

Structural Humility

Cruz Austin Davis*†

In this article I discuss various humility theses about individuals and intrinsic properties as discussed by authors such as David Lewis. I argue that we should accept a similar humility thesis about the world's space-time structure regardless of which metaphysics of space-time we accept. I argue this undercuts some important motivations opting in for an ontic structural realist metaphysic.

1. Introduction. We can see our world (and possible worlds generally) as naturally dividing up into structure and contents. The contents of the world further divide into the properties and individuals that are instantiated at and exist in the considered world, respectively. Yet, the structure of the world provides the way that the contents are organized.

Call a thesis a 'Humility Thesis' if it amounts to claiming that there is some important part of the world that we are irremediably ignorant of. Humility Theses are claims of some systematic epistemic limitations we have. For example, Lewis (2009) argues that we are irremediably ignorant of the identities of many properties of things.¹ We only come to know them as role-occupants (of dispositions or other roles). But given a contingent connection between roles and occupants, different properties can occupy the same role at different worlds. Thus, knowledge that the role is occupied is insufficient for identifying the property occupying that role. An analogous Humility Thesis arises in the case of individuals. Assume that we can know the qualitative character of the individuals in our world. If individuals are only contingently

*To contact the author, please write to: UMass Amherst, E412 South College, 150 Hicks Way, Amherst, MA 01003; e-mail: cruzdavis@umass.edu.

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1. I discuss Lewis's arguments in sec. 2.

connected with their qualitative properties (in the way role-occupants were suggested to be connected with their roles), then different individuals could occupy the same qualitative characters in different worlds. If this is so, then knowledge that a particular qualitative character is had is likewise insufficient to know the identity of the individual who has that character.

The routes just sketched for these two Humility Theses bear a significant similarity. Both aforementioned Humility Theses involve claims about our epistemic limitations regarding our knowledge of the identities of *contents* of the world. The question I want to ask in this article is whether there is reason to think that we may be irremediably ignorant of the *structure* of the world. Spatiotemporal structures provide common examples of world structures. As such I limit the following discussion to whether we should accept a Humility Thesis about the world's spatiotemporal structure.² In particular, I argue that we remain irremediably ignorant of whether we are in a world with distinct regions that are topologically indistinguishable from one another.

I begin by briefly reviewing Lewis's argument for Humility about the intrinsic properties of things ('Ramseyan Humility' henceforth). I then discuss whether we should endorse a corresponding Humility Thesis about the world's spatiotemporal structure ('Structural Humility' henceforth). I argue that the standard metaphysics of space-time fall prey to Structural Humility. This is significant because avoiding concerns of Humility is touted as a reason for adopting a particular metaphysic of space-time. I conclude with a brief discussion of the implications of Structural Humility for this view.

2. Ramseyan Humility. Lewis's argument for Humility regarding our knowledge of properties begins with two arguments for Humility about *fundamental* properties.³ Fundamental properties can come in a variety of categories. They can be all-or-nothing properties of various adicities or come in varying degrees such as scalar and vector magnitudes, and so on.

Advances in scientific theorizing and the discovery of fundamental properties stand in a mutual relationship. So much so that a true and complete final theory, \mathcal{T} , will provide us with a complete inventory of the fundamental properties at work in nature. The final theory, \mathcal{T} , however, will leave out properties that are instantiated but play no role in nature ('idlers') and those

2. In what follows I ignore current discussion about whether our world is fundamentally spatiotemporal, although I believe that my discussion will generalize to other types of world structures.

3. Lewis (2009, 204–5) tells us that the fundamental properties are those that ground objective similarity and difference; they provide a minimal base for the rest of the world's qualitative features. For more in-depth treatments of fundamental properties, see Lewis (1983; 1986, 59–63).

fundamental properties that are not instantiated in our world ('aliens'; Lewis 2009, 205).

The argument for Ramseyan Humility can be seen as proceeding in two steps. First, the argument shows that any evidence for our fundamental theory, \mathcal{T} , is just evidence for what is called the *Ramsey sentence* of \mathcal{T} . Second, it is argued that the Ramsey sentence of \mathcal{T} admits of multiple realizations. Since all evidence for \mathcal{T} is only evidence for the Ramsey sentence of \mathcal{T} and because the Ramsey sentence of \mathcal{T} is not uniquely realizable, we have no more evidence for \mathcal{T} than any other possible realizer of the Ramsey sentence of \mathcal{T} . Allow me to unpack.

Recall \mathcal{T} is our final and complete theory at the limit of empirical inquiry. The language of \mathcal{T} contains *\mathcal{T} -terms*, which are the theoretical terms implicitly defined by \mathcal{T} . Then there is the rest of our language, which Lewis calls *\mathcal{O} -language* for 'old language'. *\mathcal{O} -language* is what is available to us without the term introducing theory \mathcal{T} . The *\mathcal{O} -language* is rich enough to describe all possible observations (Lewis 2009, 205–6).

Recall that all fundamental properties except aliens and idlers will be listed in \mathcal{T} 's inventory. Importantly, all of the fundamental properties mentioned in \mathcal{T} are named by the \mathcal{T} -terms (Lewis 2009, 206). Now the theory \mathcal{T} consists in all of the logical consequences of a sentence called the *postulate* of \mathcal{T} . We can write the postulate as $\mathcal{T}(t_1, \dots, t_n)$, where t_1, \dots, t_n are the theoretical terms introduced by \mathcal{T} , and all of the rest of the language in the postulate is *\mathcal{O} -language*. When we replace all of the \mathcal{T} -terms with variables, we get $\mathcal{T}(x_1, \dots, x_n)$. An n -tuple that satisfies \mathcal{T} with respect to the actual world is called an *actual realization* of \mathcal{T} , whereas one that can satisfy \mathcal{T} with respect to some possible world is a *possible realization* of \mathcal{T} . We then get the *Ramsey sentence* of \mathcal{T} when we prefix $\mathcal{T}(x_1, \dots, x_n)$ with existential quantifiers: $\exists x_1, \dots, \exists x_n, \mathcal{T}(x_1, \dots, x_n)$ (207). Significantly, the Ramsey sentence of \mathcal{T} implies exactly those *\mathcal{O} -language* sentences that are implied by the postulate of \mathcal{T} (207 n. 6). Because the *\mathcal{O} -language* is rich enough to describe all possible experiences, the predictive success of \mathcal{T} will be the same as the Ramsey sentence of \mathcal{T} . This means that if there are multiple possible realizations of the Ramsey sentence of \mathcal{T} , no possible observation can tell us which one is the actual realization. This is because, no matter which one is the actual realization, the Ramsey sentence will be true, and our observational evidence only gives us evidence for the truth of the Ramsey sentence (207).

What is left to be shown is that there are in fact multiple realizations of the Ramsey sentence of \mathcal{T} . Lewis offers two arguments for this conclusion: the *permutation argument* and the *replacement argument*. Both rely on Lewis's acceptant of a principle of recombination, namely, that we can take apart distinct elements of a possibility and rearrange them, we can remove some of the distinct elements, we can reduplicate some of them, and we can replace

elements of some possibility with elements of others and get a new possibility (2009, 207–8).⁴ It is important to note that distinct elements cannot be recombined in any way possible but that they have to be recombined in a category-preserving way.

The permutation argument starts with the assumption that we have the actual realization of \mathcal{T} . Then we find the members of the n -tuple that satisfies \mathcal{T} that are fundamental and belong to multimembered categories. Then we permute these within their categories to get a new n -tuple that satisfies \mathcal{T} . The principle of recombination is what allows us to permute these properties to get a possibility. *Quidditism*, the view that two worlds can differ merely by permutation of fundamental properties, gets us that the resulting possibility is distinct from the original possibility. Note that the argument from permutation only gets us humility insofar as there are actual fundamental properties of multimembered categories that can be swapped. If there are only a small number of categories of fundamental properties in \mathcal{T} that are multimembered, this does not guarantee a sweeping Humility Thesis (Lewis 2009, 208–12). The replacement argument is designed to provide a more sweeping conclusion.

The replacement argument gets us Humility through replacing the fundamental properties in \mathcal{T} with fundamental alien and idling properties of the same category. If there are alien or idling properties that fall into the same categories as the fundamental properties mentioned in \mathcal{T} , then recombination entails that there are distinct possibilities where some or all of the fundamental properties in \mathcal{T} have been replaced with aliens or idlers of the same category. Lewis offers a few reasons to think that there will be enough alien properties to replace at least a large majority of the fundamental properties in the actual realization of \mathcal{T} . The reason I find the most powerful begins by noting that it is a contingent matter what fundamental properties are instantiated. And once we have appreciated this fact we should think that there is a world where more fundamental properties are instantiated than are instantiated at this world. And there is a further world with more properties instantiated at it than the second one, and so on. It is implausible to think that among these worlds with more fundamental properties than ours that there will not be alien properties that are members of most, if not all, of the categories of the fundamental properties mentioned in \mathcal{T} . Thus, we have good reason to think that there are sufficiently enough alien properties for the replacement argument to go through. This gives us an argument for a much more sweeping Humility Thesis than the permutation argument (Lewis 2009, 212–14).

4. For an in-depth discussion into formulating a principle of recombination and other principles of plenitude, see Bricker (2020, chap. 10).

3. Humility about Spatiotemporal Structure. We have seen how Lewis argues for a Humility Thesis about our knowledge of the properties our world instantiates in his arguments for Ramseyan Humility. To get to Structural Humility we need to proceed differently. One important reason for thinking this has to do with the inapplicability of recombination to structure. Lewis's arguments for Ramseyan Humility made use of recombination to swap properties around from within a world or swap properties from a different world into the structure of the old one in order to get new possibilities. We cannot swap around parts of structures in the same way. Trying to use recombination to fill out the possible world structures runs into serious problems. Further, the recombination principle that Lewis uses presupposes that there is a structure to recombine the elements into. Instead, we need a different principle of plenitude for structures. I believe if we accept a plausible principle of plenitude for world structures and we accept some plausible views about the nature of the world's geometric structure, then we remain irremediably ignorant of important aspects of the world's geometric structure, namely, of whether the world we live in contains distinct topologically indistinguishable points and how the distinct indistinguishable points are distributed.⁵

3.1. Metric and Merely Pseudometric Spaces. First, let us take a look at two different classes of geometric structures. *Metric spaces* are spaces whose topology is solely determined by a distance function that meets the following definition:

$$\mathbf{D1} \quad d(x, y) = 0 \Leftrightarrow x = y. \quad (\text{Identity of Indiscernables})$$

$$\mathbf{D2} \quad d(x, y) = d(y, x). \quad (\text{Symmetry})$$

$$\mathbf{D3} \quad d(x, y) + d(y, z) \geq d(x, z). \quad (\text{Triangle Inequality})$$

Three-dimensional Euclidean spaces count as examples of a metric space. The metric spaces are part of the larger class of *pseudometric spaces*. That is, all metric spaces are pseudometric spaces, but not all pseudometric spaces are metric spaces. The class of pseudometric spaces is the class of spaces whose topology is defined by a distance function that replaces D1 with

$$\mathbf{D1}^* \quad x = y \Rightarrow d(x, y) = 0. \quad (\text{Indiscernibility of Identicals})$$

In other words pseudometric spaces include geometric structures that have distinct points at zero distance from one another. Call the pseudometric spaces that have distinct points at zero distance from one another *merely pseudometric*

5. Any distinct points, p and p^* , are *topologically indistinguishable* just in case for any open set, S , p belongs to S just in case p^* belongs to S .

spaces. The metric spaces and the merely pseudometric spaces are mutually exclusive and exhaust the class of pseudometric spaces. Metric spaces and merely pseudometric spaces only differ over whether they have distinct topologically indistinguishable points. In metric spaces, the open sets that fix the topology also uniquely determine the points in that space; in merely pseudometric spaces, this is not the case. Moreover, in merely pseudometric spaces there will also be distinct topologically indistinguishable regions apart from the point-sized ones. For any two distinct topologically indistinguishable regions, R and R^* , there are some distinct topologically indistinguishable points, p and p^* , such that p is in both R and R^* yet p^* is in R but not R^* (or vice versa).

3.2. The Possibility of Merely Pseudometric Spaces. We are accustomed to thinking in terms of spaces that are metric spaces. In fact, I imagine most think it is constitutive of being a point that it is uniquely identified by its place in the world's geometric structure. The possibility of merely pseudometric spaces flouts this intuition. So there needs to be good reason to think that merely pseudometric spatial structures are possible. The best way to go about this requires providing a principled way to determine what structures are possible and which ones are not. Bricker (1991) provides what I take to be the best method for determining the possibility of a class of world structures.

The method can be summed up as follows: first, we need to determine what structures have played an explanatory role in our theorizing about the world.⁶ Here, playing an explanatory role is not understood in sociological but objective terms—the structures must have genuine explanatory power (Bricker 1991, 609). Determining these structures provides the base of logically possible structures from which we can generalize to other possible structures. Next, we need to determine which classes of structures are natural classes. The members of natural classes of structures objectively resemble each other in ways that members of classes that are not natural do not. We determine the natural classes of structures by seeing whether each of them serves as a principle object of study in some major area of study in mathematics—the ones that do are the natural classes (611–12).⁷ This gives us candidate natural classes of structures to generalize to as logically possible-ones. Finally, not just any generalization from the base classes of structures

6. In particular Bricker tells us “we have warranted belief that a structure is logically possible if that structure plays, or has played, an explanatory role in our theorizing about the actual world” (1991, 609). This just gives us a base set of structures from which we will determine the whole class or classes of possible structures.

7. Although, they are not natural because they are the principle objects of study of some major area in mathematics. Instead, they are the principle objects of study in some major area in mathematics because they are natural.

to a natural class will count as a good generalization. Only those natural classes that are *natural generalizations* of the structures in our base count as logically possible structures (617). Here, again, we defer to mathematicians to see what classes of structures are natural generalizations of others. This method gives us the following principle of plenitude:

Principle of Plenitude of Structures Suppose \mathcal{S} is a class of logically possible structures. Any structure belonging to any natural generalization of \mathcal{S} is logically possible. (617)

The argument for the possibility of merely pseudometric structures is straightforward. First, the class of Euclidean spaces, \mathcal{E} , is a prime example of a class of structures that have played a role in our theorizing about the actual world. So \mathcal{E} is a class of logically possible structures. The class of metric spaces, \mathcal{M} , is a natural generalization of \mathcal{E} , so this means any structure in \mathcal{M} is logically possible. This is the same as saying that \mathcal{M} is a class of logically possible structures. Finally, the class of pseudometric spaces, \mathcal{P} , is a natural generalization of \mathcal{M} . Because \mathcal{M} is a class of logically possible structures, and \mathcal{P} is a natural generalization of \mathcal{M} , any structure in \mathcal{P} is logically possible. All of the structures of pseudometric spaces are in \mathcal{P} . This includes all of the merely pseudometric spaces. So, merely pseudometric spaces are logically possible. Moreover, any merely pseudometric spatial structure is a logically possible one.

3.3. Undetectable Differences. Recall that Lewis's argument for Ramseyan Humility is intended to show that although we can come to know the properties of things as role-occupants this is insufficient to identify the role-occupier. The points, specifically, and regions, generally, in a geometric structure can likewise be thought of as role-occupants of that particular geometric structure. I would like to suggest that we can think of the difference between merely pseudometric and metric spaces in a similar way. The rough thought is that the distinct but topologically indistinguishable points in merely pseudometric spaces play the same role as the unique topologically distinguishable points in metric spaces. To put the idea slightly differently, we cannot tell how complex the occupants of the point-roles in the world's geometric structure are. This is not quite right but provides us with a useful, albeit imperfect, way of drawing out the similarity between Ramseyan Humility and Structural Humility.

An important feature of merely pseudometric spaces is that there is a way to "convert" them into metric spaces. Recall that the only difference between a particular metric spatial structure and its equivalent merely pseudometric structures is that they disagree on whether there are distinct topologically indistinguishable points. Different merely pseudometric structures that are otherwise structurally the same as a given metric space will only differ on

how many distinct indistinguishable points there are and the distribution of the distinct topologically distinguishable points. This could be as minimal of a difference from the corresponding metric space as there being exactly two points in a merely pseudometric structure that are topologically indistinguishable to all of the points being topologically indistinguishable from some other distinct points. Some pseudometric spaces may uniformly increase the topologically indistinguishable points, so that for each distinguishable point in the metric space, there are two or three or four or more indistinguishable points in the merely pseudometric space. Or, the increase could be nonuniform. Nevertheless, each of these merely pseudometric spaces can be converted into metric spaces by treating the pluralities, or fusions, or sets of distinct topologically indistinguishable points in a merely pseudometric space as single points in a metric space.

To see this, let X be a merely pseudometric space. Let $x \sim y$ just in case $d(x, y) = 0$ (i.e., just in case x and y are topologically indistinguishable in X). So any points stand in the equivalence relation ‘ \sim ’ if they are zero distance from each other according to the distance function, d , defined on X . We can then define a new space X^* where $X^* = X / \sim$. In the new space, X^* , each of the points are equivalence classes of points in X , represented as $[x]$, $[y]$. We define a distance function $d^*: X / \sim \times X / \sim \rightarrow \mathbb{R}_+$ such that $d^*([x], [y]) = d(x, y)$. We can see that d^* is a metric and X^* is a metric space. For, we already know that d^* will satisfy D1*, D2, and D3 of the definition of a metric above, and, further, because $x \sim y$ if and only if $d(x, y) = 0$, then $d^*([x], [y]) = 0$ if and only if $[x] = [y]$. So D1 will be satisfied. The space X^* is called the *metric identification* of X .⁸

Through metric identification, it seems like any theory that is cast in terms of a metric structure could be cast in terms of a merely pseudometric structure. Where the metric theory has simple, singular, and distinguishable points filling the roles of the point-sized regions, the merely pseudometric theory will have pluralities of distinct indistinguishable points or their fusions filling these roles. Further, no matter which way the world turned out it seems we would be none the wiser. The pluralities of distinct indistinguishable points in the pseudometric version of the theory will do the same work in the theory’s predictions as will the single distinguishable points in the metric version of the theory: same predictive work, same amount of confirmation. If this is right, then there is an important part of the world’s geometric structure we will remain forever ignorant of.

Now, I imagine that one might want to object that we would have no reason to posit the extra indistinguishable points that the pseudometric version of the theory does. This is because simplicity dictates that we should accept the simpler of the two versions of the theory. Because the pseudometric version

8. For a more thoroughly spelled out version of this proof, see Simon (2015, 3–4).

of the theory makes unnecessary posits, then we should prefer the metric version of the theory. I do not find this objection compelling. We are interested in what we can know. If the sense of ‘prefer’ here has to do with knowledge, then the objector has to tell us how we could know that the world is simpler in this way. But, this is just what I have argued we could not do. Perhaps the objector might say that we could, in principle, build some detection device that could detect whether indistinguishable points or regions were present. Assume that one could build such a device. This device would have to operate based off of some sort of *causal connection* with the distinct indistinguishable regions that allowed it to detect when multiple regions take the same position in space-time. Even if this were possible, this would still leave undetermined important facts about the world’s geometric structure. Any theory, \mathcal{T} , by which our detection device would work, would have to spell out what the causal conditions were whereby it would be able to detect the presence of multiple indistinguishable points. Note that theory \mathcal{T} will only distinguish topologically distinguishable points by the causal role that they play. So we only come to know and identify the points by the causal role they play. Now, imagine a different theory, \mathcal{T}^* , which is identical to \mathcal{T} except in the following regard. Instead of having unique points fill the causal roles that allow us to detect the presence of distinct topologically indistinguishable points (as is the case with \mathcal{T}), \mathcal{T}^* has pairs of topologically indistinguishable points fill that role. Our detection device would operate in much the same way, and would be able to detect some instances of distinct topologically indistinguishable regions, but it would be none the wiser as to whether it was in a \mathcal{T} world or a \mathcal{T}^* world. The thrust of the idea here is that if we have a theory that makes some claim about the points and how they are distinguished, we can replace it with a theory where pluralities or complexes of points of whatever number are playing those exact same roles. Because of this we will forever remain unable to know important features of our world’s geometric structure.

It is important to notice that this argument takes seriously the idea that the spatiotemporal structure of the world includes something like points. How seriously must we take the existence of points to get Structural Humility off of the ground? Not very, I think. There are three major contenders in the debate over the nature of space-time: substantivalism, ontic-structural realism (‘structuralism’ henceforth), and relationalism. None escape Structural Humility. Let me briefly explain why. Substantivalists of all stripes take the world’s space-time to be a fundamental, independent thing. This means the substantivalist takes regions and the space-time structure as fundamental. Substantivalists will agree that space-time is made up of points connected in a structure of spatiotemporal relations. Since points are genuine objects according to the space-time substantivalist, the world structures that are strictly pseudometric will be understood in terms of real, physical, distinct topologically indistinguishable points, and the threat of Structural Humility

will loom. Structuralists, however, do not take points very seriously at all. For them, the spatiotemporal structure is fundamental, and the points are, at best, placeholders in the structure lacking intrinsic natures and, at worst, just places or intersections in the series of relations that constitute the world's spatiotemporal structure.⁹ However, structuralists still have to worry about Structural Humility. Roughly, the structuralist maintains the relational structure posited by the substantialist but loses the points (see, e.g., Esfeld and Lam 2008, 42–43). So a world with a pseudometric structure, for the structuralist, will have distinct indistinguishable places within its structure. How many of these there are, or how they are distributed will remain forever unknown to us. Finally, the relationalist takes the world's spatiotemporal structure to be dependent on the material objects and the fundamental spatiotemporal relations they stand in. For the relationalist the problem arises when we have colocated material objects that are constantly adjoined throughout their existence.

4. Concluding Thoughts: Structuralism and Humility. So far we have reviewed how Lewis argued for our irremediable ignorance of the identities of many of the properties in the world, and I have argued that a similar Humility Thesis about the geometric structure of the world can be seen to follow from some important ontologies of space-time. The worry was that we are irremediably ignorant of the existence and distribution of distinct indistinguishable regions. This kind of Humility afflicted all three major metaphysical theories of space-time. Before closing the article I would like to briefly note how Structural Humility relates to a kind of strategy that has been used to motivate structuralism.

Structuralism about space-time is of a piece with a broader ontic structural realist project that seeks to downplay the importance of objects and inflate the importance of structure. Structure is generally treated as being fundamental, and objects are taken to be eliminated, reduced to, grounded in, or dependent on fundamental structure.¹⁰ One important motivation for structuralism is the following kind of consideration:

Epistemological-Ontological Coherence (EOC) Our metaphysics should be coherent with our epistemology. Metaphysics that posit entities that lead

9. See Esfeld and Lam (2008) for an overview about ontic structural realism and a defense of a moderate structuralism about space-time.

10. See Frigg and Votsis (2011) for a wonderful overview of the varieties of ontic structural realism. French (1998) and Ladyman (1998), depending on how they are read, can be seen as advocating either an eliminative or reductionist approach. McKenzie (2020) provides a grounding-based understanding of ontic structural realism. And Esfeld and Lam (2008) and McKenzie (2013) offer versions of structuralism in which the relation between objects and structures should be understood in terms of dependence that is not grounding.

to unknowable gaps between our metaphysics and epistemology should be done away with. We should not deny ourselves in principle epistemic access portions of (physical) reality. Only structuralism avoids a metaphysics that entails epistemic gaps.¹¹

Other motivations for structuralisms in various areas of ontology exploit similar considerations.¹² Motivations, like EOC, can just be seen as denials of a particular Humility Thesis. In the case of EOC the denial of Humility is broad and global. So, if this kind of motivation for structuralism holds water, then structuralism better be able to avoid Humility Theses of any variety. However, if what I have said above is right, then structuralism cannot avoid Humility across the board—it runs into Structural Humility. As such, considerations about Structural Humility undercut one important motivation for the ontic structural realist project.

REFERENCES

- Bricker, Phillip. 1991. "Plenitude of Possible Structures." *Journal of Philosophy* 88 (11): 607–19.
- . 2020. *Modal Matters: Essays in Metaphysics*. Oxford: Oxford University Press.
- Esfeld, Michael. 2004. "Quantum Entanglement and a Metaphysics of Relations." *Studies in History and Philosophy of Science B* 35 (4): 601–17.
- Esfeld, Michael, and Vincent Lam. 2008. "Moderate Structural Realism about Space-Time." *Synthese* 160 (1): 27–46.
- French, Steven. 1998. "On the Withering Away of Physical Objects." In *Interpreting Bodies: Classical and Quantum Objects in Modern Physics*, ed. Elena Castellani, 93–113. Princeton, NJ: Princeton University Press.
- Frigg, Roman, and Ionnis Votsis. 2011. "Everything You Always Wanted to Know about Structural Realism but Were Afraid to Ask." *European Journal for Philosophy of Science* 1 (2): 227–76.
- Jantzen, Benjamin C. 2011. "No Two Entities without Identity." *Synthese* 181 (3): 433–50.
- Ladyman, James. 1998. "What Is Structural Realism?" *Studies in History and Philosophy of Science A* 29 (3): 409–24.
- Lewis, David K. 1983. "New Work for a Theory of Universals." *Australasian Journal of Philosophy* 61 (4): 343–77.
- . 1986. *On the Plurality of Worlds*. Oxford: Blackwell.
- . 2009. "Ramseyan Humility." In *Conceptual Analysis and Philosophical Naturalism*, ed. David Braddon-Mitchell and Robert Nola, 203–22. Cambridge, MA: MIT Press.
- McKenzie, Kerry. 2013. "Priority and Particle Physics: Ontic Structural Realism as a Fundamentality Thesis." *British Journal for the Philosophy of Science* 65 (2): 353–80.
- . 2020. "Structuralism in the Idiom of Determination." *British Journal for the Philosophy of Science* 71 (2): 497–522.
- Simon, Barry. 2015. *A Comprehensive Course in Analysis*. Providence, RI: American Mathematical Society.

11. This formulation roughly follows Esfeld and Lam (2008, 30). See also Esfeld (2004, 614–16).

12. See, e.g., Jantzen's (2011, 435–39) discussion of how standard or naive realism falls prey to worries about making our physical theories incomplete while structuralism avoids this problem.