Coupling the normative regulation with the constitutive state management in Situated Artificial Institutions

MAIQUEL DE BRITO¹, JOMI FRED HÜBNER², and OLIVIER BOISSIER³

¹Federal University of Santa Catarina, Blumenau, SC, Brazil
 e-mail: maiquel.b@ufsc.br
 ²Federal University of Santa Catarina, Florianópolis, SC, Brazil
 e-mail: jomi.hubner@ufsc.br
 ³MINES Saint-Etienne, CNRS Lab, Hubert Curien UMR 5516, University of Lyon Saint-Etienne, France
 e-mail: Olivier.Boissier@emse.fr

Abstract

Artificial Institutions are systems where the regulation defined through norms is based on an interpretation of the concrete world where the agents are situated and interact. Such interpretation can be defined through constitutive rules. The literature proposes independent approaches for the definition and management of both norms and constitutive rules. However, they are usually either not coupled or coupled in an ad hoc and limiting solution. This paper investigates how to make such a coupling. The main contribution of this paper is a formal model basing the regulation provided by the norms on the institutional interpretation of the world provided by constitutive rules. This contribution is based on the Situated Artificial Institutions model that proposes an integrated model of constitutive rules based on *status functions*.

1 Introduction

Multi-Agent Systems (MAS) are the systems where autonomous, goal-oriented artificial entities—the *agents*—participate in. This paper focuses on *open* MAS, which are systems where the number of agents is unpredictable, as well as their local and interaction behaviours (Piunti, 2009). For these reasons, it is necessary to regulate the agents' behaviour to conciliate their autonomy with the overall systems' expectations (Moses & Tennenholtz, 1995; Castelfranchi, 2000; Fasli, 2004). This paper refers to the element that provides such regulation in MAS as *artificial institution*, or simply *institution*. Such regulation is usually expressed through regulative norms (henceforth referred just as *norms*) based on deontic concepts such as obligations, prohibitions, and permissions. Institutions are often viewed as systems where the norms perform their regulative tasks based on an interpretation (also referred in the literature as *constitution* or *classification*) of the concrete world (or the *environment*) where the agents are immersed (Searle, 1995; Balke *et al.*, 2013). Thus, for example, in an auction scenario, norms regulate *payments* and *bids* rather than exchanges of paper bills or raising hands. Constitution is usually specified through *constitutive rules* that specify, for example, that the raising of hands counts as a bid in the context of an auction.

Institutions have thus (i) a *constitutive state*, which is the institutional interpretation of the current state of the world, according to what is specified by the constitutive rules, and (ii) a *normative state*, which is the institutional state regarding the expected behaviour of the agents, according to what is specified by the norms. Basing the management of the normative state (i.e. defining norm activations, violations, fulfilments, etc.) on the constitutive state is a key issue in MAS institutions (Boella & van der Torre, 2004; Broersen *et al.*, 2013). Norms and constitutive rules may be combined in a single conceptual model, as proposed, for instance, by Boella and van der Torre (2006b), being then jointly managed. In a different direction, some approaches consider that norms and constitutive rules have particular, independent

models and management. This is the case of the Situated Artificial Institution (SAI) approach that defines representations and dynamics for the constitutive state (de Brito *et al.*, 2014, 2015a, 2018), but is not limited to a particular normative model. On the contrary, it assumes that norms, independent of the model they follow, provide the regulation based on a unified representation of constitutive state. This constitutive state is composed of a rich and integrated set of constituted *status functions*, which are status (or classifications), with corresponding functions, assigned by the institution to the environmental elements (Searle, 1995, 2009), covering the whole set of abstractions participating in the functioning of the environment: agents acting, events occurring, and states holding. For example, in an auction scenario, (i) an agent may carry the status and perform the function of *auctioneer*, (ii) the occurrence of an utterance may be an event that carries the status and performs the function of *bid*, and (iii) a number of agents dwelling in the system may be a state that carries the status and performs the function of *minimum quorum*.

Basing norms on status functions makes the regulation (i) consistent with the environment under regulation even abstracting from it and (ii) flexible since norms following different models share the same interpretation of the environmental state (de Brito et al., 2018). However, coupling the management of the normative regulation with a constitutive state composed of constituted status functions, with their particular semantics and dynamics, requires to conceive how the environmental elements of different natures, abstracted under the notion of constituted status functions, are taken into account in the normative management. For example, considering the norm 'a bidder is obliged to bid', it is necessary to define (i) how to monitor the norm taking into account every agent considered as bidder, (ii) how to proceed when these agents are no longer considered as bidders (are the obligations kept or revoked?), and (iii) how to verify its compliance when many actions are considered as a bid (is the norm compliance conditioned to the performance of all of these actions or of at least one of them?). This paper addresses such coupling, extending and deepening the initial discussion presented in de Brito et al. (2015b). As the main contribution, we define an approach and a formal apparatus to monitor and reason about the norms coupled with a constitutive state composed of constituted status functions. Since it is not possible to investigate the coupling with each existing normative formalism, this paper addresses the coupling with the normative model proposed by Panagiotidi et al. (2013), which formalizes the deontic aspects of norms and defines the operational semantics for their monitoring.

This paper is organized as follows: Sections 2 and 3 describe, respectively, the considered normative and constitutive models. While Section 4 describes how normative and constitutive *representations* are coupled, Section 5 presents our approach to couple the normative and constitutive *dynamics*. This approach is illustrated in Section 6, discussed in Section 7, and compared with some related works in Section 8, which includes some conclusions and perspectives.

2 Normative model

This section briefly describes the model of Panagiotidi *et al.* (2013), firstly defining norms that compose a normative specification and then defining norm instances (i.e. norms enacted in the real world) and their dynamics. The focus is on the essential elements to our proposed coupling. More details about this normative model can be found in Panagiotidi *et al.* (2013).

2.1 Normative specification

DEFINITION 1 (Norm). A norm *n* is a tuple $n = \langle \alpha, c_a, c_m, c_d, c_r, c_t \rangle$, where (*i*) α is the agent obliged to comply with the norm, (*ii*) c_a is the **a**ctivation condition of the norm, (*iii*) c_m is the **m**aintenance condition, (*iv*) c_d is the **d**eactivation condition, (*v*) c_r is the **r**epair condition, and (*vi*) c_t is the **t**imeout condition. The set of all norms of an institution, noted by \mathcal{N} , is called a normative specification.

Elements of norms are expressed in first-order predicate language. The element α is either a constant referring to an agent identifier or a variable that, when grounded, refers to an agent identifier. The remainder *c* elements are expressed through formulae that may include the connectives $\{\neg, \land, \lor\}$. Informally, a norm expresses that if, at some point, c_a holds, then the agent α is obliged to see to it that c_m is maintained



Figure 1 Life cycle of norm instances, s.t. g(p) is the event of some condition p becoming true (based on Panagiotidi *et al.*, 2013)

at least until c_d holds; otherwise, α is obliged to see to it that c_r holds before the timeout c_t . For example, the norm

$$\langle Ag, driving(Ag), \neg cross red(Ag, LightID), \neg driving(Ag), fine paid(Value), time(500) \rangle$$

expresses that when an agent Ag is driving, he is obliged to not cross the red traffic light LightID until he is not driving; otherwise it has to pay Value before the time 500. Terms starting with uppercase letters are variables that are implicitly universally quantified.

2.2 Normative dynamics

The agents follow norm instances (López y López & Luck, 2003) that are a copy of the specified norms (possibly grounding existing variables). Many instances of the same norm can exist. For example, the norm '*Buyers are obliged to Pay*' could produce the instances '*bob is obliged to transfer(\$100)*' and '*tom is obliged to deposit(\$50)*'. This section defines how the instances of norms proposed by Panagiotidi *et al.* (2013) are represented, and how these instances compose the normative state of an institution.

DEFINITION 2 (Norm instance). Given a norm n and a substitution of variables θ_i^{\dagger} a norm instance is represented by $n' = \langle \alpha', c'_a, c'_m, c'_d, c'_r, c'_t \rangle$ s.t $\alpha' = \alpha \theta$ is an agent identifier, $c'_a = c_a \theta$, $c'_m = c_m \theta$, $c'_d = c_d \theta$, $c'_r = c_r \theta$, and $c'_t = c_t \theta$ s.t. α , c'_a and c'_t are fully grounded while c'_m , c'_r , and c'_d may be fully or partially grounded.

DEFINITION 3 (Normative state). The normative state of the institution is a set of norm instances $N = AS \cup VS \cup DS \cup FS$ s.t. (i) AS is the set of active instances, (ii) VS is the set of violated instances, (iii) DS is the set of deactivated instances, and (iv) FS is the set of failed instances.²

As shown in Figure 1, a norm instance n' is activated as soon as its activation condition c'_a is satisfied, getting then into AS, creating an obligation for the agent a'. The obligation is fulfilled when the deactivation condition c'_a is satisfied, becoming then deactivated (DS). Active norm instances become violated (VS) when the maintenance condition c'_m is no longer satisfied. Panagiotidi *et al.* (2013) consider that violations can be repaired before the timeout c'_t . If a norm instance is violated, either (i) satisfying its reparation condition c'_r leads it to deactivated state (DS) or (ii) the occurrence of the timeout condition c'_t leads it to the failure state (FS), when misbehaviours can no longer be repaired.

The predicates *active*, *viol*, *deactivated*, and *failed* are defined to check a norm instance with respect to the normative state N as follows:

$$N \models active(n') \text{ iff } n' \in AS \tag{1}$$

$$N \models viol(n') \text{ iff } n' \in VS \tag{2}$$

¹ In this paper, a *substitution* is always represented by θ . A *substitution* is a finite set of pairs $\{\alpha_1/\beta_1, \dots, \alpha_n/\beta_n\}$ where α_i is a variable and β_i is a term. If ρ is a literal, then $\rho\theta$ is the literal resulting from the replacement of each α_i in ρ by the corresponding β_i . If $P = \{\rho_1, \dots, \rho_n\}$ is a set of literals, then $P\theta = \{\rho_1\theta, \dots, \rho_n\theta\}$ (Brachman & Levesque, 2004).

² In this paper, sets identified by calligraphic letters (e.g. N) refer to the specification of the system, while sets identified by non-calligraphic letters (e.g. N) refer to the system execution.

M. DE BRITO, J. F. HÜBNER AND O. BOISSIER

$$N \models deactivated(n') \text{ iff } n' \in DS \tag{3}$$

$$N \models failed(n') \text{ iff } n' \in FS \tag{4}$$

A normative monitor is the element responsible for checking the current normative state with respect to the current world under regulation. In Panagiotidi *et al.* (2013), a *normative monitor* is defined as a tuple $M_N = \langle \mathcal{N}, AS, VS, DS, FS, s \rangle$ where (i) \mathcal{N} is the set of considered norms, (ii) AS, VS, DS, and FS are the sets of active, violated, deactivated, and failed norm instances, and (iii) *s* indexes the current state of the normative monitor. The transition system for a normative monitor M_N is $TS_{M_N} = \langle \Gamma_{M_N}, \rhd \rangle$, where Γ_{M_N} is the set of all possible configurations of the normative monitor and $\rhd \subseteq \Gamma_{M_N} \times \Gamma_{M_N}$ is a transition relation between configurations. The operational semantics of the normative monitor follows the transition rules (5)–(9).

$$\frac{\langle \alpha, c_a, c_m, c_d, c_r, c_t \rangle \in \mathcal{N} \quad c_a \theta \quad \neg c_d \theta}{M_N \rhd \langle \mathcal{N}, AS \cup \langle \alpha', c_a \theta, c_m \theta, c_d \theta, c_r \theta, c_t \theta \rangle, VS, DS, FS, s_{i+1} \rangle}$$
(5)

$$\frac{n' = \langle \alpha', c'_a, c'_m, c'_d, c'_r, c'_l \rangle \quad n' \in AS \quad \neg c'_m}{M_N \rhd \langle \mathcal{N}, AS \setminus n', VS \cup n', DS, FS, s_{i+1} \rangle}$$
(6)

$$\frac{n' = \langle \alpha', c'_a, c'_m, c'_d, c'_r, c'_l \rangle \quad n' \in AS \quad c'_d}{M_N \rhd \langle \mathcal{N}, AS \setminus n', VS, DS \cup n', FS, s_{i+1} \rangle}$$
(7)

$$\frac{n' = \langle \alpha', c'_a, c'_m, c'_d, c'_r, c'_i \rangle \qquad n' \in VS \qquad c'_r}{M_N \rhd \langle \mathcal{N}, AS, VS \setminus n', DS \cup n', FS, s_{i+1} \rangle}$$
(8)

$$\frac{n' = \langle \alpha', c'_a, c'_m, c'_d, c'_r, c'_t \rangle \qquad n' \in VS \qquad c'_t}{M_N \rhd \langle \mathcal{N}, AS, VS \setminus n', DS, FS \cup n', s_{i+1} \rangle}$$
(9)

The sets \mathcal{N} , AS, VS, DS, and FS are those of the M_N . Under a closed world assumption, the conditions c_a , c_d , c'_m , c'_d , c'_r , and c'_t are evaluated against the state of the world to manage the normative state N as illustrated in Figure 1. For example, by the transition rule (5), if the state of the world satisfies the activation condition but does not satisfy the deactivation condition of a norm—both under a substitution θ —then the monitor adds a norm instance $n' = \langle \alpha', c_a \theta, c_m \theta, c_d \theta, c_r \theta, c_t \theta \rangle$ into the set AS. Variables in partially grounded conditions are implicitly universally quantified (Brachman & Levesque, 2004).

3 Constitutive model

The SAI model (de Brito *et al.*, 2018), inspired by the theory of John Searle (1995, 2009), considers that, in artificial institutions, the regulation is specified using abstract concepts that do not refer directly to the environment under regulation. For example, the norm '*the winner of an auction is obliged to pay its offer*' makes sense in the institutional specification of an auction. The norm, however, does not specify (i) what an agent should do to become the *winner* of the auction or (ii) what an agent must do to perform the *payment*. In this scenario, *winner* and *payment* are *status functions*: they are status, assigned by the institution to the environmental elements, which impose functions to these elements.³ SAI considers that status functions are assigned to agents acting, events occurring, and states holding in the environment. For example, in an auction, an agent may have the agent-status function of *winner*, the utterance 'I offer \$100' may have the event-status function of *bid*, and 'more than 20 people placed in a room at Friday 10am' may have the state-status function of *minimum quorum* for its realization.

The constitution of status functions, that is, their assignment to the environmental elements, produces the *constitutive state*, which is the institutional interpretation about the environmental state. In SAI, the

³ In SAI, as in Searle's work, the expression '*status function*' means both the *status* and the corresponding *function* assigned by the institution to the environmental elements. For example, the agent *bob* carrying the status function *bidder* means that *bob* has both the status and the functions of such status.



Figure 2 Example of constitution process. In the current environmental state, agents are uttering numbers and are also typing numbers in electronic devices. In the constitutive state, these actions count as bids, and the agent that places the highest bid counts as the winner of the auction, that, according to the normative state, becomes obliged to pay the offer. This obligation can be fulfilled through a money transfer, which, according to a constitutive rule, counts as a payment

dynamics of the normative state (i.e. the activation, fulfilment, violation, etc. of the norms) is based on the constitutive state. For example, the norm 'the winner of the auction is obliged to pay its offer' is activated when an agent acting in the environment is considered by the institution as carrying the winner status function. The same norm is fulfilled when that agent produces in the environment an event considered by the institution as carrying a payment status function (Figure 2). This section presents the essential background on SAI to base the contribution of this paper. Further details and examples on SAI can be found in de Brito *et al.* (2018) among others. In the following, Section 3.1 describes how the constitution of status functions is specified in SAI, and Section 3.2 describes the dynamics of such constitution.

3.1 Constitutive specification

The constitutive specification defines, through constitutive rules, how the elements that *may* be part of the environment, defined below, are considered from the institutional perspective. This section defines constitutive rules according to the SAI model, starting by the elements which they refer to (the environmental elements) and then presenting the elements that are constituted from the environment (the status functions).⁴

DEFINITION 4 (Environmental elements). The environmental elements of interest in SAI are represented by $\mathcal{X} = \mathcal{A}_{\mathcal{X}} \cup \mathcal{E}_{\mathcal{X}} \cup \mathcal{S}_{\mathcal{X}}$, where $\mathcal{A}_{\mathcal{X}}$ is the set of agents possibly acting in the system, $\mathcal{E}_{\mathcal{X}}$ is the set of events that may happen in the environment, and $\mathcal{S}_{\mathcal{X}}$ is the set of properties used to describe the possible states of the environment.

⁴ The presented formalism employs some elements of the first-order logic language, including (i) *constants* that refer to elements existing in the modelled world, (ii) *variables*, (iii) possibly not grounded atomic formulae that represent *predicates*, and (iv) *substitutions* of variables (Brachman & Levesque, 2004).

Agents $a_{\mathcal{X}} \in \mathcal{A}_{\mathcal{X}}$ are represented by constants (e.g. *bob*). Events $e_{\mathcal{X}} \in \mathcal{E}_{\mathcal{X}}$ are pairs (e, a) s.t. e is a firstorder logic predicate identifying the event with its arguments and a is (i) either a constant identifying the agent that has triggered the event or (ii) ε if the event is produced by the environment itself (e.g. a clock tick). Properties $s_{\mathcal{X}} \in \mathcal{S}_{\mathcal{X}}$ are represented by first-order logic predicates. It is important to remark that the set \mathcal{X} is just a *representation* of the elements that potentially take part in the environment.⁵ For example, when a SAI specification contains an event $e_{\mathcal{X}} \in \mathcal{E}_{\mathcal{X}}$, it does not mean that $e_{\mathcal{X}}$ has happened in the environment. Rather, it means that the designer of the institution assumes that $e_{\mathcal{X}}$ may happen.

DEFINITION 5 (Status function). Status functions are functions that the institution assigns to the environmental elements. The status functions of a SAI are represented by $\mathcal{F} = \mathcal{A}_{\mathcal{F}} \cup \mathcal{E}_{\mathcal{F}} \cup \mathcal{S}_{\mathcal{F}}$, where $\mathcal{A}_{\mathcal{F}}$ is the set of agent-status functions (i.e. status functions assignable to agents $a_{\mathcal{X}} \in A_{\mathcal{X}}$), $\mathcal{E}_{\mathcal{F}}$ is the set of eventstatus functions (i.e. status functions assignable to events $e_{\mathcal{X}} \in E_{\mathcal{X}}$), and $\mathcal{S}_{\mathcal{F}}$ is the set of state-status functions (i.e. status functions assignable to states $s_{\mathcal{X}} \in S_{\mathcal{X}}$).

Agent-status functions are represented by constants. Event- and state-status functions are represented by first-order logic predicates. The assignment of status functions of \mathcal{F} to the environment elements of \mathcal{X} is specified through *constitutive rules*.

DEFINITION 6 (Constitutive rule). The set of all constitutive rules of a SAI is represented by C. A constitutive rule $c \in C$ is a tuple $\langle x, y, t, m \rangle$ meaning that $x \in \mathcal{F} \cup \mathcal{X} \cup Var \cup \{\varepsilon\}$ counts as (i.e. x has the status function) $y \in \mathcal{F}$ when the event $t \in \mathcal{E}_{\mathcal{F}} \cup \mathcal{E}_{\mathcal{X}} \cup \{\varepsilon\}$ has happened and while the condition represented by m holds.⁶

A constitutive rule where $x = \varepsilon$ specifies a *freestanding assignment* of the status function y, that is, an assignment where there is no concrete environmental element carrying y (Searle, 2009; de Brito *et al.*, 2018). In the case of $t = \varepsilon \land m = \top$, the constitutive rule is simply read as x count-as y since y is assigned to x in any circumstance. The element x may be a variable $var \in Var$ that is substituted by an element belonging either to \mathcal{F} or to \mathcal{X} when the constitutive rule is interpreted. When x actually counts as y (i.e. when the conditions t and m declared in the constitutive rule are true), we say that there is a *status function assignment* (SFA) of the status function y to the element x. The establishment of a SFA of y to some x is the *constitution* of y.

According to Definition 6, the constitution of status functions is conditioned by m. The following BNF grammar defines all the well-formed formulae for m (hereafter *m*-formulae)⁷

$$m ::= s_{\mathcal{X}} | e_{\mathcal{X}} | s_{\mathcal{F}} | e_{\mathcal{F}} | \neg m | m \lor m | m \land m | \bot | \top |$$
$$(a_{\mathcal{X}} | Var) " is" (a_{\mathcal{F}} | Var) | (e_{\mathcal{X}} | Var) " is" (e_{\mathcal{F}} | Var) | (s_{\mathcal{X}} | Var) " is" (s_{\mathcal{F}} | Var)$$

The semantics of the m-formulae is given in Section 3.2 as it depends on the environmental and constitutive states that are also defined in that section.

3.2 Constitutive dynamics

Status functions are dynamically assigned to the actual environmental elements by the interpretation of constitutive rules. This section introduces the elements that are relevant to coupling this dynamics with the normative one.

6

⁵ It is beyond the scope of this paper to present in detail the environment. We just consider the elements of \mathcal{X} as existing outside the institution, being available thanks to reliable interfaces.

⁶ ε represents that the element is not present in the constitutive rule. *Var*, in this paper, represents the whole set of variables that can be used in a constitutive rule. Under a substitution θ , variables $var \in Var$ are substituted by terms. ⁷ The symbols \neg , \lor , and \land represent, respectively, negation, disjunction, and conjunction, with the usual semantics

The symbols \neg , \lor , and \land represent, respectively, negation, disjunction, and conjunction, with the usual semantics of propositional logic.



Figure 3 Example of constitutive state changes along time. At some moment, while a state *m* holds, an event *t* happens (cf. the first arrow in the bottom of the picture). By the constitutive rule x count-as y when t while m ($\langle x, y, t, m \rangle \in C$), such conditions lead the environmental element *x* to count as *y* in the constitutive state (cf. the dashed line). Then, the event *t'* occurs while the state *m'* holds. By the constitutive rule y count-as y' when t' while m', the element that counts as *y* (i.e. *x*) counts also as *y'* (cf. the dotted horizontal line). When the state *m* ceases to hold, the conditions to *x* count as *y* also cease to hold, and as *x* is no longer counting as *y*, it also ceases to count *y'*. For example, if x = bob, y = bidder, and $y' = auction_participant$, s.t. $bob \in A_X$ and $\{bidder, auction_participant\} \subseteq A_F$, then bob counts as (i) bidder from *t* and (ii) auction_participant from *t'*

DEFINITION 7 (Environmental state). The actual environmental state is represented by $X = A_X \cup E_X \cup S_X$, where (i) A_X is the set of agents participating in the system, (ii) E_X is the set of events occurring in the environment, and (iii) S_X is the set of environmental properties describing the environmental state.

Agents $a_X \in A_X$ are represented by constants referring to their identifiers. States $s_X \in S_X$ are represented by atomic formulae. Events $e_X \in E_X$ are represented by pairs (e, a) where e is the event, represented by an atomic formulae, triggered by the agent a. Events can be triggered by actions of the agents (e.g. the utterance of a bid in an auction) but can also be produced by the environment itself (e.g. a clock tick). In this case, events are represented by pairs (e, ε) .

DEFINITION 8 (Constitutive state). The constitutive state of a SAI is the set of the existing SFAs. It is represented by $F = A_F \cup E_F \cup S_F$, where (i) $A_F \subseteq A_X \times A_F$ is the set of agent-SFAs, (ii) $E_F \subseteq E_X \times \mathcal{E}_F \times A_X \cup \{\varepsilon\}$ is the set of event-SFAs, and (iii) $S_F \subseteq S_X \cup \{\varepsilon\} \times S_F$ is the set of state-SFAs.

Elements of *F* are *SFAs*, that is, relations between environmental elements and status functions. Elements of A_F are pairs $\langle a_X, a_F \rangle$ meaning that the agent a_X has the status function a_F . Elements of E_F are triples $\langle e_X, e_F, a_X \rangle$ meaning that the event-status function e_F is assigned to the event e_X produced by the agent a_X .⁸ Elements of S_F are pairs $\langle s_X, s_F \rangle$ meaning that the state s_X carries the status function s_F . The process of interpretation of constitutive rules that builds the constitutive state is detailed in de Brito *et al.* (2018). Briefly, if the actual environment holds the elements *t* and *m* of a constitutive rule $\langle x, y, t, m \rangle$, then the environmental element *x* constitutes the status function *y*, producing an SFA. If the environment is no longer holding the condition *m* that maintains an existing SFA, then such SFA is dropped from the constitutive state (as illustrated in Figure 3).

Both the environmental and constitutive states are used to evaluate the *m*-formulae defined in Section 3.1. For a model $M = \langle F, X, \mathcal{F} \rangle$, the semantics of m-formulae is defined as follows:

$$M \models m \text{ iff } \exists \theta : (m\theta \in E_X \lor m\theta \in S_X) \lor$$

$$(\exists (e, a) \in E_X : \langle e, m\theta, a \rangle \in E_F) \lor$$

$$(\exists s_X \in S_X : \langle s_X, m\theta \rangle \in S_F)$$

$$(10)$$

⁸ As events are supposed to be considered at the individual agent level in normative systems (i.e. they can be related to a triggering agent) (De Vos *et al.*, 2013), it is important to record the agent that causes an event-SFA.

M. DE BRITO, J. F. HÜBNER AND O. BOISSIER

```
status_functions :
 agents: mayor, firefighter.
 events: evacuate (Zone).
 states: secure (Zone), insecure (Zone).
constitutive_rules :
              /*** Agent-Status Functions constitutive rules ***/
  /*Actors carry the status functions according to their check in the tables*/
  1: Actor count-as mayor
           when checkin(table_mayor,Actor) while not(Other is mayor)|Other==Actor.
  2: Actor count-as firefighter
           when checkin(table_fire_brigade, Actor).
             /*** Event-Status Functions constitutive rules ***/
  /*Putting a "launch_object" on (2,2) means the evacuation of the downtown*/
  3: put_tangible(launch_object,2,2,Actor) count-as evacuate(downtown).
  /*Sending a message with the proper arguments means the evacuation of the downtown*/
  4: send_message(evacuation, downtown, Actor) count-as evacuate(downtown).
            /*** State-Status Functions constitutive rules ***/
  /*A zone in preventive phase is secure for evacuation procedures
  if it has at most 500 inhabitants*/
  5: security_phase(Zone, preventive) count-as secure(Zone)
           while nb_inhabit(Zone,X)& X<=500</pre>
  /*A zone in emergency phase is insecure for evacuation procedures*/
  6: security_phase(Zone,emergency) count-as insecure(Zone).
```

Figure 4 Example of constitutive specification

$$M \models x \text{ is } y \text{ iff } \exists \theta : (x\theta \in A_X \land y\theta \in \mathcal{A}_F \land \langle x\theta, y\theta \rangle \in A_F) \lor$$

$$(x\theta \in E_X \land x = (e, a) \land y\theta \in \mathcal{E}_F \land \langle e\theta, y\theta, a\theta \rangle \in E_F) \lor$$

$$(x\theta \in S_X \land y\theta \in \mathcal{S}_F \land \langle x\theta, y\theta \rangle \in S_F)$$

$$(11)$$

From the expression (10), an m-formula *m* is satisfied by *M* (i) if it represents either an event actually occurring or a state actually holding in the environment; (ii) if it represents an event-status function assigned to some environmental elements; or (iii) if it represents a state-status function assigned to some environmental state. From the expression (11), an m-formula is satisfied by *M* if it has the form *x* is *y* and if, under a substitution θ , either (i) $x\theta$ is the identifier of an agent that carries the agent-status function $y\theta$ or (ii) $x\theta$ identifies an event that actually carries the event-status function $y\theta$ or (iii) $x\theta$ identifies a state that actually carries the state-status function $y\theta$. As usual, $M \models \top$ and $M \not\models \bot$.

3.3 Example of SAI constitutive specification

Based on the described constitutive model, a language to specify the constitution of status functions is proposed in de Brito et al. (2018). In that language, the symbols "not", "|", "&", "false", and "true" correspond respectively to \neg , \lor , \land , \bot , and \top in the m-formulae. Figure 4 shows the constitutive specification for a use case where agents collaborate to manage crisis such as flooding and car crashes in zones that may be either *insecure* (only professional people intervene) or secure (admits unprofessional intervention) (de Brito et al., 2015c). Norms regulate the collaboration (e.g. firefighters are obliged to evacuate insecure zones). The environment is composed of geographic information systems (GIS) and of tangible tables (Kubicki et al., 2012), where the agents put objects equipped with RFID tags on to signal their intended actions. The relevant information provided by the GIS are security-phase(Zone, Phase), when a Zone is in a specific Phase of the crisis management, and nb inhabit (Zone, X) when a Zone has X inhabitants. The event put tangible (Object, X, Y, Agent) is triggered when an Agent puts an Object on the coordinates (X, Y) of a tangible table. The event send message (Content, Zone, Agent) is triggered when an Agent sends a message with some Content with respect to a Zone. The actions of the agents upon the tables, as well as the information from the GIS, do not have per se any meaning in the crisis scenario and, thus, they cannot ground, by themselves, the checking of the norm compliance. For instance, an agent putting an object on a specific point of the table does not mean, by itself, a command for the evacuation of a zone. Such action becomes meaningful in the crisis scenario through the interpretation of constitutive rules. For example, agents are recognized as mayor and firefighter according to the table

8

 $\texttt{1:} \\ \texttt{(mayor, secure(downtown), secure(downtown), evacuate(downtown), } \bot, \neg \texttt{secure(downtown)} \\ \texttt{(mayor, secure(downtown), secure(downtown), evacuate(downtown), } \bot$

 $2: \langle \texttt{firefighter}, \texttt{insecure}(\texttt{downtown}), \texttt{insecure}(\texttt{downtown}), \texttt{evacuate}(\texttt{downtown}), \bot, \neg \texttt{insecure}(\texttt{downtown}) \rangle$

Figure 5 Norms using status functions

where they are acting in (constitutive rules 1 and 2) and putting a *launch_object* on the coordinates (2,2) of a table signals the evacuation of the downtown (constitutive rule 3).

4 Linking normative and constitutive representations

Normative models look to the 'state of the world' to check the agents' expected behaviour. When norms are part of SAI, this 'state of the world' is the constitutive state. Basing the normative regulation on the constitutive state requires to define (i) how the 'world' represented by the constitutive elements is captured by the representations of norms and norm instances and (ii) how the different components of the norms are evaluated considering the different nature of the constituted elements in the different states of the life cycle of the norm instances. The first point is addressed in this section. The second point is addressed in Section 5.

4.1 Representing norms through status functions

Evaluating norms with respect to the constitutive and to the normative state itself requires to define expressions that can be used to evaluate those states. Conditions over the whole constitutive state are expressed through *sf-formulae* $m_{\mathcal{F}} \in M_{\mathcal{F}}$. The sf-formulae are particular cases of the m-formulae whose atomic formulae are either event/state-status functions or expressions of the type *x* is *y*. The syntax of *sf-formulae* is given by the grammar (12) and their semantics follows the expressions (10) and (11).

$$m_{\mathcal{F}} ::= s_{\mathcal{F}} | e_{\mathcal{F}} | \neg m_{\mathcal{F}} | m_{\mathcal{F}} \lor m_{\mathcal{F}} | m_{\mathcal{F}} \land m_{\mathcal{F}} |$$

$$(12)$$

$$(a_{\mathcal{X}} | Var) " is" (a_{\mathcal{F}} | Var) | (e_{\mathcal{X}} | Var) " is" (e_{\mathcal{F}} | Var) | (s_{\mathcal{X}} | Var) " is" (s_{\mathcal{F}} | Var)$$

The sf-formulae can be combined with the predicates *active*, *viol*, *deactivated*, and *failed*, evaluated according to the expressions (1)–(4) in the *n*-formulae $m_N \in M_N$, that follow the grammar (13).

$$m_{N} ::= m_{\mathcal{F}} |active(n')| viol(n')| deactivated(n')| failed(n')|m_{N} \wedge m_{N}|m_{N} \vee m_{N}| \bot | \top$$
(13)

To link the representation of norms presented in Section 2 to the constitutive state presented in Section 3, we need to introduce status functions in the norms. For a norm $n \in \mathcal{N}$, where $n = \langle \alpha, c_a, c_m, c_d, c_r, c_t \rangle$, we define that $\alpha \in \mathcal{A}_F$, $c_a \in M_N$, $c_m \in M_N$, $c_d \in \mathcal{E}_F \cup \mathcal{S}_F$, $c_r \in \mathcal{E}_F \cup \mathcal{S}_F$, and $c_t \in M_N$. The reasons for linking the elements of the norm with these particular types are:

- A norm is directed to agents carrying an agent-status function ($\alpha \in \mathcal{A}_{\mathcal{F}}$) and not to concrete agents.
- Deactivation and repairing conditions are expressed with event- and state-status functions. From the institutional perspective, agents must behave as prescribed by the norms and then produce, in the environment, events and states that can be interpreted as the corresponding event- and state-status functions.
- Activation, maintenance, and timeout refer to the whole constitutive and normative states and, thus, are referred in norms through particular types of formulae.

Figure 5 shows the norms as conceived in Panagiotidi *et al.* (2013) using the status functions defined in the constitutive specification shown in Figure 4 to specify that (i) the *mayor* is obliged to evacuate secure zones and (ii) *firefighters* are obliged to evacuate insecure zones.

4.2 Linking representations of norm instances to the constitutive state

While norms refer to agent-status functions (i.e. $\alpha \in A_F$), their instances prescribe the behaviour of the concrete agents acting in the environment. The obligation of an agent a_X to follow a norm instance n'

is conditioned by its carrying of the status function α as prescribed in the norm *n*. As detailed later in the expressions (15)–(18), to check this condition norm instances must record both the agent to whom the norm is directed and the status function carried by that agent when the instance was created. Thus, the representation of norm instance of Panagiotidi *et al.* (2013) is extended to $n' = \langle (a_X, \alpha), c'_a, c'_m, c'_d, c'_r, c'_t \rangle$, where $a_X \in A_X$ points to the concrete agent targeted by the norm instance and $\alpha \in \mathcal{A}_F$ is the status function carried by that agent when the instance was created. The remainder elements are those from Definition 2. The elements c'_m, c'_d, c'_r may be partially grounded while the remainder ones are fully grounded.

5 Coupling normative and constitutive dynamics

Having defined how normative and constitutive representations are linked, this section explains how the dynamics of the normative and constitutive states are coupled. Section 5.1 explains when, given the constitutive and normative states, norm instances are considered activated, deactivated, violated, and failed. These definitions can be used by the normative monitors that implement the operational semantics of the normative model, as shown in Section 5.2.

5.1 Norm activation, deactivation, violation, and failure

5.1.1 Activation

Given a normative specification N, a constitutive state F, and a normative state N, the set of norm instances to be created is given by the function *activated* defined below:

$$activated(\mathcal{N}, F, N) = \{n' | \exists \theta \exists \langle \alpha, c_a, c_m, c_d, c_r, c_t \rangle \in \mathcal{N} :$$
$$F \cup N \models c_a \theta \land (a_X \text{ is } \alpha \theta) \}$$
(14)
s.t. $n' = \langle (a_X, \alpha \theta), c_a \theta, c_m \theta, c_d \theta, c_r \theta, c_t \theta \rangle$

The creation of norm instances is conditioned by the constitutive and normative states satisfying the activation condition c_a for some substitution θ (i.e. $F \cup N \models c_a \theta$). The evaluation of c_a with respect to N follows the expressions (1)–(4). Its evaluation with respect to F follows the expressions (10) and (11). By the function *activated*, a norm directed to an agent-status function α produces an instance for *every* concrete agent a_X carrying α . For example, considering the constitutive specification in Figure 4, if both agents *bob* and *tom* carry the status function of *firefighter* (i.e. {bob, firefighter}, tom, firefighter} $\subseteq A_F$) and the *downtown* is in emergency phase of crisis, being thus insecure (i.e. $security_phase(downtown, emergency), insecure(downtown)$ } $\in S_F$), then (i) $F \models insecure(downtown)$, (ii) $F \models bob$ is firefighter, and (iii) $F \models tom$ is firefighter. Thus, as illustrated in Figure 6, the following instances of the norm 2 of Figure 5 are created:

 $(bob, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), <math>\bot$, \neg insecure(downtown) $(tom, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), <math>\bot$, \neg insecure(downtown) $(tom, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), <math>\bot$, \neg insecure(downtown) $(tom, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), <math>\bot$, \neg insecure(downtown), insecure(downtown), evacuate(downtown), \bot , \neg insecure(downtown), insecure(downtown),

5.1.2 Deactivation

In the considered normative model, obligations are fulfilled when norm instances are deactivated. Deactivations are considered separately according to the nature of the deactivation condition (event or state). The functions f-deactivated^e and f-deactivated^s deal respectively with deactivations of active instances conditioned by events and by states.

$$f\text{-}deactivated^{e}(F, N) = \{ \langle n' | \exists (e_{X}, a_{X}) \in E_{X} : n' \in AS \land c'_{d} \in \mathcal{E}_{\mathcal{F}} \land$$
$$F \models ((e_{X}, a_{X}) \text{ is } c'_{d} \lor \neg (a_{X} \text{ is } \alpha)) \land F \cup N \models c'_{m} \}$$
(15)



Figure 6 Example of norm activation. The normative specification contains a norm stating that when the downtown is insecure, firefighters are obliged to evacuate it (cf. Figure 5). The environment is in a state that counts as the downtown being insecure in the constitutive state. The holding of such condition in the constitutive state produces an instance of that norm for each agent counting as firefighter

$$f\text{-deactivated}^{s}(F, N) = \{ \langle n' | n' \in AS \land c'_{d} \in \mathcal{S}_{\mathcal{F}} \land$$

$$F \models (c'_{d} \lor \neg (a_{X} \operatorname{is} \alpha)) \land F \cup N \models c'_{m} \}$$

$$\text{s.t.} \quad n' = \langle (a_{X}, \alpha), c'_{a}, c'_{m}, c'_{d}, c'_{r}, c'_{t} \rangle$$

$$(16)$$

The function *f*-deactivated^e captures the notion of events as being considered at the individual agent level. The obligation of an agent a_X with respect to the occurrence in the environment of an event that counts as the event-status function c'_d is only fulfilled when c'_d is assigned to an event e_X really produced by the agent a_X . This is expressed by the element $F \models ((e_X, a_X) \text{ is } c'_d)$, evaluated according to the Expression (11). For instance, if two agents are obliged to produce an event that counts as the event-status function evacuate(downtown), then every obliged agent must produce such an event (Figure 7).

By the function *f*-deactivated^s, an agent fulfils an obligation to achieve a state when it sees to it that such state holds, no matter by whom it has been produced. This achievement is detected when there is an assignment to the state-status function c'_d , evaluated according to the Expression (10). For example, if two agents are obliged to see to them that the environment is in a state that counts as the downtown being evacuated, then the obligations of all the agents are fulfilled when such a state is produced, no matter by whom (Figure 8).

The functions *f*-deactivated^e and *f*-deactivated^s capture the idea of norm instances directed to the concrete agents but conditioned by the agent-SFAs. If an instance is assigned to the agent a_X because it carries the agent-status function α , then it is deactivated if a_X ceases to carry α (Figure 9).

The element $F \cup N \models c'_m$ in expressions (15) and (16) captures the assumption of Panagiotidi *et al.* (2013) that an active norm instance is deactivated if the deactivation condition starts to hold while the maintenance condition is still holding. While active norm instances are deactivated when the deactivation condition c'_d is satisfied, violated instances are deactivated by the satisfaction of the repair condition c'_r . Deactivations by reparation of violated instances are also considered at the individual agent level when they are conditioned by events (function *r*-deactivated^e). Reparations conditioned by states are achieved when the agents see to them that such state holds (function *r*-deactivated^s). Different of deactivations of active instances, the maintenance condition is not considered in the reparations of violated ones. An



Figure 7 Example of norm deactivation—event-status function obligation. Both the agents *bob* and *tom* are obliged to produce, in the environment, an event that counts as the evacuation of the downtown. The agent *bob* produces such an event, fulfilling, thus, his obligation. The obligation of the agent *tom* remains active until he does the same



Figure 8 Example of norm deactivation—state-status function obligation. Both the agents *bob* and *tom* are obliged to see to them that the environment is in a state that counts as the downtown being evacuated. The agent *bob* produces such state. Then, both *bob* and *tom* have their obligation fulfilled

instance, to be repaired, must be in the violated state, reached when the maintenance condition c'_m ceased to hold in the past. If it is the case that c'_m holds while the reparation condition of a violated instance is reached, such condition has started to hold again while the instance was violated, having thus no influence on such instance.

$$r\text{-deactivated}^{e}(F, N) = \{n' | \exists (e_X, a_X) \in E_X : n' \in VS \land c'_r \in \mathcal{E}_{\mathcal{F}} \land$$
$$F \models ((e_X, a_X) \text{ is } c'_r \lor \neg (a_X \text{ is } \alpha))\}$$
(17)



Figure 9 Example of norm deactivation—loss of agent-status function. The agent *bob* loses the status function of *firefighter* and, then, their standing obligations related to that status function are deactivated

$$r\text{-}deactivated^{s}(F, N) = \{n' | n' \in VS \land c'_{r} \in \mathcal{S}_{\mathcal{F}} \land$$

$$F \models (c'_{r} \lor \neg (a_{X} \mathbf{is} \alpha))\}$$

$$\text{s.t.} \quad n' = \langle (a_{X}, \alpha), c'_{a}, c'_{m}, c'_{d}, c'_{n}, c'_{d} \rangle$$

$$(18)$$

5.1.3 Violation

Active norm instances are considered violated when the constitutive and normative states do not satisfy the maintenance condition (function *violated* below).

$$violated(F, N) = \{n' | n' \in AS \land F \cup N \not\models c'_m\}$$

$$(19)$$

s.t. $n' = \langle (a_X, \alpha), c'_a, c'_m, c'_d, c'_r, c'_t \rangle$

Following the considered normative model, the Expression (19) captures the assumption that a norm instance becomes violated as soon as the maintenance condition ceases to hold, even if the deactivation or any other condition starts to hold at the same time.

5.1.4 Failure

An instance is failed if (i) it is violated and (ii) the current constitutive and normative states satisfy the timeout condition (function *failed* below).

$$failed(F, N) = \{n' | n' \in VS \land F \cup N \models c_t \}$$

$$s.t. \quad n' = \langle (a_X, \alpha), c'_{\alpha}, c'_{m}, c'_{d}, c'_{r}, c'_{t} \rangle$$

$$(20)$$

5.2 Monitoring norms based on the constitutive state

The original operational semantics for norm monitoring proposed by Panagiotidi *et al.* (2013) considers that the life cycle of the norm instances evolves based on the satisfaction of the conditions c_a , c_d , c_m , c_r , and c_t . Basing the regulation on the constitutive state requires also to consider other conditions captured by the functions (14)–(20). For this reason, to base the operational semantics of the normative monitor proposed by Panagiotidi *et al.* (2013) on the SAI constitutive state, we redefine below the transition rules presented in Section 2.

$\frac{n' \in activated(\mathcal{N}, F, N) \quad n' \notin f\text{-}deactivated^{e}(F, activated(\mathcal{N}, F, N)) \cup f\text{-}deactivated^{S}(F, activated(\mathcal{N}, F, N))}{M_{\mathcal{N}} \rhd \langle \mathcal{N}, AS \cup n', VS, DS, FS, s_{i+1} \rangle}$

$$\frac{n' \in AS \qquad n' \in violated(F, N)}{M_N \triangleright \langle \mathcal{N}, AS \setminus n', VS \cup n', DS, FS, s_{i+1} \rangle}$$
(22)

(21)

$$\frac{n' \in AS}{M_N \rhd \langle \mathcal{N}, AS \setminus n', VS, DS \cup n', FS, s_{i+1} \rangle}$$
(23)

$$\frac{n' \in VS}{M_N \rhd \langle \mathcal{N}, AS, VS \setminus n', DS \cup n', FS, s_{i+1} \rangle}$$
(24)

$$\frac{n' \in VS \quad n' \in failed(F, N)}{M_N \triangleright \langle \mathcal{N}, AS, VS \setminus n', DS, FS \cup n', s_{i+1} \rangle}$$
(25)

6 Example

Considering the proposed coupling and the scenario introduced in Section 3.3, we illustrate the evolving of the normative regulation based on the constitutive state. It is possible thus to observe the dynamics of the norms that abstract from the concrete environment but are still grounded in the concrete environment under regulation. The constitutive specification is shown in Figure 4. The norms are shown in Figure 5. We consider five steps of the environmental dynamics. In each step, the environmental state changes causing changes in the constitutive state and, as consequence, changing the normative state, as described below and summarized in Tables 1 and 2:

- Step 1. GIS indicate that the properties security_phase(downtown,preventive) and nb_inhabit (downtown,200) hold in the environment, meaning that (i) the downtown is on preventive phase of the crisis management and (ii) the downtown has 200 inhabitants. By the constitutive rule 5, the downtown counts as a secure zone. At this moment, the actor bob checks in the table_mayor and the actors tom, jim, and ana check in the table_fire_brigade. By the constitutive rules 1 and 2, bob counts as the mayor while tom, jim, and ana count as firefighter. As the downtown is considered secure, bob is obliged to evacuate it.
- **Step 2.** *Bob* puts the *launch_object* on the coordinates (2,2). By the constitutive rule 3, this event counts as the evacuation of the downtown, deactivating the previously created obligation.
- **Step 3.** After the evacuation performed by *bob*, for some reason, the downtown has 50 inhabitants. The security phase of the crisis changes from preventive to emergency, and, from the institutional perspective, the downtown is insecure (constitutive rule 6). Thus, new norm instances are created to be followed by the *firefighters*.
- **Step 4.** *Tom* puts the *launch_object* on the coordinates (2,2) of the table, while *jim* sends a message. Both the actions count as the evacuation of the downtown (constitutive rules 3 and 4). Thus, *tom* and *jim* fulfil their obligations.
- **Step 5.** The security phase of the crisis becomes again preventive, and, from the institutional perspective, the downtown is again secure (constitutive rule 5). The agent *ana* violates its obligation as it has not evacuated the downtown while it was insecure.

7 Discussion

In institutions as conceived by SAI, norms are based on the *interpretation* of the environment provided by the constitutive state, but they regulate the elements *under such interpretation*. It is necessary, thus, to define how the elements abstracted under the constitution are considered in the management of the normative state. Since the elements referred by the norms, that is, the status functions, may abstract more than one environmental element, it is necessary to define how such possible one-to-many relation is handled in the normative management. Our proposed coupling explicitly defines that (i) regarding to

Table 1	Evolution of	of environmental	and consti	tutive states

Step	Environmental State (X)	Constitutive State (F)
1	$\begin{aligned} A_X &= \{bob, tom, jim, ana\} \\ E_X &= \{(checkin(table_maior), bob), \\ & (checkin(table_fire_brigade), tom), \\ & (checkin(table_fire_brigade), jim), \\ & (checkin(table_fire_brigade), ana)\} \\ S_X &= \{security_phase(downtown, preventive), \\ & nb_inhabit(downtown, 200)\} \end{aligned}$	$A_{F} = \{ \langle bob, mayor \rangle, \langle tom, firefighter, \rangle, \\ \langle jim, firefighter \rangle, \langle ana, firefighter \rangle \} \\ S_{F} = \{ \langle security_phase(downtown, preventive), \\ secure(downtown) \rangle \} \end{cases}$
2	$\begin{split} A_X &= \{bob, tom, jim, ana\}\\ E_X &= \{(putTangible(launch_object, 2, 2), bob)\}\\ S_X &= \{security_phase(downtown, preventive),\\ nb_inhabit(downtown, 200)\} \end{split}$	$\begin{split} A_F &= \{ \langle bob, mayor \rangle, \langle tom, firefighter, \rangle, \\ & \langle jim, firefighter \rangle, \langle ana, firefighter \rangle \} \\ E_F &= \{ \langle putTangible(launch_object, 2, 2), \\ & evacuate(downtown), bob \rangle \} \\ S_F &= \{ \langle security_phase(downtown, preventive), \\ & secure(downtown) \rangle \} \end{split}$
3	$A_X = \{bob, tom, jim, ana\}$ $S_X = \{security_phase(downtown, emergency), \\ nb_inhabit(downtown, 50)\}$	$A_F = \{ \langle bob, mayor \rangle, \langle tom, firefighter, \rangle, \\ \langle jim, firefighter \rangle, \langle ana, firefighter \rangle \} \\ S_F = \{ \langle security_phase(downtown, emergency), \\ insecure(downtown) \rangle \} $
4	$A_{X} = \{bob, tom, jim, ana\}$ $E_{X} = \{(putTangible(launch_object, 2, 2), tom),$ $(send_message(evacuation, downtown),$ $jim)\}$ $S_{X} = \{security_phase(downtown, emergency),$ $nb_inhabit(downtown, 50)\}$	$\begin{split} A_F &= \{ \langle bob, mayor \rangle, \langle tom, firefighter, \rangle, \\ & \langle jim, firefighter \rangle, \langle ana, firefighter \rangle \} \\ E_F &= \{ \langle putTangible(launch_object, 2, 2), \\ & evacuate(downtown), tom \rangle, \\ & \langle send_message(evacuation, downtown), \\ & (evacuate(downtown), jim) \rangle \} \\ S_F &= \{ \langle security_phase(downtown, emergency), \\ & insecure(downtown) \rangle \} \end{split}$
5	$A_{X} = \{bob, tom, jim, ana\}$ $S_{X} = \{security_phase(downtown, preventive), \\ nbInhabit(downtown, 50)\}$	$A_{F} = \{ \langle bob, mayor \rangle, \langle tom, firefighter, \rangle, \\ \langle jim, firefighter \rangle, \langle ana, firefighter \rangle \} \\ S_{F} = \{ \langle security_phase(downtown, preventive), \\ secure(downtown) \rangle \} $

the addressee α , norms govern all the agents under the same constitution of agent-status function and (ii) the activation, maintenance, deactivation, repair, and timeout conditions c_a , c_m , c_d , c_r , and c_t , differently, point to (at least) a single constitution of event- and state-status function. For example, if many agents count as firefighter and two events count as an evacuation (Figure 4—constitutive rules 3 and 4) and if firefighters are obliged to evacuate an insecure zone (Figure 5—norm 2), then the obligation stands to every agent counting as *firefighter* (cf. step 3 of the example in Section 6). The fulfilment of the obligation requires that every firefighter produces at least one event interpreted as *evacuation*. By the constitutive rules 3 and 4, they can either put a tangible in the table or send a message (as it is done in step 4 of the example in Section 6).

When the normative regulation is based on the constitutive state, the expected agents' behaviour is attached to the status functions instead of attaching to the agents themselves. That is why norm instances are deactivated when the responsible agents are no longer carrying the target status function (expressions (15)–(18)). But other coupling approaches can be conceived where, for example, obligations and prohibitions remain active even if the agent-SFAs are revoked. These decisions concern the management of the social meanings of the agents in a society, which is a complex question that can be addressed in different ways (Tessop, 2011).

 Table 2
 Evolution of the normative state

Step	Normative state
1	$AS = \{ (bob, mayor), secure(downtown), secure(downtown), evacuate(downtown), \bot, \neg secure(downtown) \} \}$
2	$DS = \{(bob, mayor), secure(downtown), secure(downtown), evacuate(downtown), \bot, \neg secure(downtown))\}$
3	$\begin{split} AS &= \{ \langle (tom, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), \bot, \neg insecure(downtown) \rangle, \\ & \langle (jim, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), \bot, \neg insecure(downtown) \rangle, \\ & \langle (ana, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), \bot, \neg insecure(downtown) \rangle \} \\ DS &= \{ \langle (bob, mayor), secure(downtown), secure(downtown), evacuate(downtown), \bot, \neg secure(downtown) \rangle \} \end{split}$
4	$\begin{split} AS &= \{ \langle (ana, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), \bot, \neg insecure(downtown) \rangle \} \\ DS &= \{ \langle (bob, mayor), secure(downtown), secure(downtown), evacuate(downtown), \bot, \neg secure(downtown) \rangle, \\ & \langle (tom, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), \bot, \neg insecure(downtown) \rangle, \\ & \langle (jim, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), \bot, \neg insecure(downtown) \rangle \} \end{split}$
5	DS = {((bob, mayor), secure(downtown), secure(downtown), evacuate(downtown), ⊥, ¬secure(downtown)⟩, {(tom, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), ⊥, ¬insecure(downtown)⟩, {(jim, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), ⊥, ¬insecure(downtown)⟩} VS = {((ana, firefighter), insecure(downtown), insecure(downtown), evacuate(downtown), ⊥, ¬insecure(downtown))}

Keeping in mind that norms following different models may take part in an institution (Criado *et al.*, 2011), the institutional reality in SAI-that is, the constitutive state-provides a common, shared vocabulary, composed of the status functions, in terms of which all the norms of an institution can be expressed. But more than providing the set of words to be used to write norms, the institutional reality as conceived by SAI provides semantics to the institutional vocabulary through the typing of the status functions. Such semantics is also shared among all the norms in an institution. It is possible, thus, to establish clear relations between the components of the norms and the components of the institutional reality (cf. Section 4.1). For example, it is possible to convention that the addressee of the norms is specified in terms of agent-status functions, and, thus, the ' α ' of Panagiotidi *et al.* (2013) refers to the same kind of element (i.e. agent-status functions) as the addressee in any other normative representation.

When norms are specified in terms of status functions, they are consistent with the institutional reality and also with the environment under regulation. For instance, if *firefighter* is an agent-status function and *evacuate* is an event-status function, *evacuate* cannot be the bearer and *firefighter* cannot be the goal of a norm. Such consistency depends neither on the normative model nor on the normative specification. Rather, it is provided by the proper link between the components of the norms and the different kinds of status functions.

Basing the normative regulation on the constitutive state is not just about to specify norms through status functions. It is necessary to define how to manage norms based on an *interpretation* of the environment to regulate the elements *under such interpretation*. We addressed this point in two steps: (i) aligning constitutive and normative representations (cf. Section 4) and (ii) defining how the life cycle of the norm instances evolves according to the constitutive state (cf. Section 5). These two steps can be seen as a replicable strategy (a kind of 'method') to couple different normative models with the constitutive state.

8 Related work, conclusions, and perspectives

Some works, such as those by Dastani *et al.* (2009) and Aldewereld *et al.* (2010), consider that deontic notions can be reduced to classification statements based on counts as (Grossi *et al.*, 2005). In this case, certain circumstances count as norm violations and fulfilments. In our proposal, however, counts-as statements are not used to express regulation. Rather, they have the exclusive function of constituting the conditions evaluated by the norms.

More similar to our direction, some works consider that the normative regulation is based on some kind of interpretation of the environment, usually specified through constitutive rules. Sun and van der

Torre (2014) and Boella and van der Torre (2004, 2006a) discuss logic and semantics aspects of combining norms and constitutive rules without committing with particular constitutive and normative models. While our proposal embodies some of these aspects, such as the simple-minded semantics proposed by Sun and van der Torre (2014), as well as the notions of conjunction of output (if two status functions y_1 *and* y_2 are simultaneously assigned to some x, then it is possible to say that x counts both as y_1 and y_2), disjunction of input (if the status function y is simultaneously assigned to x_1 and x_2 , then it is possible to say that x_1 or x_2 count as y), and transitivity (if x counts y_1 and y_1 counts y_2 , then x counts as y_2) discussed by (Boella and van der Torre 2004, 2006a), it also takes into account the different dynamics of norms directed to event- and state-status functions. Furthermore, we consider that constituted elements base the *whole* normative life cycle–activation, deactivation,violation, etc.–while the referred works consider that constitution bases exclusively the deactivations of obligations.

The semantics of the constituted elements is an important point to be considered when norms are coupled with constitutive rules. In Aldewereld et al. (2010), the constitution, which affects the whole normative life cycle, results in predicates added to the knowledge base accessed by the normative reasoner. Such predicates, however, do not have any associated semantics from the normative perspective. In our approach, differently, norms are coupled in meaningful institutional elements constituted from environmental ones. Other approaches, closer to our one, consider that norms refer to constituted elements with a defined semantics. In Cliffe et al. (2007), norms are fulfilled and violated from the occurrence of either physical or *institutional events*, which are the institutional interpretation of the facts occurring in the environment, analogous to the event-status functions in SAI. In Cardoso and Oliveira (2007), the fulfilment conditions of norms are based exclusively on institutional events, admitting also that norms may prescribe the behaviour to *institutional roles*, which are analogous to the agent-status functions of SAI. A similar approach is proposed by Fornara et al. (2008). Viganó and Colombetti (2007, 2008) also consider institutional events and introduce the notion of status function as an abstraction of the agents acting in the environment. As the referred works do not propose a clear dynamics for the constitution, the coupling of norms with the constituted elements is limited to refer to the constituted elements in the normative specification. Our work, in turn, couples norms on a constitutive state that has a well-defined dynamics that is taken into account in the normative management.

Pieters *et al.* (2015) and García-Camino *et al.* (2006) consider that norms can prescribe behaviours composed of sets of sub-activities. The abstraction provided by the status functions makes possible to prescribe such a composition in the case of state-status functions constituted by a set of properties. However, composition of events, which is considered by the referred work, is not envisioned by the SAI model. Analyzing composition of events and states in SAI is a future work.

Coupling the normative regulation with the SAI constitutive state requires to consider the semantics of the different kinds of status functions in both the normative representation and dynamics. This work addresses these issues in Sections 4 and 5. We focused on the reasoning about the normative and constitutive states to define when instances should be activated, deactivated, violated, and failed. We have shown how such reasoning can be used by a normative monitor that manages the regulation on top of the constitutive state. But it can be useful for the agents to plan their actions in the environment as they can reason about the normative impact of the environmental facts in the constitutive state and, then, in the normative one.

The literature on norms presents several normative models that express the expected agents' behaviour in different ways.⁹ While norms following the NPL normative model (Hübner *et al.*, 2011) are used in de Brito *et al.* (2018) to illustrate regulation based on constitutive rules in SAI, this paper focuses on the coupling between constitutive rules and regulative norms in general using the normative model proposed by Panagiotidi *et al.* (2013).¹⁰ It discusses in greater depth the main issues of such coupling,

⁹ Details and comparisons on norms can be found in Boella *et al.* (2007, 2009), Andrighetto *et al.* (2013), Alechina *et al.* (2013), Hollander and Wu (2011), and in the COIN series of workshops (http://www.pcs.usp.br/~coin/), among others.

¹⁰ An implementation of the SAI interpreter for constitutive specifications, normative monitor, interfaces to connect this interpreter to a normative engine based on the model of Panagiotidi *et al.* (2013) and to the NPL engine, as well as some examples, are available at http://github.com/artificial-institutions/sai.

describing how the semantics of the different kinds of constituted elements is taken into account both in the normative specifications and in its dynamics. Applying a similar coupling to other normative models is a future work. We also plan to work (i) on agents using the proposed coupling to reason about the normative consequence of their actions in the environment, (ii) on a deeper analysis of implicit changes in the normative state due to revocations of agent-status functions, and (iii) on the analysis of the proposed coupling considering group norms.

Acknowledgements

The authors thank the anonymous reviewers of KER for their valuable remarks that have been taken into account in this paper.

References

- Aldewereld, H., Álvarez Napagao, S., Dignum, F. & Vázquez-Salceda, J. 2000. Making norms concrete. In Proceedings of the 9th International Conference on Autonomous Agents and Multiagent Systems (AAMAS 2010): Volume 1–3, Richland, SC, Richland, S. C., van der Hoek, W., Kaminka, G. A., Lespérance, Y., Luck, M. & Sen, M. (eds), IFAAMAS, 807–814.
- Alechina, N., Bassiliades, N., Dastani, M., Vos, M. D., Logan, B., Mera, S., Morris-Martin, A. & Schapachnik, F. 2013. Computational models for normative multi-agent systems. In *Normative Multi-Agent Systems*, 71–92. doi: 10.4230/DFU.Vol4.12111.71.
- Andrighetto, G., Governatori, G., Noriega, P. & van der Torre, L. W. N. (eds). *Normative Multi-Agent Systems*, Dagstuhl Follow-Ups **4**. Schloss Dagstuhl Leibniz-Zentrum fuer Informatik.
- Balke, T., Pereira, C. C., Dignum, F., Lorini, E., Rotolo, A., Vasconcelos, W. & Villata, S. 2013. Norms in MAS: definitions and related concepts. In *Normative Multi-Agent Systems*, Andrighetto, G., Governatori, G., Noriega, P. & van der Torre, L. W. N. (eds). Dagstuhl Follow-Ups 4, 1–31. Schloss Dagstuhl–Leibniz-Zentrumfuer Informatik.
- Boella, G., Noriega, P., Pigozzi, G. & Verhagen, H. (eds). 2009. Normative Multi-agent Systems, 15.03. -20.03.2009, Dagstuhl, Germany, Dagstuhl Seminar Proceedings 09121. Schloss Dagstuhl - Leibniz-Zentrum für Informatik.
- Boella, G. & van der Torre, L. 2006a. A logical architecture of a normative system. In *Deontic Logic and Artificial Normative Systems (DEON 2006)*, Goble, L. & Meyer, J.-J. C. (eds), LNCS 4048, 24–35. Springer.
- Boella, G. & van der Torre, L. 2006b. Constitutive norms in the design of normative multiagent systems. In *Computational Logic in Multi-Agent Systems (CLIMA VI)*, Toni, F. & Torroni, P. (eds), LNCS **3900**, 303–319. Springer. doi: 10.1007/1175073_17.
- Boella, G. & van der Torre, L. W. N. 2004. Regulative and constitutive norms in normative multiagent systems. In *Principles of Knowledge Representation and Reasoning: Proceedings of the Ninth International Conference* (*KR2004*), Dubois, D., Welty, C. A. & Williams, M.-A. (eds), 255–266. AAAI Press.
- Boella, G., van der Torre, L. W. N. & Verhagen, H. (eds). 2007. Normative Multi-agent Systems, 18.03. 23.03.2007, Dagstuhl, Germany, Dagstuhl Seminar Proceedings 07122. Internationales Begegnungs- und Forschungszentrum für Informatik (IBFI).
- Brachman, R. & Levesque, H. 2004. Knowledge Representation and Reasoning. Morgan Kaufmann Publishers Inc.
- Broersen, J. M., Cranefield, S., Elrakaiby, Y., Gabbay, D. M., Grossi, D., Lorini, E., Parent, X., van der Torre, L. W. N., Tummolini, L., Turrini, P. & Schwarzentruber, F. Normative reasoning and consequence. In Andrighetto et al. (2013), 33–70. doi: 10.4230/DFU.Vol4.12111.33.
- Cardoso, H. L. & Oliveira, E. C. 2007. Institutional reality and norms: specifying and monitoring agent organizations. International Journal of Cooperative Information Systems 16(1), 67–95.
- Castelfranchi, C. 2000. Engineering social order. In Engineering Societies in the Agent World, First International Workshop, ESAW 2000, Berlin, Germany, 21 August 2000, Revised Papers, Omicini, A., Tolksdorf, R. & Zambonelli, F. (eds), LNCS 1972, 1–18. Springer. doi: 10.1007/3-540-44539-0_1.
- Cliffe, O., De Vos, M. & Padgetm, J. 2007. Answer set programming for representing and reasoning about virtual institutions. In *Computational Logic in Multi-Agent Systems*, Inoue, K., Satoh, K. & Toni, F. (eds), Lecture Notes in Computer Science 4371, 60–79. Springer. doi: 10.1007/978-3-540-69619-3_4.
- Criado, N., Argente, E. & Botti, V. J. 2011. Open issues for normative multi-agent systems. *AI Communications* **24**(3), 233–264. doi: 10.3233/AIC-2011-0502.
- Dastani, M., Grossi, D., Meyer, J. C. & Tinnemeier, N. A. M. 2009. Normative multi-agent programs and their logics. In *Normative Multi-Agent Systems*, Boella, G., Noriega, P., Pigozzi, G. & Verhagen, H. (eds), Dagstuhl Seminar Proceedings 09121. Schloss Dagstuhl - Leibniz-Zentrum für Informatik.

18

- de Brito, M., Hübner, J. F. & Boissier, O. 2014. A conceptual model for situated artificial institutions. In *Computational Logic in Multi-Agent Systems (CLIMA XV)*, Bulling, N., van der Torre, L., Villata, S., Jamroga, W. & Vasconcelos, W. (eds), LNCS 8624, 35–51. Springer.
- de Brito, M., Hübner, J. F. & Boissier, O. 2015a. Bringing constitutive dynamics to situated artificial institutions. In *Progress in Artificial Intelligence - EPIA 2015*, Pereira, F., Machado, P., Costa, E. & Cardoso, A. (eds), LNCS 9273, 624–637.
- de Brito, M., Hübner, J. F. & Boissier, O. 2015b. Coupling regulative and constitutive dimensions in situated artificial institutions. In *Multi-Agent Systems and Agreement Technologies - 13th European Conference, EUMAS 2015, and Third International Conference, AT 2015, Athens, Greece, 17–18 December 2015, Revised Selected Papers,* Rovatsos, M., Vouros, G. A. & Julián, V. (eds), Lecture Notes in Computer Science **9571**, 318–334. Springer International Publishing. doi: 10.1007/978-3-319-33509-4_25.
- de Brito, M., Thévin, L., Garbay, C., Boissier, O. & Hübner, J. F. 2015c. Situated artificial institution to support advanced regulation in thefield of crisis management. In Advances in Practical Applications of Agents, Multi-Agent Systems, and Sustainability (PAAMS 2015), Demazeau, Y., Decker, K. S., Pérez, J. B. & de la Prieta, F. (eds), LNCS 9086, 66–79.
- de Brito, M., Hübner, J. F. & Boissier, O. 2018. Situated artificial institutions: stability, consistency, and flexibility in the regulation of agent societies. *Autonomous Agents and Multi-Agent Systems* 32(2), 219–251. doi: 10.1007/s10458-017-9379-3.
- De Vos, M., Balke, T. & Satoh, K. 2013. Combining Event-and State-based Norms. In International conference on Autonomous Agents and Multi-Agent Systems, (AAMAS'13), Gini, M. L., Shehory, O., Ito, T. & Jonker, C. M. (eds), 1157–1158. IFAAMAS.
- Fasli, M. 2004. Accounting for social order in multi-agent systems: Preliminary report. In 2004 IEEE/WIC/ACM International Conference on Intelligent Agent Technology (IAT 2004), 20–24 September 2004, Beijing, China, 204–210. IEEE Computer Society. doi: 10.1109/IAT.2004.1342945.
- Fornara, N., Viganò, F., Verdicchio, M. & Colombetti, M. 2008. Artificial institutions: a model of institutional reality for open multiagent systems. *Artificial Intelligence and Law* 16(1), 89–105. doi: 10.1007/s10506-007-9055-z.
- Garcá-Camino, A., Noriega, P. & Rodrguez-Aguilar, J. A. 2006. An algorithm for conflict resolution in regulated compound activities. In *Engineering Societies in the Agents World VII, 7th International Workshop, ESAW 2006, Dublin, Ireland, September 6–8, 2006 Revised Selected and Invited Papers*, O'Hare, G. M. P., Ricci, A., O'Grady, M. J. & Dikenelli, O. (eds), LNCS 4457, 193–208. Springer. doi: 10.1007/978-3-540-75524-1_11.
- Grossi, D., Meyer, J. C. & Dignum, F. 2005. Modal logic investigations in the modal logic investigations in the semantics of counts semantics of counts-as as. In 10th International Conference on Artificial Intelligence and Law (ICAIL 2005), Sartor, G. (ed), 1–9. ACM.
- Hollander, C. D. & Wu, A. S. 2011. The current state of normative agent-based systems. *Journal of Artificial Societies and Social Simulation* 14(2). doi: 10.18564/jasss.1750.
- Hübner, J. F., Boissier, O. & Bordini, R. H. 2011. A normative programming language for multi-agent organisations. Annals of Mathematics and Artificial Intelligence 62(1–2), 27–53. ISSN 1012-2443. doi: 10.1007/s10472-011-9251-0.
- Kubicki, S., Lepreux, S. & Kolski, C. 2012. Rfid-driven situation awareness on tangisense, a table interacting with tangible objects. *Personal and Ubiquitous Computing* **16**(8), 1079–1094.
- López y López, F. & Luck, M. 2003. Modelling norms for autonomous agents. In 4th Mexican International Conference on Computer Science (ENC 2003), 8–12 September 2003, Apizaco, Mexico, 238–245. IEEE Computer Society Press. ISBN 0-7695-1915-6. doi: 10.1109/ENC.2003.1232900.
- Moses, Y. & Tennenholtz, M. 1995. Artificial social systems. Computers and Artificial Intelligence 14(6), 533–562.
- Panagiotidi, S., Álvarez-Napagao, S. & Vázquez-Salceda, J. 2013. Towards the norm-aware agent: bridging the gap between deontic specifications and practical mechanisms for norm monitoring and norm-aware planning. In *Coordination, Organizations, Institutions, and Norms in Agent Systems (COIN IX)*, Balke, T., Dignum, F., van Riemsdijk, M. B. & Chopra, A. K. (eds), LNCS 8386, 346–363. Springer.
- Pieters, W., Padget, J., Dechesne, F., Dignum, V. & Aldewereld, H. 2015. Effectiveness of qualitative and quantitative security obligations. *Journal of Information Security and Applications* 22, 3–16. doi: 10.1016/j.jisa.2014.07.003.
- Piunti, M. 2009. Designing and Programming Organizational Infrastructures for Agents Situated in Artifact-based Environments. PhD thesis, Universit' di Bologna.

Searle, J. 1995. The Construction of Social Reality. Free Press.

- Searle, J. 2009. Making the Social World: The Structure of Human Civilization. Oxford University Press.
- Sun, X. & van der Torre, L. W.N. 2014. Combining constitutive and regulative norms in input/output logic. In Deontic Logic and Normative Systems - 12th International Conference, DEON 2014, Ghent, Belgium, 12–15 July 2014. Proceedings, Cariani, F., Grossi, D., Meheus, J. & Parent, X. (eds), Lecture Notes in Computer Science 8554, 241–257. Springer. doi: 10.1007/978-3-319-08615-6_18.
- Tessop, R. K. 2011. Gestion de lóuverture au sein dórganisations multi-agents: une approche basée sur des artefacts organisationnels. PhD thesis, École Nationale Supéurieure des Mines de Saint-Étienne.

- Viganò, F. & Colombetti, M. 2007. Specification and verification of institutions through status functions. In *Coordination, Organizations, Institutions, and Norms in Agent Systems II*, Noriega, P., VÄzquez-Salceda, J., Boella, G., Boissier, O., Dignum, V., Fornara, N. & Matson, E. (eds), LNCS **4386**, 115–129. Springer. doi: 10.1007/978-3-540-74459-7_8.
- Viganò, F. & Colombetti, M. 2008. Model checking norms and sanctions in institutions. In *Coordination, Organizations, Institutions, and Norms in Agent Systems III*, Sichman, J. S. A., Padget, J., Ossowski, S. & Noriega, P. (eds), LNCS 4870, 316–329. Springer. ISBN 978-3-540-79002-0. doi: 10.1007/978-3-540-79003-7_23.