

Modeling Cutaneous Radiation Injury from Fallout

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ABSTRACT

Objective: Beta radiation from nuclear weapons fallout could pose a risk of cutaneous radiation injury (CRI) to evacuating populations but has been investigated only cursorily. This work examines 2 components of CRI necessary for estimating the potential public health consequences of exposure to fallout: dose protraction and depth of dose.

Methods: Dose protraction for dry and moist desquamation was examined by adapting the biological effective dose (BED) calculation to a hazard function calculation similar to those recommended by the National Council on Radiation Protection and Measurements for other acute radiation injuries. Depth of burn was examined using Monte Carlo neutral Particle version 5 to model the penetration of beta radiation from fallout to different skin tissues.

Results: Nonlinear least squares analysis of the BED calculation estimated the hazard function parameter θ^1 (dose rate effectiveness factors) as 25.5 and 74.5 (Gy-eq)² h⁻¹ for dry and moist desquamation, respectively. Depth of dose models revealed that beta radiation is primarily absorbed in the dead skin layers and basal layer and that dose to underlying tissues is small (<5% of dose to basal layer).

Conclusions: The low relative dose to tissues below the basal layer suggests that radiation-induced necrosis or deep skin burns are unlikely from direct skin contamination with fallout. These results enable future modeling studies to better examine CRI risk and facilitate effectively managing and treating populations with specialized injuries from a nuclear detonation. (*Disaster Med Public Health Preparedness*. 2019;13:463-469)

Key Words: acute radiation syndrome, nuclear weapons, radiation injuries, radioactive fallout, risk assessment

Following the detonation of an improvised nuclear device, populations evacuating through areas contaminated by fallout will be exposed to ionizing radiation. Although the gamma radiation dose to these populations during evacuation has been thoroughly studied, beta radiation dose to the skin has been largely ignored.¹⁻³ Beta radiation dose to the skin can be large from either direct skin contamination or groundshine, possibly exceeding midline dose by 3 to 66 times during the first 48 hours postdetonation.⁴ The large dose to the skin poses a risk of cutaneous radiation injury (CRI), caused by death of sensitive cells in the basal layer of the skin.⁴⁻⁷ The symptoms typical of CRI include erythema (reddening of the skin), dry desquamation (peeling), and moist desquamation (oozing skin).^{6,8,9} More severe injuries can be caused as well, including ulcers that do not heal or necrosis, but these require doses to deeper skin tissues than the basal layer.¹⁰

CRI has not been studied extensively in the past in evacuation scenarios because of the relatively large ED₅₀ for CRI (dose that causes CRI in 50% of the population). The ED₅₀ for dry and moist desquamation are 14 and 20 Gy to the skin, respectively, well

above the 3 Gy to the red bone marrow required to reach the ED₅₀ for hematopoietic injury.^{6,8,11} However, the focus on hematopoietic injury neglects doses to other parts of the body which may experience much larger doses, particularly the skin. Because beta radiation dose from groundshine and skin contamination can be many times larger than the dose to the red bone marrow from combined gamma and beta radiation, CRI may still occur in evacuating populations without lethal hematopoietic injury. Although erythema can also be caused by radiation exposure to the skin, this work focuses on desquamation due to the potential loss of the protective skin barrier. Moist desquamation alone may warrant a medical response due to infection risk, but, if CRI occurs concurrently with hematopoietic injury, this infection risk could be compounded by reduced white blood cell counts.

Determining the dose from fallout contamination is complicated by fallout fractionation. Fallout fractionation is the process by which volatile chain elements (radionuclides with condensation points less than 1400° C) are separated from refractory chain elements (radionuclides with condensation points greater than

1400°C) both geographically and physically.^{12,13} Radioactive fallout forms when superheated fission products mix with the soil and debris entrained in the mushroom cloud. The bulk material—ie, concrete, soil, weapon debris, and other detritus—will begin condensing at approximately 1400°C.¹³ Refractory chain radionuclides which condense at higher temperatures will either condense onto larger particles which did not fully vaporize or form nucleation points for the condensation of bulk material. These early-formed particles generally have refractory chain radionuclides distributed throughout their volume and tend to be larger.¹⁴ By contrast, volatile chain radionuclides with lower condensation points take longer to condense and, when they do, they tend to condense onto the surface of fallout particles.¹⁴ As smaller particles remain aloft longer, the lower the condensation point of the radionuclide and the longer it takes to condense, the more likely the volatile radionuclide will be found only on smaller particles. The separation of refractory and volatile radionuclides in fallout alters the gamma and beta radiation energy spectra, resulting in slight changes to skin dose with depth. Fallout fractionation was included in this study by assuming contamination occurred just outside the physical damage zones.

Estimating the probability and severity of CRI injuries is complicated by a variable dose rate and beta energy spectrum, both of which vary with time and alter the dose profile to tissues underlying the basal layer. This paper discusses an adaptation of the biological effective dose (BED) for CRI and MCNP modeling of depth of dose across the body. Given knowledge of a specific individual's contamination—including time of contamination, time from contamination to decontamination, path through contaminated areas, clothing worn, etc—the methods presented herein allow improved estimation of the risk of CRI to the individual with lower computational complexity.

METHODS

General Modeling Assumptions

While the overall method presented below for both dose rate effectiveness and depth of dose can be applied to any contamination scenario, this paper assumes the exposure was received from fallout from a 10 kt, pure fission nuclear weapon. Fallout exposure from both direct contamination of skin or clothing and groundshine are considered and calculated separately. Only fission products were considered—because of the enormous situational dependence of activation products on both the specific weapon's design and the surrounding environment at the time of detonation, the inclusion of activation products can only be done on a specific-scenario level. Prompt radiation from the detonation of the weapon was not included in this analysis.

Dose Rate Effectiveness Factor

As skin is a fast-healing tissue, with a cell repair half-time of only 1.1 to 1.3 hours, dose rate becomes a critical variable in

determining the extent of injury.⁵ Omitting healing of irradiated tissue in the modeling would lead to overestimation of radiation injury in the affected population, particularly for doses received at varying dose rates over long periods of time. Evacuation through contaminated areas following an improvised nuclear device detonation could take hours depending on the evacuation route chosen, and evacuating populations could be exposed to fluctuating dose rates.^{2,3} Fallout trapped against skin or on clothing may remain until the individual decontaminates, as was seen in previous fallout contamination incidents.^{15,16}

CRI, radiation dose, and the healing of skin tissues are well studied in the medical fields.^{5,17-21} Radiotherapy, fluoroscopy, and other radiation treatments or diagnostics are specially designed to spare skin tissue and avoid injury. Unfortunately, the calculation of CRI risk becomes increasingly complicated when the dose rate is not constant. Further, as injury in the most sensitive layer of the skin (ie, the basal layer) is avoided, medical knowledge of injury thresholds in deeper tissues is incomplete.

In the medical field, risk of injury is estimated using the BED calculation, which accounts for fractionation and/or protraction of radiation dose. The general form of the equation is shown in Equation 1.^{18,22,23} The Lea-Catcheside protraction factor, *G*, accounts for noninstantaneous doses and is shown in Equation 2.^{18,23} Tissues, especially rapidly repairing tissues such as the skin, repair radiation damage while the dose is ongoing. Thus, the effective dose saturates based on the dose rate. The Lea-Catcheside equation, however, contains a nested integral that becomes computationally complex for exposures with variable dose rates.

The general form of the BED equation^{18,22,23} is

$$BED = nd \left(1 + \frac{G \times d}{\alpha/\beta} \right), \quad (1)$$

where

n = the number of irradiation fractions,

d = the dose per fraction (Gy-eq),

G = Lea-Catcheside Protraction Factor, aka effect of tissue repair (tissue specific),

α = linear dose response parameter [Gy⁻¹], and

β = quadratic dose response parameter [Gy⁻²].

The Lea-Catcheside protraction factor^{18,23} is

$$G(t, T) = \frac{2}{D^2} \int_0^T R(t) \times \left(\int_0^t R(w) e^{-\mu_i(t-w)} dw \right) dt, \quad (2)$$

where

D = total dose received between 0 and T received by the tissue of interest (Gy),

T = total time period individual is irradiated (h),

$R(t)$ = dose rate in at time t (or time w) (Gy h⁻¹), and

μ = tissue repair constant (tissue specific) (h⁻¹).

The National Council on Radiation Protection and Measurements (NCRP) has recommended a different equation for calculation of acute radiation syndrome.^{8,9} This hazard equation, shown in Equations 3 and 4, still includes an integral but can be broken into a series summation. Adjusting the equation in this fashion allows a variable dose rate to be approximated as a series of constant-dose periods. There are published values for some parameters for CRI but there are no published estimates of θ^1 , the dose rate effectiveness factor, for CRI.⁸

The NCRP hazard functions^{8,9} for acute radiation syndrome is

$$P(T, S) = 1 - e^{-H_{T,S}(t)}, \text{ and} \quad (3)$$

$$H_{T,S}(t) = \ln(2) \left[\int_0^t \frac{\dot{D}_T(t)}{\theta_{T,S}^\infty + \theta_{T,S}^1 \dot{D}_T^{-1}(t)} dt \right]^{V_{T,S}} \text{ for } \dot{D}_T(t) \times t > TD_{T,S}, \quad (4)$$

where

$P(T,S)$ = probability of specific syndrome S and tissue T ,

$H_{T,S}(t)$ = hazard function of syndrome S in tissue T ,

t = time (h),

$\dot{D}_T(t)$ = dose rate to tissue T at time t (Gy-eq h⁻¹),

$\theta_{T,S}^\infty$ = dose rate that causes the syndrome in 50% of the population at an infinite dose rate (Gy-eq),

$\theta_{T,S}^1$ = dose rate effectiveness parameter [(Gy-eq)² h⁻¹],

$V_{T,S}$ = shaping parameter for a given syndrome S and tissue T , and

$TD_{T,S}$ = threshold dose for a given syndrome S and tissue T (Gy-eq).

In order to adapt the hazard function to the BED, the probability of injury versus dose for dry or moist desquamation was calculated using the BED equation for dose protraction varying between 0 hours (immediate, acute dose) and 24 hours. A nonlinear, least

squares regression method was used to determine the best fit of the hazard function to the BED-estimated risk for all doses and dose rates between the BED-predicted ED₅ and ED₉₅. For this calculation, the only parameter that was fit was the dose rate effectiveness factor, θ^1 . The region of fit was limited because fits below the threshold for injury (ED₅) or above the ED₉₅ would provide no additional information while biasing the fit to match extremely high or extremely low doses, in which outcome does not change significantly with dose. Instead, by limiting the fit to the ED₅ to ED₉₅ region, the fit is focused on the region in which a change in dose makes the greatest difference in outcome. Parameters used in the regression for both the BED equation and the hazard function are shown in Table 1.

Depth of Dose

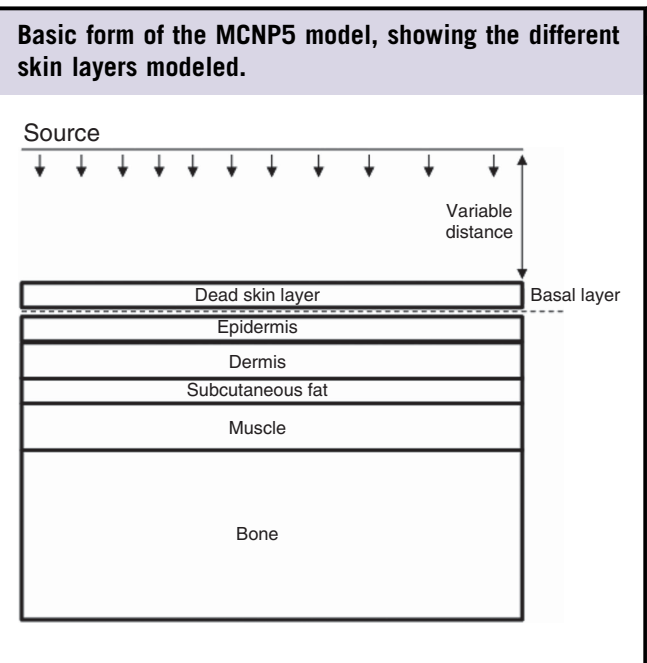
Depth of dose is important to modeling as deeper tissues that do not receive large doses will not experience radiation injury. The beta dose profile versus depth from either groundshine or direct skin contamination was modeled using

TABLE 1

Modeling parameters for least-squares fit of the hazard function to the biological effective dose equation.^{5,6,8}

Parameter	Value
Skin repair, μ (hr ⁻¹)	0.72
Dose rate response, α/β (Gy)	11.2
ED ₅₀ at infinite dose rate, θ^∞ (Gy-eq)	14 (dry), 20 (moist)
Shaping parameter, V	5

FIGURE 1



Modeling Radiation Injury

MCNP5.²⁴ The basic model form, shown in Figure 1, was based on the same model framework as were previous models of fallout injury to the skin.⁴ The model was run using the skin layer thicknesses of the upper arm, where data on the thickness of skin layers are the most robust, using thin, medium, and thick skin layer thicknesses (Table 2).²⁵⁻²⁸ Other areas of the body see much greater variation of subcutaneous fat layer thicknesses, especially the skin around the abdomen, or subcutaneous muscle layers.²⁹

Dose to the skin from fallout has been examined previously, particularly dose to the basal layer. The present work originally came out of an examination of the methodology used by the Defense Threat Reduction Agency in their ED04 report regarding skin dose to soldiers caused by fallout from atmospheric nuclear tests.³⁰ Other codes exist to model dose to the skin, including VARSKIN, but are primarily designed for regulatory compliance. VARSKIN in particular was designed to measure dose from dermal contamination and hot particles with respect to a contiguous 10-cm² area of skin at a depth of 0.007 cm up to the dose limit of 0.5 Gy.³¹ As this work focuses on acute radiation injury to tissue including but not limited to the basal skin layer at potentially extreme doses (>10 Gy in some cases, far exceeding regulatory limits), MCNP5 was used instead.

The beta energy spectra from fallout was estimated using the fractionated fallout composition for fallout just outside the damage zones of a 10 kt pure-fission detonation.³² This composition was compiled for a series of time points of interest and the beta spectra were calculated using beta energy spectra data for each radionuclide from the International Commission on Radiation Protection.³³ Due to the sensitive nature of fallout energy spectra, the composition and spectrum data are not shown (may be available upon request, at the discretion of the government sponsor). As beta energy also varies with distance between the source and skin, the relative dose to layers from groundshine was modeled at

TABLE 2

Modeled thicknesses of the various skin layers on the upper arm. Dead skin and basal layer thickness were not varied in this work.²⁵⁻²⁸

Skin Layer	Layer Thickness (mm)		
	Thin	Medium	Thick
Dead skin layer		0.070	
Basal skin layer		0.001	
Epidermis	0.500	1.000	1.500
Dermis	0.600	1.800	3.000
Subcutaneous fat	8.180	10.00	11.82
Muscle	21.50	25.10	28.70
Bone	2.300	4.400	6.100

several different time points and distances. The spectral effects of shielding by clothing were also included in the analysis. The time and distance combinations modeled are reported in Table 3. Groundshine was examined only in the 1- and 2-hour cases because these times are when dose from groundshine is expected to be large enough to threaten CRI in addition to other acute radiation injury.

RESULTS AND DISCUSSION

Dose Rate Effectiveness Factor

The dose rate effectiveness factors estimated were 25.5 (Gy-eq)² h⁻¹ for dry desquamation and 74.5 (Gy-eq)² h⁻¹ for moist desquamation. Both values are exceptionally high, most likely due to the extremely rapid repair of cells

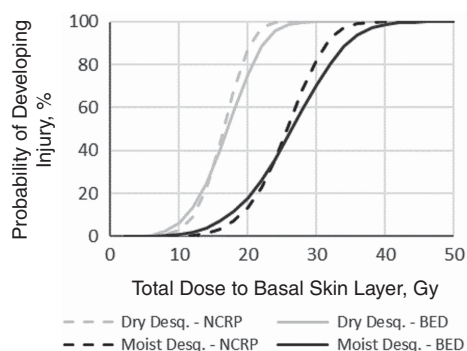
TABLE 3

Times postdetonation and distance between contamination source and the surface of the skin when modeling depth of radiation dose from beta radiation from fallout. A distance of 0 cm represents direct skin contamination. Distances greater than 0 cm represent exposure to groundshine.

Time Postdetonation (hr)	Distance (cm)
1	0, 1, 20, 100
2	0, 1, 20, 100
4	0
12	0
24	0
48	0
96	0
168	0

FIGURE 2

Probability of developing dry or moist desquamation (Desq.) following a 2-hour protracted dose at a constant dose rate. Data were estimated using both the biologically equivalent dose (BED) equation and the National Council on Radiation Protection and Measurements (NCRP) hazard function.



in the basal layer. Figure 2 shows a comparison of fit between the NCRP hazard function and the BED equation for a 2-hour protracted dose at a constant dose rate. The fit between the two equations is close, but not perfect. The NCRP equation produces a slightly steeper probit function resulting in underestimation of injury risk at low doses and an overestimation at high doses. The hazard function, however, allows for easier inclusion of CRI in complex models.

The difference in model outcomes between the BED model and the best-fit hazard function model is dependent on the dose distribution in the afflicted population. For a population whose individual doses are uniformly distributed between 0 and 50 Gy-eq to the basal layer, the best-fit hazard function model would overestimate the number of cutaneous injuries. If the population's doses were skewed lower, or if the upper limit was closer to 20 or 25 Gy-eq, the best-fit model would likely underestimate injuries. Given the wide range of possible ratios of basal layer

dose to whole body dose, it is not immediately clear how the dose to the evacuating population would be distributed, even assuming that no evacuating individual received a radiation dose greater than 8 or 10 Gy to the whole body.

Depth of Burn

In the MCNP5 model, the skin layers beneath the basal layer received very little dose relative to the basal layer (Figure 3 and Table 4). Underlying muscle and fat received almost no dose, and the dermis received less than 1% of the basal layer dose. Increased distance between the source and the skin changed the absolute dose of each layer but did not significantly affect the ratios (data not shown). As the dermis is one of the primary target tissues for necrosis, necrosis is unlikely in survivors except those with the most extreme doses. To achieve a dose of 25 Gy to the dermis, the ED₅₀ for necrosis, the basal layer would need to receive a dose of approximately 1938 Gy. Further, as the dose to the basal layer can be up to 66 times greater than the whole body dose, a dose of 25 Gy to the dermis from groundshine would correspond to a whole body dose of at least 29 Gy.⁴ At these doses, necrosis would not develop as the individual would die from radiation-induced hematopoietic, gastrointestinal, and cerebrovascular complications before the onset of necrosis. Even if the injury was due entirely to the direct skin contamination, the injury to the upper layers of the skin would be astronomical, causing erythema and desquamation long before necrosis.

The combination of acute skin injury without radiation-induced necrosis is not unexpected given the thicknesses of the tissues involved and the relatively low energy and penetration power of beta radiation. This outcome is in stark contrast to necrosis seen following radiotherapy, wherein radiation treatment is intentionally designed to penetrate to deeper tissues and resulting in larger doses to muscle, bone, and tendons. Historical exposures to fallout have similarly seen acute skin injury without necrosis. For example, the Marshallese Islanders on Rongelap, who suffered protracted skin contamination by fallout particles, experienced epilation, skin lesions, and hematopoietic effects (from gamma injury to red bone marrow), but no necrosis.¹⁵ Workers and cleanup crews working at the Chernobyl nuclear power plant experienced a wide range of cutaneous radiation injury without any necrosis.¹⁶ Although the chemical composition and isotopes present at a nuclear power plant are different than those from nuclear weapon fallout, the lack of necrosis or more severe injuries beyond nonhealing ulcers suggests that radiation injury is still limited to the upper layers of skin.¹⁶ It is still possible that necrosis may occur in these populations due to secondary injury or infection if initial radiation injuries are not treated. Moist desquamation, for example, destroys the natural skin barrier and leads to high risk of infection.²¹ Infection could, in turn, lead to necrosis if left untreated.

FIGURE 3

Relative dose of underlying skin layers to that of the basal skin layer over time for the medium thickness case at a distance of 0 cm (direct skin contamination). Changes in relative doses are driven by the changes in beta energy spectra from fallout.

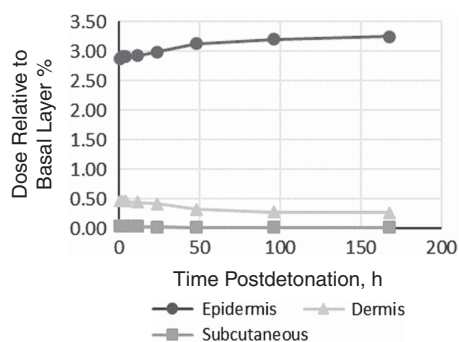


TABLE 4

Average relative dose of underlying skin layers to that of the basal skin layer for direct skin contamination by fallout

Skin Layer	Dose Ratio to Basal Layer	High	
		Low	High
Epidermis	3.02	0.16	4.95
Dermis	0.38	0.01	1.29
Subcutaneous	0.02	0.00	0.09
Muscle	0.00	0.00	0.00

CONCLUSIONS

These results provide a framework for better estimating CRI from protracted exposure to fallout. The basal layer of the skin heals quickly for both dry and moist desquamation, meaning inclusion of dose rate is critical to developing accurate models. If moist desquamation develops over large areas of the body, it can be life-threatening.⁸ Radiation-induced necrosis and more severe injury, on the other hand, are extremely unlikely. These injuries may still occur as a result of secondary infection following moist desquamation.

The results of this study can be used in combination with blast and evacuation models to estimate the number and severity of injuries and the amount and type of medical countermeasures that would be necessary to treat CRI following an improvised nuclear device detonation in a domestic US city.

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REFERENCES

1. Buddemeier BR, Valentine JE, Millage KK, et al, National Capital Region: Key Response Factors for the Aftermath of Nuclear Terrorism. Livermore, CA: Lawrence Livermore National Laboratory; 2011.
2. Brandt LD, Yoshimura AS. *Analysis of Sheltering and Evacuation Strategies for a National Capital Region Nuclear Detonation Scenario*. Albuquerque, NM: Sandia National Laboratory; 2011.
3. Brandt LD, Yoshimura AS. *Analysis of Sheltering and Evacuation Strategies for a Chicago Nuclear Detonation Scenario*. Livermore, CA: Department of Energy; 2011.
4. Barss NM, Weitz RL. Reconstruction of external dose from beta radiation sources of nuclear weapon origin. *Health Phys.* 2006;91:379-389. doi:10.1097/01.HP.0000218431.06620.ef
5. Turesson I, Thames HD. Repair capacity and kinetics of human skin during fractionated radiotherapy: erythema, desquamation, and

- relangiectasia after 3 and 5 year's follow-up. *Radiother Oncol.* 1989;15:169-188. doi:10.1016/0167-8140(89)90131-X
6. Archambeau JO, Pezner R, Wasserman T. Pathophysiology of irradiated skin and breast. *Int J Radiat Oncol Biol Phys.* 1995;31:1171-1185. doi: 10.1016/0360-3016(94)00423-I
7. Blackmar A. Radiation-induced skin alterations. *Medsurg Nurs.* 1997;6:172-175.
8. International Atomic Energy Agency. *Development of an Extended Framework for Emergency Response Criteria*. Vienna, Italy: International Atomic Energy Agency; 2005.
9. Evans J, Moeller D, Cooper D. *Health Effects Model for Nuclear Power Plant Accident Consequence Analysis (NUREG/CR-4214)*. Washington, DC: Superintendent of Documents, US Government Printing Office; 1985.
10. Hopewell J. Mechanisms of the action of radiation on skin and underlying tissues. *Brit J Radiol.* 1986;19:39-47.
11. Strom DJ. *Health Impacts from Acute Radiation Exposure*. Richland, WA: Pacific Northwest National Laboratory; 2003.
12. Mamuro T, Yoshikawa K, Maki N. Radionuclide fractionation in fallout particles. *Health Phys.* 1965;11:199-209. doi:10.1097/00004032-196503000-00006.
13. Freiling E, Kay M, Sanderson J. *Fractionation IV: Illustrative Calculations of the Effect of Radionuclide Fractionation on Exposure-Dose Rate from Local Fallout*. San Francisco, CA: Department of Defense; 1964.
14. Glasstone S, Dolan P. *The Effects of Nuclear Weapons*. Washington, DC: US Department of Defense and Energy Research and Development Administration; 1977.
15. Canard RA. *Review of Medical Findings in a Marshallese Population Twenty-Six Years After Accidental Exposure to Radioactive Fallout*. Upton, NY: Brookhaven National Laboratory; 1980.
16. Gottlob P, Steinert M, Weiss M, et al. The outcome of local radiation injuries: 14 years of follow-up after the Chernobyl accident. *Radiat Res.* 2001;155:409-416. doi:10.1667/0033-7587(2001)155[5B0409:TOOL RI]5D2.0.CO;2.
17. Barendsen GW. Dose fractionation, dose rate and iso-effect relationships for normal tissue responses. *Int J Radiat Oncol Biol Phys.* 1982;8:1981-1997. doi:10.1016/0360-3016(82)90459-X.
18. Brenner DJ, Hlatky LR, Hahnfeldt PJ, et al. The linear-quadratic model and most other common radiobiological models result in similar predictions of time-dose relationships. *Radiat Res.* 1998;150:83-91.
19. Chougule A, Supe SJ. Early skin reactions in head and neck malignancy treated by twice-daily fractionated radiotherapy - estimation of alpha/beta of lq model. *Phys Med Biol.* 1993;38:1335-1342.
20. Turesson I, Notter G. The influence of the overall treatment time in radiotherapy on the acute reaction: comparison of the effects of daily and twice-a-week fractionation on human skin. *Int J Radiat Oncol Biol Phys.* 1984;10:607-618. doi:10.1016/0360-3016(84)90291-8.
21. Koenig TR, Wolff D, Mettler FA, et al. Skin injuries from fluoroscopically guided procedures part 1, characteristics of radiation injury. *Am J Roentgenol.* 2001;177:3-11.
22. Fowler JF. 21 years of biologically effective dose. *Brit J Radiol.* 2010;83:554-568. doi:10.1259/bjr/31372149.
23. Brenner DJ. Point: The linear-quadratic model is an appropriate methodology for determining iso-effective doses at large doses per fraction. *Sem Rad Oncol.* 2008;18:234-239.
24. X-5 Monte Carlo Team. MCNP - A General Monte Carlo N-Particle Transport Code, Version 5. Vol 2; 2003. Los Alamos, NM: Los Alamos National Laboratory.
25. Tingart MJ, Apreleva M, von Stechow D. The Cortical thickness of the proximal humeral diaphysis predicts bone mineral density of the proximal humerus. *Bone Joint J.* 2003;85-B:611-617. doi:10.1302/0301-620X.85B4.12843.
26. Toomey C, McCreesh K. Technical considerations for accurate measurements of subcutaneous adipose tissues thickness using b-mode ultrasound. *Ultrasound Med Biol.* 2011;38:28-34.

27. Ogasawara R, Thiebaut RS, Loenneke JP, et al. Time course for arm and chest muscle thickness changes following bench press training. *Interv Med Appl Sci*. 2012;4:217-220. doi:10.1556/IMAS.4.2012.4.7.
28. National Cancer Institute, US National Institutes of Health. Layers of the skin. SEER Training Modules. <https://training.seer.cancer.gov/melanoma/anatomy/layers.html>. Accessed January 12, 2017.
29. Kim J, Lim H, Lee SI, et al. Thickness of rectus abdominis muscle and abdominal subcutaneous fat tissue in adult women: correlation with age, pregnancy, laparotomy, and body mass index. *Arch Plast Surg*. 2012;39:528-533. doi:10.5999/aps.2012.39.5.528.
30. Defense Threat Reduction Agency. *EDO4 - Skin Dose from Dermal Contamination*. Fort Belvoir, VA: Defense Threat Reduction Agency; 2010.
31. Hamby DM, Mangini CD, Caffrey JA, et al. *VARSKIN 5: A Computer Code for Skin Contamination Dosimetry*. Corvallis, OR: US Nuclear Regulatory Commission; 2014.
32. Monterial MJ, Vincent J. *Updated Properties of Fractionated Fallout: Predictions of Activities, Exposure Rates, and Gamma Spectra for Selected Situations*. Oak Ridge, TN: Oak Ridge National Laboratory; 2012.
33. Radionuclide transformations: energy and intensity of emissions. *Annals of the International Commission on Radiation Protection, Publication 38*. 1983:11-13.