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# **Research Article**

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# Excitation of Gould–Trivelpiece mode by streaming particles in dusty plasma

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#### Abstract

In this paper, we study the excitation of Gould–Trivelpiece (TG) waves by streaming ions in dusty plasma and derive the dispersion relation of the excited waves using first-order perturbation theory. The motion of charged particles is controlled by electromagnetic fields in plasma. The energy transfer processes which occur in this collisionless plasma are believed to be based on wave–particle interactions. We have found that the TG waves may be generated in a streaming ion plasma via Cerenkov interaction, and the ions may be accelerated by TG waves via cyclotron interaction, which enable energy and momentum transfer. The variation in the growth rate of TG wave with dust grain size and relative density of negatively charged dust grains is also studied. The dust can cause an unstable TG mode to be stable in Doppler resonance, and can induce an instability in Cerenkov interaction.

## Introduction

Gould-Trivelpiece (TG) waves are electrostatic waves which are significantly observed in the range of frequency between ion plasma frequency and electron cyclotron frequency. For many decades, the TG waves are being investigated theoretically and experimentally (Trivelpiece and Gould, 1959; Malmberg and Wharton, 1966; Mannheimer, 1969; Lynov et al., 1979; Schamel, 1979) by the researchers due to their property of absorbing and heating the electrons effortlessly near the boundary of the plasma. In bounded plasmas, the TG wave appears as a short radial wavelength, whereas in unbounded plasmas, it is found to be accompanied with a short azimuthal wavelength (Stenzel and Urrutia, 2016). Praburam and Sharma (1992) have studied the excitation of TG wave of higher frequency vibrations by electron beam of low-energy. Carmel et al. (1990) have experimentally demonstrated the effect of high-power relativistic electron beam on a plasma column. They found that electrostatic TG modes propagate with the frequency below the plasma frequency, whereas electromagnetic waves propagate with the frequency above the plasma frequency. Zhai et al. (1993) observed TG mode in the experimental investigation of a plasma-filled backward wave oscillator. Haas and Pascoal (2017) have studied the electrostatic instabilities in magnetized plasma driven by neutrino. They found that the magnetic field significantly improves the linear instability growth rate for Supernova type II environments. High-frequency electromagnetic waves have been studied in unbounded as well as warm plasma by Assis and Sakanaka (1990). Mouzouris and Scharer (1998) examined the helicon wave along with TG wave through wave propagation and absorption simulations. In their study, they developed a computer code in which they found that the power absorption is due to TG wave near the edge region, whereas transportation and deposition of energy in the core region of plasma is due to helicon wave.

Over the decades, there has been a great deal of interest shown by the researchers in the study of electrostatic and electromagnetic waves in dusty plasma environments. In laboratory, these waves have been investigated in non-magnetized dusty plasma (Pieper and Goree, 1996) and magnetized dusty plasma (Thompson et al., 1997). Theoretically, these waves have been studied for the effect of dust parameters on the dispersion and growth rate of these waves in various interactions (Prakash et al., 2013a, 2013b, 2014; Sharma et al., 2014; Gupta et al., 2015). Recently, excitation of TG wave by relativistic electron beam in magnetized dusty plasma has been studied by Kaur et al. (2018). In their study, they observed that the growth rate decreases with relativistic factor. Barkan et al. (1996) have studied ion-acoustic waves in magnetized dusty plasmas and found that the phase velocity of the ion acoustic waves (IAWs) lift up with the negatively charged dust grains. The drastic reduction in the strength of the Landau damping has also been reported in this case. Prakash et al. (2013a) have studied the excitation of surface plasma wave via Cerenkov and fast cyclotron interaction by a densitymodulated electron beam in a magnetized dusty plasma cylinder and found that the dust significantly affects the dispersion and growth rate of waves. Excitation of lower hybrid wave by an ion beam has been investigated by Prakash et al. (2013b) and they found that the lower

hybrid modes showed maximum growth when phase velocity of mode is comparable to the electron thermal velocity. Interaction of whistler waves with an electron beam in magnetoplasmas has been studied by Gupta *et al.* (2015) for parallel and oblique propagation of beam and whistlers. The effect of negatively charged dust grains on the excitation of dust-acoustic waves by an ion beam has been reported by Sharma *et al.* (2014).

In this paper, we have developed a model for the excitation of TG mode by streaming ions in magnetized dusty plasmas. Section "Instability analysis" contains the instability analysis. Using linear first-order perturbation theory, the response of TG waves due to streaming ions in dusty plasma is obtained. Section "Numerical results and discussion" gives the results and discussion of instability. The results of work are concluded in section "Conclusion".

#### Instability analysis

Consider a plasma with equilibrium electron number density  $n_{e0}$ , ion number density  $n_{i0}$ , and dust grain number density  $n_{d0}$ . The dusty plasma is under the influence of the static magnetic field  $B_s$ in the z-direction. The electrons are defined by  $(-e, m_e, T_e)$ , ions by  $(e, m_i, T_i)$  and dust particles by  $(-Q_{d0}, m_d, T_d)$ . Consider an electrostatic wave, say, TG mode, propagating almost perpendicular to the external magnetic field (propagation vector **k**) in the *x*-*z* plane. The streaming ions are considered to be magnetized and moving parallel to applied magnetic field with velocity  $v_i$ , electrons are taken to be non-streaming and magnetized and dust grains are considered as negatively charged, non-streaming, and unmagnetized. Prior to the perturbation, plasma system is quasineutral such that  $-n_{e0} + n_{i0} - n_{d0} \approx 0$ . This equilibrium is perturbed due to electrostatic TG mode and potential associated with it is given by

$$\phi = \phi_0 \exp[-i(\omega t - k_x x - k_z z)]. \tag{1}$$

The plasma species are taken as fluids and governed by the equation of motion  $[m(d\vec{v}/dt) = e\vec{E} + (e/c)\vec{v} \times \vec{B_s}]$  and equation of continuity  $[(\partial n/\partial t) + \nabla .(n\vec{v}) = 0]$ . On linearization, the equation of motion and the equation of continuity lead to the plasma electron, plasma ion, and dust grain density perturbations as:

$$n_{1e} = -\frac{n_{e0}e\varphi}{m_e} \left[ \frac{k_x^2}{\omega^2 - \omega_{ce}^2} + \frac{k_z^2}{\omega^2} \right],$$
(2)

$$n_{1i} = \frac{n_{i0} e \phi}{m_i} \left[ \frac{k_x^2}{(\omega - k_z v_i)^2 - \omega_{ci}^2} + \frac{k_z^2}{(\omega - k_z v_i)^2} \right],$$
(3)

$$n_{\rm 1d} = -\frac{n_{\rm d0} Q_{\rm d0} k^2 \phi}{m_{\rm d} \omega^2}, \tag{4}$$

where  $\omega_{ce}(=eB_s/m_ec)$  is the electron-cyclotron frequency and  $\omega_{ci}(=eB_s/m_ic)$  is the ion-cyclotron frequency.

In this case, dust is taken as unmagnetized since  $\omega \gg \omega_{cd}$ with  $\omega_{cd}(=Q_{d0}B_s/m_dc)$  (dust cyclotron frequency). Further applying the probe theory to a dust grain,  $Q_d$  is said to be wellbalanced with the plasma currents present on the grain surface (Whipple *et al.*, 1985; Jana *et al.*, 1993) and the dust grain charge fluctuation as

$$Q_{\rm 1d} = \frac{|I_{\rm e0}|}{i(\omega + i\eta)} \left(\frac{n_{\rm 1i}}{n_{\rm i0}} - \frac{n_{\rm 1e}}{n_{\rm e0}}\right).$$
 (5)

Substituting the values of  $n_{1e}$  and  $n_{1i}$  from Eqs. (2) and (3) in Eq. (5), we obtain

$$Q_{1d} = \frac{|I_{e0}|}{i(\omega + i\eta)} \left[ \frac{k_x^2 \phi}{[(\omega - k_z v_i)^2 - \omega_{ci}^2]m_i} + \frac{k_z^2 \phi}{(\omega - k_z v_i)^2 m_i \omega^2} + \frac{k_x^2 \phi}{m_e (\omega^2 - \omega_{ce}^2)} + \frac{k_z^2 \phi}{m_e \omega^2} \right].$$
(6)

Under the view of overall charge neutrality in equilibrium, we can write,

$$-en_{i0} + en_{e0} + Q_{d0}n_{d0} = 0$$
 or  $n_{d0}/n_{e0} = (\delta - 1)(e/Q_{d0})$ ,

where  $\delta = n_{i0}/n_{e0}$  is the relative density of negatively charged dust grains.

Using Poisson's equation

$$\nabla^2 \phi = 4\pi n_{1e} e - 4\pi n_{1i} e + 4\pi n_{d0} Q_{1d} + 4\pi Q_{d0} n_{1d}$$
(7)

and substituting the values from Eqs. (2)–(4) and (6) in (7), and taking  $\omega \ll \omega_{ce}$  for TG mode, we obtain

$$1 + \frac{\omega_{\rm pe}^2}{\omega^2 K k^2} \frac{k_z^2}{k^2} + \frac{i\beta}{(\omega + i\eta)K} \frac{\omega_{\rm pe}^2}{\omega_{\rm ce}^2} \frac{k_x^2}{k^2} - \frac{i\beta}{(\omega + i\eta)K} \frac{m_{\rm e}}{m_{\rm i}} \frac{\omega_{\rm pe}^2}{\omega^2} \frac{k_z^2}{k^2} + \frac{\omega_{\rm pd}^2}{\omega^2 K} = \frac{\omega_{\rm pi}^2}{(\omega - k_z v_{\rm i})^2 K k^2} \frac{k_z^2}{k^2} + \frac{\omega_{\rm pi}^2}{[(\omega - k_z v_{\rm i})^2 - \omega_{\rm ci}^2] K k^2} \frac{k_z^2}{k^2}$$
(8)
$$+ \frac{i\beta}{(\omega + i\eta)K} \frac{\omega_{\rm pe}^2}{[(\omega - k_z v_{\rm i})^2 - \omega_{\rm ci}^2] k^2} \frac{k_z^2}{k^2},$$

where

$$\omega_{\rm pe}^2 = \left(\frac{4\pi n_{\rm e0}e^2}{m_{\rm e}}\right), \ \omega_{\rm pi}^2 = \left(\frac{4\pi n_{\rm i0}e^2}{m_{\rm i}}\right)$$

and

$$\omega_{\rm pd}^2 = \left(\frac{4\pi n_{\rm d0}e^2}{m_{\rm d}}\right). \ \beta = \left(\frac{|I_{\rm e0}|}{e}\frac{n_{\rm d0}}{n_{\rm e0}}\right)$$

is the dust plasma coupling parameter given as

$$\beta = 0.397(1 - (1/\delta)) (a/v_{\rm te})(m_{\rm i}/m_{\rm e})\omega_{\rm pi}^2, \text{ and}$$
(9)

$$\eta = 10^{-2} \omega_{\rm pe} \left( \frac{a}{\lambda_{\rm De}} \right) \frac{1}{\delta}.$$
 (10)

where,  $\eta$  is the time scale of delay and  $v_{te}(=\sqrt{2T_e/m_e})$  is the thermal velocity of electrons (Prakash and Sharma, 2009). For nonstreaming ions  $v_i = 0$  and for a plasma without dust grains  $\delta = 1$ . Using the conditions for the existence of TG wave, that is,  $\omega_{pi} \ll \omega \ll \omega_{ce}$ , we get  $\omega = \omega_{pe}(k_z/k)$  which is the standard dispersion relation of TG wave (Jain and Khristiansen, 1983; Jain and Khristiansen, 1984).

Equation (8) can be rewritten as

$$\begin{aligned} (\omega^{2} - \alpha^{2})(\omega + i\eta + i(\beta_{1} + \beta_{2})) \\ &= \left[ \frac{\omega_{\text{pi}}^{2} \omega^{3}}{\left[ (\omega - k_{z} v_{\text{i}})^{2} - \omega_{\text{ci}}^{2} \right] K k^{2}} + \frac{\omega_{\text{pi}}^{2} \omega^{3}}{(\omega - k_{z} v_{\text{i}})^{2} K k^{2}} \right] \\ &+ i \left[ \frac{\omega_{\text{pi}}^{2} \omega^{2}}{\left[ (\omega - k_{z} v_{\text{i}})^{2} - \omega_{\text{ci}}^{2} \right] 1 K k^{2}_{z}} (\eta + \frac{\beta}{\delta}) + \frac{\omega_{\text{pi}}^{2} \omega^{2} \eta}{(\omega - k_{z} v_{\text{i}})^{2} K k^{2}} \frac{1 k^{2}_{z}}{K k^{2}} \right], \end{aligned}$$
(11)

where

$$\alpha^2 = \frac{1}{K} \left( \omega_{\text{pe}}^2 \frac{k_z^2}{k^2} - \omega_{\text{pd}}^2 \right), \tag{12}$$

$$\beta_1 = \beta \frac{1}{K} \frac{\omega_{\text{pe}}^2 k_x^2}{\omega_{\text{ce}}^2 k^2},$$
$$\beta_2 = \left(-\beta \frac{1}{K} \omega_{\text{pe}}^2 \frac{k_z^2}{k^2} \left(1 + \frac{m_{\text{e}}}{m_{\text{i}}}\right)\right) / \omega^2,$$

and

$$K = 1 + \frac{\omega_{\rm pe}^2}{\omega_{\rm ce}^2}.$$

Equation (11) gives dispersion relation for the TG wave. The first bracket on the left-hand side of Eq. (11) associates with TG modes in a dusty plasma with frequency given by Eq. (12). The second bracket of Eq. (11) gives the damping mode due to dust charge fluctuations. From Eq. (11), in the absence of streaming ions and putting  $\delta(=n_{10}/n_{e0}) = 1$ , that is,  $\beta \rightarrow 0$ , we obtain

$$\omega^2 = \omega_{\rm tg}^2 \left( 1 + \frac{m_{\rm i}}{m_{\rm e}} \frac{k_z^2}{k^2} \right),$$

where

$$\omega_{\rm tg}^2 = \omega_{\rm pi}^2 / \left( 1 + \frac{\omega_{\rm pe}^2 k_x^2}{\omega_{\rm ce}^2 k^2} \right),$$

which are the standard expressions for TG mode in plasma.

Further, solving Eq. (11) under three limits:

**Case I**: For fast cyclotron interaction between TG wave and streaming plasma ions, that is, when  $\omega - k_z v_i = +\omega_{ci}$ , Eq. (11) can be rewritten as

$$\Delta_1^2 = \left[\frac{\omega_{\rm pi}^2}{4K\omega_{\rm ci}}\frac{k_x^2}{k^2}\alpha\right] + i\left[\frac{\omega_{\rm pi}^2}{4K\omega_{\rm ci}}\frac{k_x^2}{k^2}\left(\eta + \frac{\beta}{\delta}\right)\right],$$

where we have considered only the cyclotron interaction terms from RHS of Eq. (11).  $\Delta_1$  is the small frequency discrepancy

due to the finite value on RHS of Eq. (11). This gives the growth rate of TG mode as

$$\gamma_1 = \operatorname{Im}(\Delta_1) = \frac{Q_1}{2\sqrt{P_1}},\tag{13}$$

where

$$P_1 = \frac{\omega_{\rm pi}^2}{4K\omega_{\rm ci}} \frac{k_x^2}{k^2} \alpha$$

and

$$Q_1 = \frac{\omega_{\rm pi}^2}{4K\omega_{\rm ci}}\frac{k_x^2}{k^2}\left(\eta + \frac{\beta}{\delta}\right).$$

**Case II:** For slow cyclotron interaction between TG wave and streaming plasma ions, that is, when  $\omega - k_z v_i = -\omega_{ci}$ , Eq. (11) can be rewritten as

$$\Delta_2^2 = \left[\frac{\omega_{\rm pi}^2}{4K(-\omega_{\rm ci})}\frac{k_x^2}{k^2}\alpha\right] + i\left[\frac{\omega_{\rm pi}^2}{4K(-\omega_{\rm ci})}\frac{k_x^2}{k^2}\left(\eta + \frac{\beta}{\delta}\right)\right]$$

where again we have considered only the cyclotron interaction terms from RHS of Eq. (11).

The growth rate of TG mode in this limit is obtained as

$$\gamma_2 = \operatorname{Im}(\Delta_2) = \frac{Q_2}{2\sqrt{P_2}},\tag{14}$$

where  $\Delta_2$  is the small frequency discrepancy,

$$P_2 = \frac{\omega_{pi}^2}{4K(-\omega_{ci})} \frac{k_x^2}{k^2} \alpha$$

and

$$Q_2 = \frac{\omega_{\rm pi}^2}{4K(-\omega_{\rm ci})} \frac{k_x^2}{k^2} \left(\eta + \frac{\beta}{\delta}\right).$$

**Case III:** For Cerenkov interaction when  $\omega = k_z v_i$  then Eq. (11) can be written as

$$\Delta_3^3 = \frac{\omega_{\rm pi}^2 k_z^2}{2K k^2} (\alpha + i\eta),$$

where we have considered only the Cerenkov interaction terms from RHS of Eq. (11).  $\Delta_3$  is the small frequency discrepancy.

Therefore, the growth rate of TG mode in this case is given by

$$\gamma_3 = \operatorname{Im}(\Delta_3) = \frac{\eta}{3\alpha} \left[ \frac{\omega_{\rm pi}^2 k_z^2}{2K k^2} \alpha \right]^{1/3}.$$
 (15)

## Numerical results and discussion

For numerical calculations, the plasma parameters are taken as: number density of plasma ions  $n_{i0} = 10^9 \text{ cm}^{-3}$ , number density of plasma electrons  $n_{e0} = 0.2 \times 10^9 - 1 \times 10^9 \text{ cm}^{-3}$ , temperatures



**Fig. 1.** Growth rate  $\gamma_1(s^{-1})$  as a function of normalized parallel wave number  $k_z/k$  during fast cyclotron interaction for  $\delta = 1, 2, 3, 4, 5$ .

of electrons and ions are taken as 0.2 eV, external magnetic field is 3kG, number density of dust grains density is  $10^4$  cm<sup>-3</sup>, and  $m_i/$  $m_{\rm e} = 7.16 \times 10^4$  for potassium plasma and the average dust grain size  $a = 2 \mu m$ . Using Eq. (13), we have plotted the growth rate  $\gamma_1(s^{-1})$  of TG mode during fast cyclotron interaction with plasma ions as a function of normalized parallel wave number  $k_z/k$  for different values of  $\delta = (n_{i0}/n_{e0})$  (relative density of negatively charged dust grains) (c.f. Fig. 1). It is observed that the growth rate decreases as the parallel wave number increases. This shows that the growth rate of unstable mode decreases in the direction of the applied magnetic field or the direction of streaming ions. Therefore, we can say that the TG wave grows with an increase in perpendicular wave number or the unstable mode grows along its direction of propagation, if the magnetized plasma ions undergo a normal cyclotron resonance interaction with the TG waves. It can also be inferred from Eq. (13) that the growth rate of TG mode increases with an increase in the value of magnetic field, as observed by Haas and Pascoal, (2017). The growth of TG waves across the magnetic field may be attributed to the fact that these waves have a frequency between ion and electron gyrofrequencies. Due to which electrons are strongly magnetized but ions do not feel the presence of the magnetic field and can oscillate freely across the field lines. Therefore, the ions interact with waves having phase velocities perpendicular to the magnetic field. During normal resonance, the fast parallel component waves give energy to the streaming ions and their velocity increases. The high-velocity plasma ions interact with the perpendicular component of waves and the wave grows across the magnetic field.

Figure 2 represents the growth rate  $\gamma_1(s^{-1})$  as a function of dust grain size *a* (cm)for different values of  $\delta$  keeping all the other parameters [c.f. Eq. (13)] same as used for plotting Figure 1. The growth rate of unstable mode first increases, reaches a maximum value, and then decreases to zero for  $\delta = 1$  and  $\delta = 2$ . The reason for the above result is that as dust grains are added in the plasma, free electrons in the plasma approach it, increasing the surface potential of dust grains, further increasing the average dust grain charge  $Q_{d0}$ . Hence the number density of free electrons in the plasma reduces with respect to number density of plasma ions. Thus the ions have an effective mass  $m_{ieff} = (m_i/n_{i0})n_{e0}$ ,



**Fig. 2.** Growth rate  $\gamma_1(s^{-1})$  as a function of size of dust grains *a* (cm) during fast cyclotron interaction, for  $\delta$  = 1, 2, 3, 4, 5.



Fig. 3. Growth rate  $\gamma_1(s^{-1})$  during fast cyclotron interaction as a function of  $\delta$  for a =  $1.2\times10^{-4}$  cm .

which is less than  $m_i$  and their greater mobility leads to wave generation along the magnetic field direction also. As the size of dust grain increases, more and more electrons approach it, and the growth rate of TG wave is enhanced. The growth rate shows a maxima and then decreases as observed in Figure 1 also. The parallel phase velocity of TG wave  $(\omega/k_z)$  is more than the streaming ions velocity during normal cyclotron resonance. The relative motion of the waves and ions across the magnetic field causes a Doppler shift of the wave frequency up to the ion cyclotron frequency and the waves are generated across the magnetic field. Thus the growth rate of TG mode decreases with parallel wave number as shown in Figure 2. It is also observed that the peak value of growth rate decreases as  $\delta$  increases. The critical value of dust grain size to obtain a maximum growth for  $\delta = 1$  is  $2.5 \times 10^{-4}$  cm. Our trend of growth rate is similar to the results of Tribeche and Zerguini (2001) for a dusty plasma.

Again, using Eq. (13) we have plotted Figure 3 which shows the variation of growth rate  $\gamma_1(s^{-1})$  as a function of  $\delta = (n_{i0}/n_{c0})$ 

 $r_{y} = \frac{10^{\circ}}{10^{\circ}}$ 

**Fig. 4.** Damping rate  $\gamma_2(s^{-1})$  as a function of normalized parallel wave number  $k_z/k$  during slow cyclotron interaction for  $\delta = 1, 2, 3, 4, 5$ .

for dust grain size  $a = 1.2 \times 10^{-4}$  cm. The growth rate decreases with increase in the value of  $\delta$ . As the value of  $\delta$  increases, the relative density of electrons in dusty plasma decreases and the ambient plasma becomes deficient of electrons. Hence more and more energy will be supplied by the TG wave to the dusty plasma through dust grains, which decreases its growth.

Using Eq. (14) we have plotted Figure 4 which shows the damping rate of TG mode in slow cyclotron interaction  $\gamma_2(s^{-1})$ as a function of normalized parallel wave number  $k_z/k$ . Figure 4 indicates that damping rate of TG wave reduces with an increase in parallel wave number. This indicates that the TG wave damps with an increase in the parallel wave number during anomalous cyclotron resonance interaction with the streaming ions. It can also be inferred that the wave damping reduces along the magnetic field direction or along the direction of streaming ions but enhances in a direction perpendicular to the magnetic field. During anomalous resonance, the positive ions overtake the waves  $(\omega - k_z v_i = -\omega_{ci})$  as phase velocity of waves is less than the streaming ions velocity. The Doppler shift decreases the wave frequency to that of ion cyclotron frequency. The waves gain energy from the ions, and the damping of waves is reduced along the magnetic field lines.

Further, when the phase velocity of TG mode is equal to the streaming ions velocity, that is, for Cerenkov interaction between plasma ions and TG mode, using Eq. (15) Figure 5 is plotted, which shows the growth rate  $\gamma_3(s^{-1})$  of unstable mode as a function of normalized parallel wave number  $k_z/k$  for different values of  $\delta$ , keeping all other plasma parameters constant. It is observed that the growth rate of unstable mode increases with increase in parallel wave number for all the values of  $\delta$ . In other words, the TG wave grows with an increase in parallel wave number during Cerenkov interaction with streaming ions. In this case, the phase velocity of TG wave is comparable to the streaming ions velocity, and therefore the wave grows due to inverse Landau damping. Due to cyclotron interactions, a situation is created, where in a given velocity interval around the phase velocity of the wave, there are more number of faster ions than of slower ions. Thus the waves grow by gaining energy from the ions, which corresponds to inverse Landau damping. The ions are thus decelerated and they lose their energy to the wave, synchronizing with the wave.



**Fig. 5.** Growth rate  $\gamma_3(s^{-1})$  as a function of normalized parallel wave number  $k_z/k$  during Cerenkov interaction for  $\delta = 1, 2, 3, 4, 5$ .



Fig. 6. Growth rate  $\gamma_3(s^{-1})$  as a function of size of dust grains *a* (cm) during Cerenkov interaction for  $\delta$  = 1, 2, 3, 4, 5.

Figure 6 shows the variation of growth rate  $\gamma_3(s^{-1})$  of unstable mode during Cerenkov interaction with respect to dust grain size *a* (cm) for different values of  $\delta$ . It is found that growth rate of unstable TG mode increases (c.f. Eq. 15) with the increasing size of dust grains due to electron capturing ability. The dust grains capture electrons and wave will gain energy from these electrons through dust grains in the plasma which lead to the enhancement in the growth of TG wave, as obtained in the case of fast cyclotron interaction. In this case, a maxima in growth rate is not observed as the parallel phase velocity of wave is equal to the streaming ions velocity, due to which a strong interaction occurs between the two and the wave keeps growing along the ion streaming direction.

Figure 7 displays the growth rate  $\gamma_3(s^{-1})$  of unstable mode during Cerenkov interaction as a function of  $\delta$ . The growth rate of the unstable mode increases with increase in the value of  $\delta$ , as observed in Figures 5 and 6 also. In this case, the growth rate increases as the number of dust grains are increased in the plasma, which is in contrary to the growth rate variation with  $\delta$  in case of cyclotron interactions. This is because more number of dust grains



Fig. 7. Growth rate  $\gamma_3(s^{-1})$  during Cerenkov interaction as a function of  $\delta$  for  $a = 1.2 \times 10^{-4}$  cm.

shield more plasma electrons, increasing the mobility of plasma ions. An increase in the number of fast ions leads to energy transfer from ions to the waves by inverse Landau damping.

## Conclusion

The streaming ions in a dusty plasma are capable of generating TG waves, via Cerenkov and cyclotron interactions. In the case of fast cyclotron interaction or normal Doppler resonance ( $\omega$  –  $k_z v_i = +\omega_{ci}$ , it follows from Eq. (13) that growth rate is positive, the streaming ions are unstable, and the amplitude of the wave increases along its direction of propagation. Conversely, for the slow cyclotron interaction or anomalous Doppler resonance ( $\omega$  $-k_z v_i = -\omega_{ci}$ , it follows from Eq. (14) that the growth rate is negative, that is, in this case the build-up is replaced by inverse Landau damping. The negatively charged dust grains decrease the growth rate during cyclotron interactions; however, the growth rate increases with the addition of dust grains in Cerenkov interaction. The process of dust charging encourages a highly damped wave of very small wavelength corresponding to the frequency  $\omega = -(i[\eta + \beta_1 + \beta_2]/\alpha)$  in the present model. Thus, the dust grains stabilize the TG mode in cyclotron interaction and excite the instability in Cerenkov interaction.

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