of effect sizes.

Cohen's
$$d_s = \frac{\overline{X}_1 - \overline{X}_2}{\sqrt{\frac{(n_1 - 1)SD_1^2 + (n_2 - 1)SD_1}{n_1 + n_2 - 2}}}$$

It refers to the standardised mean difference between two groups of independent observations for the suitable sample. It is founded on sample means and provides a biased estimate of the effect size. Throughout the mathematical algorithm for Cohen's d_s , the numerator is the variation between the means of two groups of observations. The denominator is the pooled standard deviation. These differences are squared. Next, they are summed and divided by the number of observations minus one for bias, in the estimation of the variance. To conclude, the square root is imposed on the denominator.

Hedges's
$$g_s = Cohen's \ d_s x \left[1 - \frac{3}{4(n_1 + n_2) - 9} \right]$$

Hedges's g_s is unbiased.³⁶ The change between Cohen's d_s and Hedges's g_s is very small in sample sizes >20. As regards, the Cohen's d_s and Hedges's g_s effect sizes' designated ranges are 0.01 > very small effect; 0.20 > small effect; 0.50 > medium effect; 0.80 > large effect. These are the benchmarks from Cohen³⁵ and Sawilowsky.³⁷

Results

A total of 70 volunteers of both genders between three and five years of age were split equally. Characteristics of the population are given in Table 1.

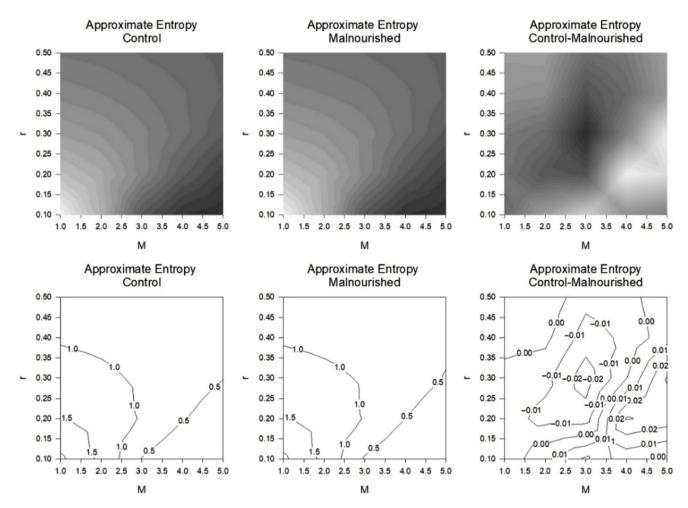


Figure 1. Contours Greyscale (Above) and Contour Lines (Below) Approximate Entropy (ApEn) for controls and subjects with Malnutrition (both n = 35). There were precisely 1000 RR intervals. Other parameters consist of tolerance, *r* and embedding dimension, *M*. There were 25 groups of values for tolerance, *r* ($0.1 \rightarrow 0.5$ in intervals of 0.1) and embedding dimension, *M* ($1 \rightarrow 5$ in intervals of 1) hence a grid of 5-by-5. The ApEn for the controls (left), those with Malnutrition (middle), the difference in ApEn between the controls and those with Malnutrition (right).

Childhood malnutrition's effect on the autonomic dysfunction has been established by chaotic global analysis.³⁸ It was demonstrated to lessen the chaotic responses and irregularities of RR intervals. Then, Approximate Entropy is methodically applied to 25 parameters for tolerance, r, and embedding dimension, M (Figure 1 & Table 2). This determined that under 50% were appropriate when judged physiologically. This is since, chaos and irregularities usually decrease for pathological states.^{10,11,38} In Table 2, Approximate Entropy for controls and malnourished children has tolerances, $r (0.1 \rightarrow 0.5$ in intervals of 0.1) and embedding dimensions, M (1 \rightarrow 5 in intervals of 1). A similar survey of parameter space was achieved in the study with subjects exhibiting type I diabetes mellitus¹³ and Chronic Obstructive Pulmonary Disease.¹⁵

In this study on malnourished subjects, as the embedding dimension, M increases the level of tolerance, r is less critical. For, M = 1.0, two of the values for r are fitting as malnutrition has (and, should have) a lesser chaotic response than the control with negative effect sizes. This is physiologically accurate and was demonstrated by chaotic globals.³⁸ Here, when M = 2.0, three out of five r values were apt and still negative effect sizes. Similarly, for M = 3.0, one of the values for r is suitable and for M = 4.0, two of

the five values for r are suitable. At M = 5.0, four out of the five values for r are apposite. All appropriate values have negative effect sizes for both statistical procedures, Cohen's d_s and Hedges's g_s .

Also, whilst the embedding dimension, *M* approaches 5.0, those values that are physiologically accurate have enlarged negative effect sizes by both measures. When studying the results in Table 2, we notice that the optimal statistical combination of *M* is 5.0 and *r* is 0.3 with ES = -0.2897 (Cohen's d_s) and -0.2865 (Hedges's g_s).

On closer inspection, where the *M* values are fixed, this could be surpassed. Perusing in finer detail (Table 3), setting values of *M* and manipulating *r*. We set M = 3 and $r = 0.1833 \rightarrow 0.4167$ in intervals of 0.0167, hence 15 values of Approximate Entropy. Then, M = 4 and $r = 0.1833 \rightarrow 0.4167$ in intervals of 0.0167, hence a further 15 values of Approximate Entropy, and so forth, until an *M* value of M = 6. For combinations of *M* and *r*, we determine that M = 5 achieves the greatest significance when tolerance r = 0.3 This corresponds to ES = -0.2897 (Cohen's d_s) and -0.2865 (Hedges's g_s), hence both with small effect sizes. This is the highest value of statistical significance reached for any of the combinations presented in either Tables 1–3.

Table 2. Approximate Entropy (ApEn) for controls and malnourished (MAL) subjects (both n = 35). There were exactly 1000 RR intervals for each subject. Other parameters consisted of tolerance, r and embedding dimension, M. There were 25 groups of values for tolerance, r (0.1 \rightarrow 0.5 in intervals of 0.1) and embedding dimension, M (1 \rightarrow 5 in intervals of 1). Illustrated are the ApEn for the mean controls with standard deviation, mean malnourished and standard deviation, then their effect sizes for control versus malnourished by Cohen's d_s and Hedges's g_s

		Approximate Entropy (n = 35)			Effect Sizes (ES)		
М	r	Mean Control	±SD Control	Mean MAL	±SD MAL	Cohen's d _s	Hedges's g _s
1.0	0.1	2.0835	0.1995	2.0906	0.2154	0.0343	0.0340
1.0	0.2	1.5309	0.2084	1.5361	0.2214	0.0242	0.0240
1.0	0.3	1.1877	0.1928	1.1911	0.2099	0.0170	0.0168
1.0	0.4	0.9567	0.1806	0.9528	0.1916	-0.0208	-0.0205
1.0	0.5	0.7859	0.1607	0.7791	0.1764	-0.0402	-0.0397
2.0	0.1	1.3842	0.0531	1.3760	0.0778	-0.1217	-0.1204
2.0	0.2	1.3296	0.1700	1.3430	0.1759	0.0775	0.0767
2.0	0.3	1.0904	0.1821	1.0974	0.1897	0.0377	0.0373
2.0	0.4	0.8996	0.1735	0.8969	0.1790	-0.0149	-0.0148
2.0	0.5	0.7508	0.1546	0.7435	0.1680	-0.0458	-0.0453
3.0	0.1	0.4799	0.1499	0.4581	0.1389	-0.1508	-0.1491
3.0	0.2	0.9566	0.0630	0.9709	0.0886	0.1859	0.1838
3.0	0.3	0.9349	0.1180	0.9608	0.1491	0.1925	0.1904
3.0	0.4	0.8117	0.1383	0.8263	0.1637	0.0962	0.0951
3.0	0.5	0.6899	0.1295	0.6966	0.1604	0.0464	0.0459
4.0	0.1	0.1028	0.0660	0.0996	0.0876	-0.0404	-0.0400
4.0	0.2	0.5306	0.1294	0.4997	0.1301	-0.2383	-0.2356
4.0	0.3	0.7356	0.0668	0.7360	0.0901	0.0040	0.0040
4.0	0.4	0.7125	0.1016	0.7202	0.1252	0.0678	0.0671
4.0	0.5	0.6306	0.1138	0.6344	0.1389	0.0299	0.0296
5.0	0.1	0.0199	0.0181	0.0224	0.0350	0.0888	0.0879
5.0	0.2	0.2365	0.1294	0.2109	0.1265	-0.1995	-0.1973
5.0	0.3	0.5068	0.1030	0.4760	0.1097	-0.2897	-0.2865
5.0	0.4	0.5952	0.0616	0.5892	0.0826	-0.0829	-0.0820
5.0	0.5	0.5735	0.0868	0.5664	0.1096	-0.0722	-0.0714

The bold values are the optimum values.

Discussion

We endeavoured to evaluate different combinations of r and M in malnourished children. Malnutrition in children has been demonstrated as a condition that greatly reduces chaotic response.^{10,39} Results demonstrated that Approximate Entropy is able to identify the reduction in chaotic response and the best combination of M and r for this study was 5.0 and 0.3, respectively.

Approximate Entropy measurements have some advantages in that they can be applied to short time series (RR < 50). Likewise, it is reasonably accurately at responding in the presence of substantial levels of signal noise. Nevertheless, its foremost disadvantage is the optimal choice of parameters for tolerance, *r* and embedding dimension, *M*.

In this study, initially, we enforced 25 different combinations r (0.1 \rightarrow 0.5 in intervals of 0.1) and embedding dimension M (1 \rightarrow 5 in intervals of 1). It was anticipated that since malnutrition is a condition which lessens the chaotic response of Heart Rate

Variability,³⁸ those combinations of r and M which increase their responses for malnutrition can be disregarded. They are physiologically inappropriate. These inapt values reached positive effect sizes for both Cohen's d_s and Hedges's g_s .

Thirteen out of twenty-five of the permutations provided a higher value for the control than for malnourished subjects. So, less than half of the computations provided a true assessment. When scrutinising the results further in Table 2, we can detect that the optimum combination of M is 5.0 and r is 0.3. We now need to examine the values more closely regarding the tolerance, r levels, whilst fixing M, embedding dimension (Table 3).

Consequently, for Table 3, we fixed the values of M and inspected the values more closely regarding its tolerance, r. Tolerance, r, was initially set at 0.1833 and increased up to 0.4167 in equal units (0.1833 \rightarrow 0.4167 at intervals of 0.0167). Therefore, we computed 15 values for each value of embedding dimension, M. In Table 3, the embedding dimension, M, varies from 3 to 6. The results for the two effect sizes were similar.

Table 3. Effect sizes (ES) by Cohen's d_s and Hedges's g_s for the ApEn for controls versus malnourished subjects (both n = 35). Exactly 1000 RR intervals were required in the calculations for each subject. Other parameters consisted of tolerance, r and embedding dimensions, M which are fixed at 3, 4, 5 and 6. There were 15 groups of values for tolerance, r (0.1833 \rightarrow 0.4167 in intervals of 0.0167)

		ES by Cohen's <i>d</i> _s				ES by Hedges's g _s			
r	M = 3	M = 4	M = 5	M = 6	M = 3	M = 4	M = 5	M = 6	
0.1833	0.0782	-0.2110	-0.1033	-0.0140	0.0773	-0.2087	-0.1021	-0.0138	
0.2000	0.1859	-0.2383	-0.1995	-0.1044	0.1838	-0.2356	-0.1973	-0.1033	
0.2167	0.1893	-0.1565	-0.1878	-0.1123	0.1872	-0.1548	-0.1857	-0.1110	
0.2333	0.2561	-0.1466	-0.2336	-0.2010	0.2532	-0.1450	-0.2310	-0.1988	
0.2500	0.1593	-0.1078	-0.1675	-0.0742	0.1576	-0.1066	-0.1657	-0.0733	
0.2667	0.1575	-0.0566	-0.1652	-0.1336	0.1557	-0.0559	-0.1634	-0.1321	
0.2833	0.1844	0.0555	-0.1942	-0.1943	0.1824	0.0549	-0.1921	-0.1922	
0.3000	0.1925	0.0040	-0.2897	-0.2515	0.1904	0.0040	-0.2865	-0.2487	
0.3167	0.1501	0.0103	-0.2324	-0.2004	0.1484	0.0102	-0.2298	-0.1982	
0.3333	0.1210	0.0292	-0.2467	-0.2080	0.1197	0.0289	-0.2440	-0.2057	
0.3500	0.1369	0.0728	-0.1922	-0.2246	0.1354	0.0720	-0.1901	-0.2221	
0.3667	0.1185	0.0791	-0.1401	-0.1916	0.1172	0.0783	-0.1385	-0.1895	
0.3833	0.1103	0.0689	-0.1545	-0.2382	0.1091	0.0681	-0.1528	-0.2355	
0.4000	0.0962	0.0678	-0.0829	-0.2056	0.0951	0.0671	-0.0820	-0.2033	
0.4167	0.1006	0.0680	-0.0975	-0.2783	0.0995	0.0672	-0.0965	-0.2752	

The bold values are the optimum values.

The highest level of discrimination for the suitable physiological responses by Cohen's d_s and Hedges's g_s was ES = -0.2897 and -0.2865, respectively (small effect size for M = 5.0 and r = 0.5). This is synonymous to Table 2.

Thus, Approximate Entropy has been demonstrated to be a moderately reliable marker if the embedding dimension M and tolerance r are carefully chosen such that the differences are maximised by Cohen's d_s and Hedges's g_s . There is at present no procedure or algorithm by which these values can be selected. So, Approximate Entropy can be viewed as an unpredictable marker which can only be used effectively when the M and r are selected by trial and error. Routinely, when assessing Heart Rate Variability studies, we set M = 2.0 and r = 0.2 where this represents 20% of the standard deviation of the time series.¹⁴ Now, in this study, that would give a positive effect size and as such, physiologically inapt. The chaotic global analysis would seem more reliable and dependable.³⁸ This is vital if we were enforcing Approximate Entropy when results were required online or under conditions that need to be calculated quickly as, for example, in an intensive care unit. It would be too slow and laborious to calculate all the possible values of Approximate Entropy. It would necessitate performing multiple calculations for every statistical outcome to reach the exact values to assess if an individual is pathological or healthy.

Approximate Entropy has been recognised to be an undependable mathematical marker. Yet, it has advantages such as performing well on short time series, even in the presence of substantial signal noise. Based on the results obtained, we encourage the use of the chaotic global methods as a substitute for judging severity of pathological conditions. Chaotic global analysis is easier to enforce, performs well on relatively short time series (RR > 256),⁴⁰ even with levels of noise, discriminates between the groups better and needs less computational time.^{10,11,41,42} Some points need to be addressed in our study. The present results should not be interpreted to smaller sample sizes, as we evaluated just 70 individuals. Different autonomic approaches were not used, including baroreflex sensitivity, skin conductance and neuroelectromyograph. It would provide additional physiological data for our analysis. And finally, our study reinforces the importance to emphasize the relationship between experimental HRV with clinical practice.

Conclusion

Childhood malnutrition has been established as a dynamic condition which lessens chaotic response. In this study, Approximate Entropy was able to identify the reduction in chaotic response during malnutrition. Until now, Approximate Entropy has been confirmed to be a relatively unreliable mathematical marker.

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References

- 1. Goldberger AL. Cardiac chaos. Science 1989; 243: 1419.
- Ho M-W. The Rainbow and the Worm: The Physics of Organisms. World Scientific, Singapore, 2008.
- Prigogine I. Non-equilibrium statistical mechanics. Interscience, New York, 1962.

- Mackey MC, Milton JG. Dynamical diseases. Ann N Y Acad Sci 1987; 504: 16–32.
- 5. Chang S. Physiological rhythms, dynamical diseases and acupuncture. Chin J Physiol 2010; 53: 77–90.
- Vanderlei LC, Silva RA, Pastre CM, et al. Comparison of the Polar S810i monitor and the ECG for the analysis of heart rate variability in the time and frequency domains. Braz J Med Biol Res 2008; 41: 854–859.
- Rachow T, Berger S, Boettger MK, et al. Nonlinear relationship between electrodermal activity and heart rate variability in patients with acute schizophrenia. Psychophysiology 2011; 48: 1323–1332.
- Wiertel-Krawczuk A, Hirschfeld AS, Huber J, et al. Sympathetic skin response following single and combined sound and electrical stimuli in young healthy subjects. J Med Sci 2016; 85: 106–113.
- 9. Baum P, Petroff D, Classen J, et al. Dysfunction of autonomic nervous system in childhood obesity: a cross-sectional study. PLoS One 2013; 8: e54546.
- De Souza NM, Vanderlei LCM, Garner DM. Risk evaluation of diabetes mellitus by relation of chaotic globals to HRV. Complexity 2015; 20: 84–92.
- Bernardo AF, Vanderlei LC, Garner DM. HRV analysis: a clinical and diagnostic tool in chronic obstructive pulmonary disease. Int Sch Res Notices 2014; 673232: 2014.
- 12. Pincus SM. Approximate entropy as a measure of system complexity. Proc Natl Acad Sci 1991; 88: 2297–2301.
- Garner DM, de Souza NM, Vanderlei LCM. Unreliability of approximate entropy to locate optimal complexity in diabetes mellitus via heart rate variability. Series Endo Diab Met 2020; 2: 32–40.
- Vanderlei F, Vanderlei LCM, de Abreu LC, et al. Entropic analysis of HRV in obese children. Int Arch Med 2015; 8.
- Garner DM, Bernardo AFB, Vanderlei LCM. HRV analysis: unpredictability of approximate entropy in chronic obstructive pulmonary disease. Series Cardiol Res 2021; 3: 1–10.
- Organization W H and Unicef. WHO Child Growth Standards and the Identification of Severe Acute Malnutrition in Infants and Children: A Joint Statement. United Nations Children's Fund, Washington, DC, 2009.
- Lohman TG, Roche AF, Martorell R. Anthropometric standardization reference manual, vol. 177. Human Kinetics Books Champaign, IL, USA, 1988.
- Barbosa MP, da Silva NT, de Azevedo FM, et al. Comparison of Polar(R) RS800G3 heart rate monitor with Polar(R) S810i and electrocardiogram to obtain the series of RR intervals and analysis of heart rate variability at rest. Clin Physiol Funct Imaging 2016; 36: 112–117.
- Gamelin FX, Berthoin S, Bosquet L. Validity of the polar S810 heart rate monitor to measure R-R intervals at rest. Med Sci Sports Exerc 2006; 38: 887–893.
- Vanderlei LCM, Silva RA, Pastre CM, et al. Comparison of the Polar S810i monitor and the ECG for the analysis of heart rate variability in the time and frequency domains. Braz J Med Biol Res 2008; 41: 854–859.
- Gamelin FX, Baquet G, Berthoin S, et al. Validity of the polar S810 to measure R-R intervals in children. Int J Sports Med 2008; 29: 134–138.
- 22. Godoy MF, Takakura IT, Correa PR. Relevância da análise do comportamento dinâmico não linear (Teoria do Caos) como elemento prognóstico de morbidade e mortalidade em pacientes submetidos à cirurgia de revascularização miocárdica. Arq Ciênc Saúde 2005; 12: 167–171.

- Pimentel RMM, Ferreira C, Valenti V, et al. Complexity measures of heartrate variability in amyotrophic lateral sclerosis with alternative pulmonary capacities. Entropy 2021; 23: 159.
- 24. Pincus S. Approximate entropy (ApEn) as a complexity measure. Chaos 1995; 5: 110–117.
- Richman JS, Moorman JR. Physiological time-series analysis using approximate entropy and sample entropy. Am J Physiol Heart Circ Physiol 2000; 278: H2039–H2049.
- Tarvainen MP, Niskanen J-P, Lipponen JA, et al. Kubios HRV-heart rate variability analysis software. Comput Methods Programs Biomed 2014; 113: 210–220.
- Anderson TW, Darling DA. A test of goodness of fit. J Am Stat Assoc 1954; 49: 765–769.
- Ryan TA, Joiner BL. Normal probability plots and tests for normality. In: Minitab Statistical Software: Technical Reports. The Pennsylvania State University, State College, PA. Available from MINITAB: Inc, 1976.
- Razali NM, Wah YB. Power comparisons of Shapiro-Wilk, Kolmogorov-Smirnov, Lilliefors and Anderson-darling tests. J Stat Model Anal 2011; 2: 21–33.
- Blanco-Topping R. The impact of Maryland all-payer model on patient satisfaction of care: a one-way analysis of variance (ANOVA). Int J Healthcare Manage 2020; 1–8.
- McKight PE, Najab J. Kruskal-Wallis test. In: Weiner IB, Craighead WE (eds). The Corsini Encyclopedia of Psychology. Wiley, Hoboken, NJ, 2010: 1–1.
- Kazis LE, Anderson JJ, Meenan RF. Effect sizes for interpreting changes in health status. Med Care 1989; 27(Suppl 3): S178–S189.
- Grissom RJ, Kim JJ. Effect Sizes for Research: A Broad Practical Approach. Lawrence Erlbaum Associates Publishers, Mahwah, NJ, 2005.
- Thompson B. Effect sizes, confidence intervals, and confidence intervals for effect sizes. Psychol Sch 2007; 44: 423–432.
- Cohen J. Statistical Power Analysis for the Behavioral Sciences. Routledge, Oxfordshire, England, UK, 2013.
- Hedges LV, Olkin I. Statistical Methods for Meta-Analysis. Academic Press, Cambridge, MA, USA, 2014.
- Sawilowsky SS. New effect size rules of thumb. J Mod Appl Stat Methods 2009; 8: 26.
- Barreto GS, Vanderlei FM, Vanderlei LCM, et al. Risk appraisal by novel chaotic globals to HRV in subjects with malnutrition. J Hum Growth Dev 2014; 24: 243–248.
- Garner DM, De Souza NM, Vanderlei LCM. Risk assessment of diabetes mellitus by Chaotic globals to heart rate variability via six power spectra. Rom J Diabetes Nutr Metab Dis 2017; 24: 227–236.
- 40. Garner DM, Vanderlei FM, Valenti VE, et al. Non-linear regulation of cardiac autonomic modulation in obese youths: interpolation of ultra-short time series. Cardiol Young 2019; 29(9): 1196–1201.
- Vanderlei FM, Vanderlei LC, Garner DM. Chaotic global parameters correlation with heart rate variability in obese children. J Hum Growth Dev 2014; 24: 24–30.
- 42. Vanderlei FM, Vanderlei LCM, Garner DM. Heart rate dynamics by novel chaotic globals to HRV in obese youths. J Hum Growth Dev 2015; 25: 82–88.