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# Short-run fluctuations and long-run growth with recursive preferences

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#### **Abstract**

What is the relationship between short-run fluctuations in economic activity and the long-run evolution of the economy? There is empirical evidence that more perturbed economies tend to grow less. Yet matching this evidence has proven challenging for growth models without market failures. This paper examines the relationship between short-term fluctuations and long-term growth within a complete-market economy featuring Epstein-Zin preferences and unbounded growth driven by human and physical capital accumulation. With these preferences, risk aversion and intertemporal elasticity of substitution are allowed to be independent of each other. When the model is plausibly calibrated, the relationship between the mean and variance of growth turns out to be negative. In most cases, the effect of fluctuations on welfare is found to be negative and sizable, even when the long-run effect on growth is positive.

Keywords: Volatility and growth; Epstein-Zin preferences; intertemporal elasticity of substitution; risk aversion

JEL Classification: D92; E22; E32; O49

# 1. Introduction

Traditionally, business cycle theory and growth theory have been treated as unrelated areas of macroeconomics. As endogenous growth theory developed in the late 1980s, it explored the idea of analyzing interactions between growth and business cycles, abandoning the traditional decomposition approach that defined cycles as deviations from exogenous trends.<sup>1</sup>

If we look at the data for the G7 countries, we see a negative relationship between the frequency and the amplitude of the business cycle and the average per capita growth, as shown in Figure 1. Figure 2 makes this effect even more explicit, showing the correlation between ten-year moving averages of per capita GDP growth and its standard deviation. The correlations, computed over twenty-year sliding windows, are mostly negative across all G7 countries.<sup>2</sup>

A wide empirical literature looks systematically at this relationship between economic fluctuations and long-term economic growth. The study by Ramey and Ramey (1995) set a benchmark in this respect. Based on a complete panel consisting of 92 countries covering a time horizon

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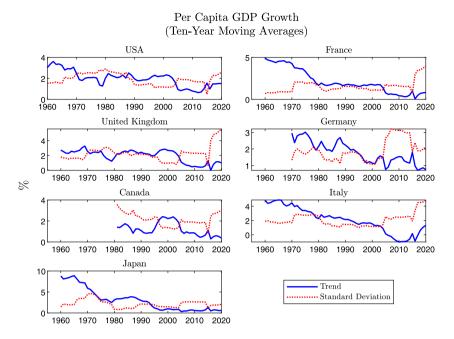
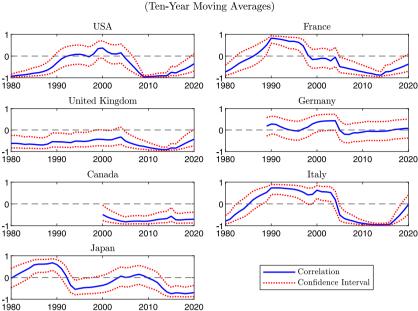


Figure 1. Growth and business cycles in G7 countries.

Source: Our elaborations on available yearly per capita GDP data for the period 1954-2019 across G7 Countries. The graphs show ten-year moving averages of per capita GDP growth and its standard deviation. Data source: World Bank Group (2023), World Development Indicators, retrieved from the Federal Reserve Bank of St Louis Data (FRED).

of 1960–1985, as well as a complete sub-panel of 24 OECD countries for the period 1950–1988, the authors show that countries with higher volatility in output, measured as the standard deviation of the growth rate, have significantly lower growth rates on average, even after controlling for key growth drivers. The effect has been broadly confirmed by later research, even if estimates vary considerably across empirical studies, being sensitive to the countries considered, the period examined, the nature of data, and the methodology employed. An overview of the empirical literature is in the meta-analysis by Bakas et al. (2019), to which we refer the interested reader.<sup>3</sup>

However, endogenous growth theory has experienced difficulties in generating a negative relationship between long-run growth and the variance of innovations assumed to drive business cycles. In fact, with standard constant relative risk aversion preferences (CRRA) when the degree of risk aversion is above one, as the micro evidence suggests, an increase in the standard deviations of shocks driving fluctuations causes an increase in precautionary investment, which is conducive to an increase in both long-run growth and its time variability (see De Hek, 1999, Canton, 2002 and Jones et al. 2005). Then explanations hinging on various frictions have been proposed for the negative relationship that the data seem to indicate: irreversible investment in machines or technology (as in Pindyck, 1991 and Ramey and Ramey, 1991), credit constraints making it impossible to exploit the reduced opportunity cost of innovating during slumps (Aghion et al. 2010), New Keynesian features (e.g. wage and price rigidities) because of which negative demand shocks cause a fall in real activity and reduced accumulation of tangible and intangible capital, not compensated by the increased accumulation during booms (Blackburn and Pelloni, 2004, Blackburn and Pelloni, 2005 and Annicchiarico and Pelloni, 2014). Other explanations go from intergenerational complementarities in education (Palivos and Varvarigos, 2013) and countercyclical markups leading to extrinsic uncertainty (Wang and Wen, 2011) to bad institutions and undisciplined governments (Loayza and Hnatkovska, 2004, Varvarigos, 2010, Fatás and Mihov, 2013).5



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Correlation Coefficient Per Capita GDP Growth and SD

Figure 2. Relationship between growth and business cycles in G7 countries. Source: Our elaborations on available yearly per capita GDP data for the period 1954-2019 across G7 Countries. The graphs show correlations between ten-year moving averages of per capita GDP growth and its standard deviation (SD). Correlations are computed over twenty-year sliding windows. Data source: World Bank Group (2023), World Development Indicators, retrieved from the Federal Reserve Bank of St Louis Data (FRED).

Recent literature has shown the usefulness of Epstein-Zin (EZ) preferences (see Epstein and Zin, 1989) in explaining standard asset pricing puzzles.<sup>6</sup> A key feature of these preferences is that the relationship between risk (RA) and intertemporal elasticity of substitution (IES) is not restricted to be reciprocal, as is the case with CRRA preferences. This generalization is attractive because it is unclear why individuals' willingness to substitute consumption across random states of nature should be so tightly linked to their willingness to substitute consumption deterministically over time.<sup>7</sup>

Since in modern economic theory asset prices are evaluated using marginal utilities, empirical evidence from asset markets can potentially guide the choice of preferences in macroeconomic analysis. EZ preferences have been incorporated into dynamic stochastic general equilibrium models to match basic asset pricing observations while maintaining good business cycle properties. A seminal paper in this stream of research is Tallarini (2000). More recent contributions are Van Binsbergen et al. (2012), Croce et al. (2012) and Kung and Schmid (2015).

This paper adds value by showing how EZ preferences can also be useful in theoretically investigating the relationship between business cycles and growth. To streamline the analysis and make the intuitive interpretation of our results more transparent, we introduce such preferences in a model specified to conform as closely as possible to the standard frictionless real business cycle model. More specifically, we adopt the framework in Jones et al. (2005), in which the accumulation of human and physical capital drives unbounded growth, while the source of fluctuations is a productivity shock.

We will see how the relationship between the dispersion of shocks and mean growth in the model depends on the interplay between the elasticity of intertemporal substitution and the coefficient of risk aversion. In particular, a negative relationship is obtained when the IES and RA are both high enough, as is the case under preference parameterizations widely used for calibration purposes and empirically supported. When we go back to CRRA preferences, constraining IES and RA to be the inverse of each other, this is not possible.

To explain our results intuitively, we can reason as follows: in a stochastic environment, agents will work more when the realization of the productivity shock is higher. The expected return to savings will then increase in the shock variance. However, the certainty equivalent of the return will be reduced by risk aversion. If RA is high enough, more volatile shocks will decrease rather than increase the certainty equivalent of the return on savings. However, this will reduce savings and growth only if the IES exceeds one, so the substitution effect prevails over the income effect when choosing current consumption.

Epaulard and Pommeret (2003) analyze the effect of the dispersion of productivity shocks on mean growth in a model with EZ preferences. Using an AK model with no labor, they show that the sign of the effect of a higher level of the dispersion on growth is exclusively governed by the IES and is, in fact, negative whenever the IES is larger than one, while risk aversion only influences the size of the effect. In our model, instead, the sign of the effect crucially depends on both risk aversion and the intertemporal elasticity of substitution. We trace back this substantial difference in results to the restrictive assumption in Epaulard and Pommeret (2003) that only physical capital, not labor, is needed for production. We drop this assumption and show that labor supply and the possibility of accumulating human as well as physical capital are important in determining how short-run fluctuations influence average growth.

Our results differ from those in Epaulard and Pommeret (2003) not only as regards the effects of shock volatility on growth but also as regards its effects on welfare, which in their analysis are always negative, while in our model can be positive, albeit only for very low levels of RA. The possibility of welfare increasing uncertainty is the central point of Cho et al. (2015) who look at the issue using a standard Ramsey model. Specifically, they assume CRRA preferences and strictly decreasing returns to capital, and they find that for very low values of RA agents can use uncertainty in their own favor. We show this is also possible with EZ preferences, although again, only for implausibly low levels of RA. With EZ preferences, higher volatility of the shocks is, in most cases, harmful even when it enhances long-run growth. This possible divergence of growth and welfare effects is also new in the literature. For instance, in an influential paper, Barlevy (2004) criticized the famous argument in Lucas (1987) that the welfare gains from reducing volatility in consumption are negligible by showing that fluctuations generate high welfare costs when they negatively influence growth because of diminishing returns to investment. We show that with EZ preferences, the welfare costs of fluctuations may be high, even when the shocks causing them positively affect long-run growth.

The remainder of this paper is structured as follows. Section 2 introduces the model, Section 3 presents our results, and Section 4 concludes.

# 2. The model

This section outlines the baseline stochastic endogenous growth model we use for our analysis. The model features optimizing firms, households with EZ preferences, human and physical capital investments, time-stationary technology subject to random shocks, and perfect competition in all markets.

The representative firm has the following production function:

$$Y_t = As_t K_{d,t}^{\alpha} L_t^{1-\alpha}, \ 0 < \alpha < 1, \tag{1}$$

where  $K_{d,t}$  is physical capital and  $L_t$  is demand for labor in efficiency units, A is a technological constant, while  $s_t$  introduces innovation into the model and is such that

$$s_t = \exp\left(\zeta_t - \frac{\sigma^2}{2\left(1 - \varphi^2\right)}\right),\tag{2}$$

$$\zeta_t = \varphi \zeta_{t-1} + \varepsilon_t, \ \varphi \in (0,1) \tag{3}$$

with  $\varepsilon_t \sim N$  (0,  $\sigma^2$ ). This parameterization implies that the levels of  $\sigma$  and  $\varphi$  do not affect the expected value of  $s_t$ . This will allow us to consider mean-preserving increases in the dispersion of shocks, as measured by the ergodic standard deviation of  $s_t$ . This is given by  $\left(\exp\frac{\sigma^2}{1-\varphi^2}-1\right)^{1/2}$  and is therefore increasing in both  $\sigma$  and  $\varphi$ . We can take this as a measure of uncertainty following use in the related theoretical literature.<sup>8</sup>

The final good is the numéraire, so its price is normalized to one. Let  $r_t$  be the rental price of capital and  $W_t$  the wage. Profit maximization then imposes:

$$r_t = \alpha A s_t K_{dt}^{\alpha - 1} L_t^{1 - \alpha} \tag{4}$$

and

$$W_t = (1 - \alpha) A s_t K_{dt}^{\alpha} L_t^{-\alpha}, \tag{5}$$

so as to determine the demand for physical capital and labor.

The representative household has the following Kreps-Porteus preferences in their EZ specification:

$$U_{t}\left(C_{t}, l_{t}\right) = (1 - \beta) u(C_{t}, l_{t}) + \beta \left(\mathbb{E}_{t} U(C_{t+1}, l_{t+1})^{\frac{1-\rho}{1-\rho}}\right)^{\frac{1-\rho}{1-\rho}}, \ 0 < \rho < 1,$$
 (6)

or alternatively:

$$U_{t}(C_{t}, l_{t}) = (1 - \beta) u(C_{t}, l_{t}) - \beta \left[ \mathbb{E}_{t} \left( -U(C_{t+1}, l_{t+1}) \right)^{\frac{1-\gamma}{1-\rho}} \right]^{\frac{1-\rho}{1-\gamma}}, \ \rho > 1$$
 (7)

where  $\beta \in (0, 1)$  is the discount factor, and  $u(C_t, l_t)$  is the period utility function with arguments consumption  $C_t$  and leisure  $l_t$ ;  $\rho$  is the inverse of the intertemporal elasticity of substitution, say  $\psi$  (i.e.  $\rho = \psi^{-1}$ ), and  $\gamma$  is the coefficient of relative risk aversion. See Swanson (2012, 2018). Standard Von Neumann-Morgenstern preferences constrain the risk aversion to be the inverse of the intertemporal elasticity of substitution (in our context, this would mean  $\gamma = \rho$ ), while with EZ preferences, these two parameters are allowed to take any positive value.

We assume that preferences are multiplicatively separable between consumption and leisure with a period utility function:

$$u(C_t, l_t) = \frac{C_t^{1-\rho} \left[ 1 - \chi (1-\rho) n_t^{1+\frac{1}{\eta}} \right]^{\rho}}{1-\rho},$$
(8)

where  $1 - \chi(1 - \rho) > 0$  for concavity,  $\eta > 0$  is the Frisch elasticity of labor supply and  $\chi > 0$  is a scaling parameter weighting the disutility from labor effort  $n_t = 1 - l_t$ . For non-recursive preferences, this specification of the period utility function was first proposed by Trabandt and Uhlig (2011) and is consistent with long-term growth. The fact that the Frisch elasticity of labor supply is captured by just one parameter, instead of changing with the level of consumption or labor supply, makes it easier to isolate its role in sensitivity exercises and to understand the importance of endogenous leisure choices in shaping our results. Note that if  $\rho < 1$ , marginal labor disutility is stronger if consumption is higher, while the opposite is true if  $\rho > 1$ .

The representative household accumulates not only physical capital (i.e. the final good) but also human capital  $H_t$  that increases labor efficiency. The two types of capital accumulate according to the following functions:

$$K_{t+1} = (1 - \delta_K) K_t + I_{K,t},$$
 (9)

$$H_{t+1} = (1 - \delta_H) H_t + I_{H,t}, \tag{10}$$

where  $I_K(I_H)$  denotes investment in physical (human) capital and the parameter  $\delta_K(\delta_H)$  measures the rate of physical (human) capital depreciation. The representative household then maximizes:

$$V_t = \max_{\{n_t, K_{t+1}, H_{t+1}\}} U_t \tag{11}$$

subject to the constraints in (9)-(10), given (8), the initial stocks of capital  $K_0$  and  $H_0$  as well as the following flow budget constraint:

$$W_t H_t n_t + r_t K_t = C_t + I_{K,t} + I_{H,t}. (12)$$

Epstein and Zin (1991) prove the existence and uniqueness of  $V_t$  when there is a single consumption good and no labor, which also applies if consumption and leisure form an aggregate good, as in the specification we adopt. Assuming that an interior and unique solution exists, the optimality conditions are then found to be:

$$C_{t} = \frac{W_{t} H_{t}}{\rho \chi \left(1 + \frac{1}{\eta}\right) n_{t}^{\frac{1}{\eta}}} \left[1 - \chi (1 - \rho) n_{t}^{1 + \frac{1}{\eta}}\right], \tag{13}$$

$$1 = \mathbb{E}_t \left[ M_{t+1} \left( 1 - \delta_K + r_{t+1} \right) \right], \tag{14}$$

and

$$1 = \mathbb{E}_t \left[ M_{t+1} \left( 1 - \delta_H + W_{t+1} n_{t+1} \right) \right], \tag{15}$$

where (13) determines labor supply, while (14) and (15) are the Euler equations referring to physical and human capital,  $^{12}$  with  $M_{t+1}$  being the stochastic discount factor in our economy, in turn, given by:

$$M_{t+1} = \beta \left\{ \frac{\left[ \left( \mathbb{E}_{t} V_{t+1}^{\frac{1-\gamma}{1-\rho}} \right) \right]^{\frac{1-\rho}{1-\rho}}}{V_{t+1}} \right\}^{\frac{\gamma-\rho}{1-\rho}} \left[ \frac{1-\chi(1-\rho)n_{t+1}^{1+\frac{1}{\eta}}}{1-\chi(1-\rho)n_{t}^{1+\frac{1}{\eta}}} \right]^{\rho} \left( \frac{C_{t}}{C_{t+1}} \right)^{\rho}, \ 0 < \rho < 1$$
 (16)

or by:

$$M_{t+1} = \beta \left\{ \frac{\left[ \mathbb{E}_{t} \left( -V_{t+1} \right)^{\frac{1-\gamma}{1-\rho}} \right]^{\frac{1-\rho}{1-\rho}}}{-V_{t+1}} \right\}^{\frac{\gamma-\rho}{1-\rho}} \left[ \frac{1-\chi(1-\rho)n_{t+1}^{1+\frac{1}{\eta}}}{1-\chi(1-\rho)n_{t}^{1+\frac{1}{\eta}}} \right]^{\rho} \left( \frac{C_{t}}{C_{t+1}} \right)^{\rho}, \ \rho > 1.$$
 (17)

If the labor market is in equilibrium,  $H_t n_t = L_t$ , while  $K_t = K_{d,t}$  is necessary to clear the capital market. Market general equilibrium requires these two conditions to be respected, together with the technology of production (1), the optimality conditions for the representative firm (4) and (5), and for the representative household (9), (10) and (12)-(15).

#### 3. Calibration and results

After calibrating the model and solving it using a second-order perturbation method as in Van Binsbergen et al. (2012), we will present the results for our baseline calibration and discuss their implications.<sup>13</sup> Next, we will do a sensitivity analysis to see what happens when we change some critical parameters. This will help us learn more about how the primitives of the model affect our results with a focus on preferences, in particular, risk aversion, the intertemporal elasticity of substitution in consumption and the Frisch elasticity of labor supply.

Table 1. Benchmark calibration

Fixed Parameters		
α	Share of capital	0.33
β	Discount factor	0.95
γ	Risk aversion (RA)	20
$\delta_{K}$	Capital depreciation rate	0.1
$\delta_H$	Human capital depreciation rate	0.04
η	Frisch elasticity	1
$\psi = \rho^{-1}$	Intertemporal elasticity of substitution (IES)	1.73
σ	Standard deviation of the shock	0.011
φ	Persistence of the shock	0.90
Implied Parameter	'S	
Α	Technological constant	0.75
χ	Leisure scaling parameter	32.32

#### 3.1. Calibration

To carry out the simulations, we calibrate the model by assuming a constant population and normalizing its size to one. This normalization ensures that all macroeconomic variables are expressed in per capita terms. We set the individual discount rate,  $\beta$ , equal to 0.95, which means that the duration of a period is equal to one year. For our benchmark simulation, we will set the IES,  $\psi = \rho^{-1}$ , equal to 1.73, as estimated by Van Binsbergen et al. (2012). This value is in between the one adopted by Bansal and Yaron (2004) and the one used in Croce et al. (2012) and Kung and Schmid (2015). As far as it concerns the parameter measuring RA,  $\gamma$ , we fix it at 20, which is an intermediate value between the standard value in the literature dealing with EZ preferences (e.g. Bansal and Yaron, 2004, Croce et al. 2012 and Kung and Schmid, 2015 who set it to 10 and the estimated value found in Van Binsbergen et al. 2012, which is around 66). <sup>14</sup> Finally, the Frisch elasticity,  $\eta$ , is set equal to one, which is an intermediate value in the range of macro and micro data estimates.

Turning to the production side of the economy, we set the capital share,  $\alpha$ , to 0.33, while, as in Jones et al. (2005), the depreciation rate of physical and human capital are set to 0.1 and 0.04, respectively. In our benchmark case, we want to achieve a steady-state growth rate for output, say  $g^Y$ , equal to 2%, and a labor supply, n, equal to 0.17. Note that  $g^Y$  is close to the annual growth rate of GDP per capita observed in US data for the period 1960-2019, which is 1.97%, according to World Bank data. To match these desired values we set A equal to 0.75 and  $\chi$  equal to 32.32. Finally, we assume that the standard deviation of the shock is equal to  $\sigma = 0.011$  and its persistence equal to  $\varphi = 0.9$ . With these values, we can fairly match the annual standard deviation of GDP per capita growth for the US in the period 1960-2019, which is around 1.94%, and its autocorrelation coefficient, which is around 0.14, while in the model, output growth exhibits a standard deviation of 1.938 and an autocorrelation coefficient of 0.122. The calibration is summarized in Table 1.

#### 3.2. Results

To analyze the effects of higher dispersion of the TFP shocks on growth, we adopt the standard procedure in the literature, that is, we calculate the unconditional mean of output growth,  $E(g^Y)$  implied by the model and compare  $E(g^Y)$  with its deterministic counterpart. In our benchmark simulation, we observe that the mean growth rate of the output is 1.86%, which is 14 basis

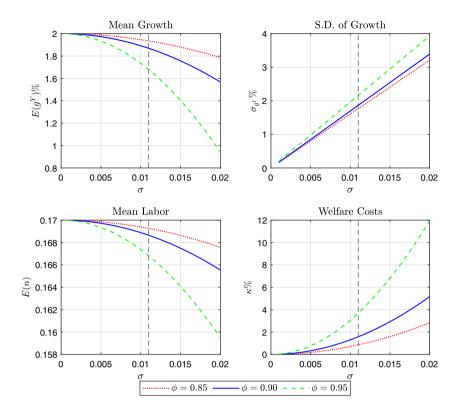


Figure 3. Volatility of shocks, growth, labor, and welfare costs. Note: The figure plots the unconditional means for output growth, its standard deviation (S.D.), the unconditional means for labor, and the welfare cost of volatility for different values of the technological shock volatility  $\sigma$ . The vertical lines refer to the baseline value set for  $\sigma$ . At the deterministic steady state,  $q^{\gamma} = 2\%$  and n = 0.17.

points lower than in a deterministic environment, where it is 2%. This is a remarkable result since, in traditional expected utility models, a mean-preserving spread in the TFP shocks leads to a higher mean and standard deviation of growth. With CRRA preferences, the intensity of the effect depends on the curvature of the utility function but is always positive for reasonable values of the intertemporal elasticity of substitution (see Jones et al. 2005). However, we show that this is a direct consequence of the artificial limitation the CRRA assumption imposes on preferences by constraining risk aversion to be the inverse of the elasticity of intertemporal substitution. With EZ preferences, this constraint, which lacks any clear rationale, is removed, and the negative relationship between growth and its volatility suggested by the data can be obtained.

In Figure 3, we plot the unconditional mean of output growth, its standard deviation, and mean labor E(n) for different values of the standard deviation of the innovation  $\sigma$  and of the autocorrelation coefficient  $\varphi$ . We also plot the welfare cost of increases in  $\sigma$ , which, following Epaulard and Pommeret (2003), is defined as an equivalent variation and, specifically, as the percentage of physical capital, say  $\kappa$ , an agent in a deterministic world is willing to give up at period t=0 to avoid moving to a stochastic one. In our benchmark calibration, this cost is around 1.7%. This cost represents a substantial welfare loss, consistent with the findings of Epaulard and Pommeret (2003) and Barlevy (2004). As can be seen from Figure 3, the loss of economic growth and welfare can be significant in the face of economic perturbations of the order of magnitude recently experienced in many countries. In

To explain our finding, we isolate five different effects: (i) the mean effect, (ii) the risk aversion effect, (iii) the labor welfare effect, (iv) the substitution effect, and (v) the income effect. The first two effects combine to determine how the certainty equivalent return to saving changes with uncertainty. The third effect captures the welfare cost of the fluctuations through changing labor supply. The last two effects determine the impact of the first three effects on investment (saving) decisions.

The mean effect arises as the expected return to savings increases in the standard deviation of the shocks. To understand why this may be the case, consider that a favorable realization of  $s_t$  makes output increase one-for-one, given the inputs. In addition, if agents adjust their choices depending on the realization, for instance, by working more when it is more productive to do so, output can increase further. Hence, an increase in productivity will raise output more than proportionally: the reduced form (equilibrium) production function and its first derivatives are then convex with respect to the shocks. Through Jensen's inequality, the expected return to savings will then increase in the volatility of the shocks.  $^{21}$ 

The risk aversion effect works in the opposite direction. Risk aversion means that the certainty equivalent of a gamble of a given expected value is lower, the higher the variance of the payoffs across states. Or, equivalently, uncertainty has a negative effect on the expected utility of future resources of a given expected value. As long as the risk aversion effect prevails over the mean effect, the certainty equivalent of returns to savings will decrease with the standard deviation of the shocks, reducing both welfare and the relative price between current and future consumption.

The labor welfare effect arises from the changes in the mean and variance of labor that a rise in uncertainty may induce, as the period utility is strictly increasing and strictly concave in leisure.

Finally, the relative force of the substitution and income effects will decide how the change in the certainty equivalent return to savings and the change in welfare through labor influences saving decisions. The substitution effect discourages saving when the certainty equivalent return to saving is lower. A negative income effect works in the opposite direction. When RA is high enough, the certainty equivalent return to saving is negatively affected by uncertainty. When the IES exceeds one, the substitution effect prevails over the negative income effect. This leads to higher initial consumption and lower savings, on average. It also leads to a lower mean labor supply. An intuitive explanation for this latter outcome is that, as shown before, when  $\rho < 1$ , labor disutility increases with consumption. This trumps the negative income effect, pushing the labor supply up.

#### 3.3. Sensitivity

In this section, we conduct some sensitivity analysis to assess the robustness of our findings and to gain deeper insights into the role of various features of the model in shaping results. We will also stress the differences in results with respect to Epaulard and Pommeret (2003) and Jones et al. (2005), and single out the mechanisms through which these differences emerge.

# 3.3.1. Risk aversion and intertemporal elasticity of substitution

Our first exercise consists of making the risk aversion  $\gamma$  take different values (ranging from 0.5 to 40) for six different values of the elasticity of substitution (from 0.1 to 2). Table 2 reports the unconditional means for output growth,  $E(g^Y)$  and labor, E(n), along with the welfare cost of fluctuations,  $\kappa$ , for each parameterization. When changing the IES, the parameters A and  $\chi$  are adjusted so that the steady-state growth rate remains equal to 2% and the labor supply equals 0.17.<sup>22</sup>

From the table, we see that the negative effect of an increase in the volatility of the shocks on growth is possible only if the IES is higher than one and if the RA is high enough, while if the IES is lower than one the effect is always positive.

	$\psi = 1.5$				$\psi = 1.73$			$\psi = 2$		
γ	$E(g^{Y})$	E(n)	κ	$E(g^{Y})$	E(n)	κ	$E(g^{Y})$	E(n)	К	
0.5	2.0388	0.1701	-0.1746	2.0510	0.1702	-0.1982	2.0694	0.1704	-0.2275	
2	2.0296	0.1701	-0.0324	2.0363	0.1701	-0.0511	2.0470	0.1702	-0.0758	
5	2.0112	0.1699	0.2515	2.0067	0.1698	0.2426	2.0022	0.1698	0.2273	
10	1.9805	0.1696	0.7236	1.9574	0.1694	0.7312	1.9275	0.1692	0.7315	
20	1.9191	0.1690	1.6632	1.8589	0.1686	1.7041	1.7782	0.1680	1.7360	
30	1.8577	0.1685	2.5968	1.7603	0.1677	2.6715	1.6289	0.1668	2.7355	
40	1.7963	0.1679	3.5245	1.6618	0.1669	3.6334	1.4795	0.1656	3.7298	
	$\psi=0.1$			$\psi = 0.5$			$\psi = 0.7$			
		$\psi = 0.1$			$\psi = 0.5$			$\psi = 0.7$		
γ	$E(g^{Y})$	$\psi = 0.1$ $E(n)$	κ	$E(g^{Y})$	$\psi = 0.5$ $E(n)$	κ	$E(g^{Y})$	$\psi = 0.7$ $E(n)$	К	
γ 0.5	E(g <sup>Y</sup> ) 2.0054	· ·	κ -0.0178	$E(g^{\gamma})$ 2.0108	<u>'</u>	κ -0.0758	E(g <sup>Y</sup> ) 2.0140	<u> </u>	κ -0.0969	
-		E(n)			E(n)			E(n)		
0.5	2.0054	E(n) 0.1700	-0.0178	2.0108	E(n) 0.1699	-0.0758	2.0140	E(n) 0.1700	-0.0969	
0.5	2.0054 2.0136	E(n) 0.1700 0.1700	-0.0178 0.0153	2.0108 2.0160	E(n) 0.1699 0.1700	-0.0758 0.0201	2.0140 2.0176	E(n) 0.1700 0.1700	-0.0969 0.0143	
0.5	2.0054 2.0136 2.0301	E(n) 0.1700 0.1700 0.1701	-0.0178 0.0153 0.0811	2.0108 2.0160 2.0265	E(n)  0.1699  0.1700  0.1701	-0.0758 0.0201 0.2114	2.0140 2.0176 2.0247	E(n)  0.1700  0.1700  0.1701	-0.0969 0.0143 0.2360	
0.5 2 5	2.0054 2.0136 2.0301 2.0575	E(n)  0.1700  0.1700  0.1701  0.1702	-0.0178 0.0153 0.0811 0.1898	2.0108 2.0160 2.0265 2.0440	E(n) 0.1699 0.1700 0.1701 0.1703	-0.0758 0.0201 0.2114 0.5285	2.0140 2.0176 2.0247 2.0365	E(n)  0.1700  0.1700  0.1701  0.1702	-0.0969 0.0143 0.2360 0.6040	

Table 2. Mean growth and labor, and welfare costs—the role of IES and RA

Note: The table reports the unconditional means for output growth and labor, and the welfare cost of volatility,  $\kappa$  (in %) for different values of the risk aversion (RA)  $\gamma$  and of the intertemporal elasticity of substitution (IES)  $\psi$ . For the triplet of values of  $\psi$ , {1.5, 1.73, 2}, the corresponding values of  $\gamma$ , above which mean growth goes below its deterministic counterpart, are {6.82, 5.68, 5.15}. At the deterministic steady state,  $g^{\gamma} = 2\%$  and g = 0.17.

An intuitive explanation for these findings is the following: when RA is low, the certainty equivalent return to savings will increase with the volatility of the shocks, pushing toward more savings and growth through the substitution effect, whose size is increasing in the IES. When RA is high, the certainty equivalent return to savings will decrease with the volatility of the shocks, pushing toward less savings and growth through the substitution effect; however, when the IES is below one, the negative income effect will prevail and push towards lower initial consumption, that is more growth. We also observe that more volatility of the shocks tends to push average labor and average growth in the same direction.

Our finding that an IES higher than one does not rule out the possibility of a positive effect on growth (or even welfare) goes counter to Epaulard and Pommeret (2003). In fact, they adopt a streamlined AK model and conclude that as long as the IES is higher than one, mean growth (and welfare) will always be lower than in the deterministic counterpart of the model. Our analysis shows that their conclusion no longer holds when their assumptions are relaxed to allow for endogenous leisure and for human capital as a factor of production. This difference between our results and theirs can be simply explained by recalling that in our model, agents can activate two margins of choice that are assumed out in Epaulard and Pommeret (2003): agents can distribute labor supply intertemporally and can invest relatively more in physical or human capital at different times. This activation makes for a positive mean effect. Absent these two margins of choice, more volatility in the shocks will induce a lower certainty equivalent return to savings for all levels of RA, which discourages growth when the IES is higher than one because the negative substitution effect prevails over the negative income effect. In our model, instead, if RA is low, the

mean effect can make for an increase in the certainty equivalent return to savings, leading to more savings and higher growth.

Another significant result from Table 2 is that, in most cases, uncertainty decreases welfare, whatever its effect on mean growth. The few exceptions occur when RA is very low. For higher RA, the certainty equivalent return to savings goes down with uncertainty, which directly negatively affects welfare. Moreover, the increased average and/or variance of labor also hurts welfare (the third effect we isolated). The fact that the changes in labor supply have a welfare cost may seem puzzling. If a higher and/or less stable path of labor hurts welfare, why choose it? The answer is that these labor choices are the best response to the underlying stochastic environment: without them, the certainty equivalent returns to saving would be lower. In other words, the welfare cost of fluctuations is not provoked by labor choices, but by the fact that the more volatile economic conditions induce those choices. Agents, given the uncertainty, will always be better off than they would be if their labor were constrained to stay at all times at the level that is optimal in a deterministic world. Still, this does not mean that uncertainty will make them better off.

Note that in Table 2 for  $\psi = 0.5(2)$  and  $\gamma = 2(0.5)$ , risk aversion and intertemporal elasticity of substitution are the inverse of each other so we are back to the standard CRRA specification of preferences. We can see that, as in Jones et al. (2005), under this assumption, the economy features mean growth higher than its deterministic value. We complement their analysis by also showing the effects on welfare, and interestingly, we find that the effect is negative despite the positive impact on growth.

All in all, our results confirm the intuition of Jones et al. (2005), that the parameters that govern the curvature of the utility function are crucial in determining the sign of the relationship between volatility and growth. However, with EZ preferences, we see that the relationship between volatility and growth depends on both the absolute values of RA and IES and on the ratio between the two values.

## 3.3.2. Labor-leisure choices

Our previous discussion highlighted the role of labor flexibility behind the mean effect. To clarify this role, we conduct two sets of exercises. First, we compute the unconditional means of output growth and labor when labor supply is fixed, second, we vary the Frisch elasticity of labor supply,  $\eta$  beyond and above unity, the baseline value. In both sets of exercises, we consider different values of risk aversion and the intertemporal elasticity of substitution.

We conduct our first set of exercises with the following question in mind. Does the mean effect only depend on the flexibility of the labor supply? To answer the question, we built Table 3, which presents results with a fixed labor supply, IES set to 1.73 or 0.5, and for the same range of values of RA as in Table 2. Comparing entries in Table 3 with those in the central columns of Table 2, we see that the impact of uncertainty on mean growth and welfare is always less favorable than when the labor supply can adjust. See also Figure A-6 of the online appendix. However, the effects can still be positive for growth and even for welfare (the latter case only arises for RA is 0.5). This implies that the difference in results with Epaulard and Pommeret (2003), described in the previous section, depends not only on the assumption in their model that labor is not a factor of production but also on the distinct assumption that there is only one kind of capital. Indeed, we have to qualify this statement. We have already seen that if the depreciation rate is the same for the two capitals, the optimal ratio between the two will be unaffected by uncertainty. However, when the capitals differ in terms of their rates of depreciation, uncertainty creates the possibility of exploiting this difference, for instance, by investing more in the capital which depreciates faster than one would in a deterministic environment, to make one's choice "less irreversible."

In our second set of exercises, we vary the Frisch elasticity of labor supply,  $\eta$ , and compute the unconditional means of output growth and labor for different values of risk aversion and two values of the IES. See Table 4. We see that as labor supply becomes more flexible, the impact of the

Table 3. Mean growth and labor and welfare costs with inelastic labor

	ψ =	= 1.73	$\psi=0.5$		
γ	$E(g^Y)$	К	$E(g^{Y})$	κ	
0.5	2.0146	-0.1276	2.0076	-0.0690	
2	2.0098	0.0194	2.0112	0.0269	
5	2.0001	0.3131	2.0184	0.2181	
10	1.9841	0.8014	2.0304	0.5352	
20	1.9521	1.7740	2.0544	1.1634	
30	1.9201	2.7410	2.0784	1.7837	
40	1.8881	3.7024	2.1024	2.3962	

Note: The table reports the unconditional means for output growth and the welfare cost volatility,  $\kappa$  (in %) for different values of the risk aversion  $\gamma$  and of the intertemporal elasticity of substitution  $\psi$ . For  $\psi = 1.73$ , the corresponding value of  $\gamma$ , above which mean growth goes below its deterministic counterpart is 4.11. At the deterministic steady state,  $g^{\gamma} = 2\%$  and n = 0.17.

Table 4. Mean growth and labor, welfare costs, and the frisch elasticity

$\psi=1.73$										
	$\eta = 0.5$				$\eta = 1$			$\eta = 1.5$		
γ	$E(g^{Y})$	E(n)	κ	$E(g^{Y})$	E(n)	κ	$E(g^{Y})$	E(n)	κ	
0.5	2.0337	0.1701	-0.1693	2.0510	0.1702	-0.1982	2.0659	0.1703	-0.2195	
2	2.0230	0.1700	-0.0222	2.0363	0.1701	-0.0511	2.0481	0.1702	-0.0724	
5	2.0016	0.1699	0.2715	2.0067	0.1698	0.2426	2.0124	0.1698	0.2214	
10	1.9661	0.1696	0.7600	1.9574	0.1694	0.7312	1.9530	0.1693	0.7100	
20	1.8949	0.1691	1.7328	1.8589	0.1686	1.7041	1.8342	0.1682	1.6831	
30	1.8237	0.1686	2.7000	1.7603	0.1677	2.6715	1.7154	0.1671	2.6506	
40	1.7526	0.1681	3.6617	1.6618	0.1669	3.6334	1.5967	0.1659	3.6126	
				ψ	= 0.5					
	$\eta = 0.5$			$\eta = 1$			$\eta = 1.5$			
γ	$E(g^{Y})$	E(n)	κ	$E(g^{Y})$	E(n)	κ	$E(g^{Y})$	E(n)	κ	
0.5	2.0117	0.1700	-0.0914	2.0140	0.1700	-0.0969	2.0159	0.1700	-0.1010	
2	2.0146	0.1700	0.0197	2.0176	0.1700	0.0143	2.0200	0.1700	0.0101	
5	2.0205	0.1700	0.2414	2.0247	0.1701	0.2360	2.0280	0.1701	0.2319	
10	2.0303	0.1701	0.6094	2.0365	0.1702	0.6040	2.0413	0.1703	0.5999	
20	2.0498	0.1703	1.3396	2.0601	0.1705	1.3342	2.0681	0.1706	1.3301	
30	2.0694	0.1704	2.0621	2.0838	0.1708	2.0568	2.0948	0.1710	2.0527	
40	2.0890	0.1706	2.7770	2.1074	0.1710	2.7718	2.1215	0.1714	2.7678	

Note: The table reports the unconditional means for output growth and labor, and the welfare cost of volatility,  $\kappa$  (in %) for different values of the risk aversion  $\gamma$ , of intertemporal elasticity of substitution  $\psi$  and of the Frisch elasticity of labor supply  $\eta$ . When  $\psi=1.73$  for the triplet of values of  $\eta$ , {0.5, 1, 1.5}, the corresponding values of  $\gamma$ , above which mean growth goes below its deterministic counterpart, are {5.23, 5.68, 6.05}. At the deterministic steady state,  $g^{Y} = 2\%$  and n = 0.17.

volatility of the shocks on growth, whether positive or negative, is amplified. Interestingly, *coeteris paribus*, welfare is always increasing in the Frisch elasticity in the sense that the welfare gains of fluctuations are amplified and the welfare costs reduced with higher Frisch elasticity across all the parameterizations we consider.

Finally, the magnitude of the mean effect also depends on the elasticity of output to physical capital,  $\alpha$ . As shown in Table A-1 of the online appendix, a higher  $\alpha$  implies a production function that is more concave in labor. Consequently, the mean effect becomes weaker, requiring a lower risk aversion level to generate a negative impact on growth. In general, the higher  $\alpha$ , the less favorable the effects of more uncertainty on growth and welfare, no matter whether the IES is higher or lower than one.

#### 4. Conclusion

There is convincing evidence that higher frequency and amplitude of fluctuations are related to lower long-term growth. The theoretical literature has only been able to reproduce this evidence by relying on various kinds of institutional or market failures. However, this paper demonstrates that this stylized fact can be easily replicated in a frictionless endogenous growth model where agents have Epstein-Zin preferences.

Our simulations agree with the conclusion in Jones et al. (2005) that the relationship between business cycles and long-term growth depends on the concavity of the utility function. However, adopting Von Neumann-Morgenstern preferences means constraining risk aversion and intertemporal elasticity of substitution to be the inverse of each other. As the former parameter is generally assumed to be above unity, this characterization of preferences may bias the results toward finding that business cycles are good for growth. Conversely, we have found that when risk aversion and elasticity of intertemporal substitution are disentangled, short-run fluctuations can be detrimental to growth. An interesting further result is that even when the effect of fluctuations on growth is positive, the impact on welfare will often be negative.

From this perspective, our results uncover a further potential channel for the observed negative relationship between business cycle and growth in addition to the various market failures already explored in the literature. We have adopted a deliberately streamlined model to allow a close analysis of the role of risk aversion and the elasticity of substitution in conditioning this relationship. In future work, we plan to use the results of this scrutiny to further investigate this issue by introducing in the model features such as downward wage rigidities and irreversible investments to improve the empirical properties of the model.

**Supplementary material.** The supplementary material for this article can be found at https://doi.org/10.1017/S1365100524000336.

**Competing interests.** The authors declare none.

#### **Notes**

- 1 The abandonment of the tradition has been gradual. The evidence that movements in the GDP tend to be permanent led to the development of real business cycle models, where stochastic technological variations induce fluctuations. Incorporating a mechanism for unbounded growth opens up the possibility that the distribution of these variations affects long-run growth (see, e.g. Blackburn & Pelloni, 2004).
- 2 Using five-year moving averages yields similar results, as shown in the online appendix. See Figures A-1 and A-2.
- 3 Ramey and Ramey (1995) pointed out that it is important to distinguish between the realized volatility of growth (a backward-looking variable) and uncertainty about future volatility (a forward-looking variable), as the latter notion corresponds more closely to that of uncertainty in most macroeconomic theories of stochastic growth. In these theories, uncertainty stems from unpredictable shocks to fundamentals and an increase in uncertainty is then generally defined as a mean-preserving spread in these shocks. See Acemoglu (2008) or Cho et al. (2015). Unfortunately, to quote Bloom (2014)

"uncertainty is an amorphous concept," which cannot be immediately read from the data. In trying to pin down the effect of uncertainty on growth Ramey and Ramey (1995) investigate the relationship between growth and the variance of innovations to a forecasting equation for growth, again finding a negative link between the variables. In many of the papers in the subsequent literature using time series data, the volatility of innovations is modeled as a conditional variance process within an ARCH or GARCH framework. Comprehensive measures of uncertainty have subsequently been built by looking at the forecast errors of systems of forecasting equations for a wide range of macroeconomic and financial variables, while other proxy variables for uncertainty have also been proposed, among them stock volatility, disagreement among professional forecasters, and the dispersion of productivity shocks to individual firms, (see, e.g. Jurado et al. 2015, Bloom et al. 2018, Angelini et al. 2019, and Ludvigson et al. 2021). These measures have been proven to correlate with economic activity in important ways. See, for example Bloom (2014) and Fernández-Villaverde and Guerrón-Quintana (2020). In particular, in Jovanovic and Ma (2022), a rise in uncertainty negatively affects mean growth and is positively correlated with growth volatility.

- 4 This is also the case in the presence of idiosyncratic uninsurable risk, as shown by Krebs (2003).
- 5 For a survey of the theoretical literature, see Priesmeier and Stähler (2011). The incorporation of real and nominal rigidities in endogenous growth models, as in Comin and Gertler (2006), has also been used in the years following the Great Recession of 2008-2009 to explain the protracted deterioration of growth prospects in the US and many developed countries (e.g. Benigno and Fornaro, 2018, Anzoategui et al. 2019, Bianchi et al. 2019 and Cozzi et al. 2021 among others). Annicchiarico and Pelloni (2021) and Garga and Singh (2021) study optimal monetary policy in related setups.
- 6 A leading contribution is Bansal and Yaron (2004).
- 7 With EZ preferences, a high risk aversion, consistent with a large risk premium, can coexist with a small aversion to intertemporal inequality (inverse of IES) as consistent with a small risk-free interest rate.
- 8 In the rest of the paper "volatility of the shocks" is taken to mean the same as "uncertainty." In this, we follow our closest antecedents in the literature, for example Jones et al. (2005).
- 9 Note that to express preferences, we have started from the formulation of Swanson (2018). Usually, EZ preferences are expressed as

$$\tilde{U}_t\left(C_t, l_t\right) = \left[ (1-\beta) \ \tilde{u}(C_t, l_t)^{1-\rho} + \beta \left(\mathbb{E}_t \tilde{U}(C_{t+1}, l_{t+1})^{1-\gamma}\right)^{\frac{1-\rho}{1-\gamma}} \right]^{\frac{1}{1-\rho}}.$$

It can be seen that by setting  $U = \tilde{U}^{1-\rho}$  and  $u = \tilde{u}^{1-\rho}$  for  $0 < \rho < 1$  and  $U = -\tilde{U}^{1-\rho}$  and  $u = -\tilde{u}^{1-\rho}$  for  $\rho > 1$ , the above specification corresponds to (6) and (7).

10 The restriction  $1 - \chi(1 - \rho) > 0$  must hold; otherwise, the marginal utility of consumption could be negative for low leisure values. For a proof of the strict concavity in  $C_t$  and  $l_t$  of the periodic utility function in (8), see Annicchiarico et al.

- (2022).

  11 In fact,  $\frac{\partial^2 U}{\partial C} = C^{-\rho} \left[ 1 \chi (1-\rho) n_t^{1+\frac{1}{\eta}} \right]^{\rho-1} \frac{\rho \chi(\rho-1) n_t^{\frac{1}{\eta}}}{1+\frac{1}{\eta}}$ .

  12 Notice that if  $\delta_H = \delta_K$  the ratio between human and physical capital will be fixed at  $\alpha/(1-\alpha)$ . In fact, equating (14) and (15) after plugging in the first (4), in the second (5) and reordering we obtain  $K_{t+1}/H_{t+1} = \frac{\mathbb{E}_t \left[ M_{t+1} \left( \alpha A s_{t+1} n_{t+1}^{1-\alpha} \right) \right]}{\mathbb{E}_t \left[ M_{t+1} (1-\alpha) A s_{t+1} n_{t+1}^{1-\alpha} \right]} = \frac{1}{2} \frac{1}$  $\alpha/(1-\alpha)$ . Of course  $K_{t+1}$  and  $H_{t+1}$  are choice variables and as such known at t. However if  $\delta_H \neq \delta_K$  there is no closed

form solution for the optimal  $K_{t+1}/H_{t+1}$  implicitly given by:  $K_{t+1}^{\alpha}H_{t+1}^{-\alpha}\left(-\alpha K_{t+1}^{-1}H_{t+1}+1-\alpha\right) = \frac{\mathbb{E}_{t}M_{t+1}(\delta_{H}-\delta_{K})}{\mathbb{E}_{t}M_{t+1}As_{t+1}\eta_{t-1}^{1-\alpha}}$ . From this formula, we see that if  $\delta_{H} - \delta_{K} > 0$ , then  $K_{t+1}/H_{t+1} > 0$  implies  $K_{t+1}/H_{t+1} > (1-\alpha)/\alpha$  while if  $\delta_{H} - \delta_{K} < 0$  we will have  $K_{t+1}/H_{t+1} < (1 - \alpha)/\alpha$ .

- 13 The model has been solved with Dynare. See Adjemian et al. (2023).
- 14 For other recent estimates of the parameters with EZ preferences, see, e.g., Chen et al. (2013), Bollerslev et al. (2015), Schorfheide et al. (2018) and Pohl et al. (2021).
- 15 World Bank, Constant GDP per capita for the United States [NYGDPPCAPKDUSA], retrieved from FRED, Federal Reserve Bank of St. Louis; https://fred.stlouisfed.org/series/NYGDPPCAPKDUSA, January 28, 2024.
- 16 However, even when solved at third-order approximation, the model fails to capture the observed excess of kurtosis (3.440) and skewness (-0.6180) in GDP per capita growth data. To capture these statistical properties, the model should incorporate frictions, such as downward wage rigidities or imperfect credit markets, able to amplify business cycle fluctuations and introduce a source of asymmetry. We leave these extensions for future research.
- 17 As seen in the previous section, we take steady-state values for growth and labor as suggested by the data. It would have been possible to calibrate the model in such a way that the unconditional mean of growth, not the deterministic growth rate, matched the data. However, the first route is generally used in the literature, and thus, opting for it makes for easier comparability of results.
- 18 Note that, in the spirit of Lucas (1987), the welfare cost of business cycles is usually expressed in consumption-equivalent units (i.e. the fraction of consumption an agent is willing to give up at all dates to live in a deterministic world). However, in a model with endogenous growth, the trend in the consumption process may differ due to changes in the agent's propensity to consume when transitioning from a deterministic to a stochastic environment. In this case, a welfare cost based on consumption units is no longer informative.

- 19 In the online appendix, we show the counterpart of Figure 3 for CRRA preferences. It shows that, in line with Jones et al. (2005), mean growth is always higher than its deterministic counterpart and rises as shocks become more volatile. See Figure A-5.
- 20 This is shown in the online appendix, where we plot the impulse response functions following a positive realization of the technological shock. See Figures A-3 and A-4.
- 21 Cho et al., (2015), whose terminology we have partially followed, consider the mean and fluctuations effects (our RA effect) to study the welfare cost of business cycles. If the mean effect prevails, the indirect utility function will be convex in shocks, and higher volatility will raise welfare.
- 22 Other experiments can be considered, such as anchoring all the scale parameters to their baseline values and letting the steady-state values of growth and labor change consistently with different intertemporal elasticity of substitution. The results, however, do not change qualitatively with this alternative approach. These findings are available on request.
- 23 This is further explored in the online appendix, in Table A-2. The depreciation rates of human and physical capital further influence the mean effect. When the substitution effect dominates the income effect, for  $\gamma$  set to its baseline value, higher depreciation rates lead to a stronger negative effect on mean growth. This is because faster depreciation implies shorter lifespans for capital stocks, limiting the duration of the mean effect. Conversely, for low IES, since the income effect tends to dominate over the substitution effect, higher depreciation rates incentivize households to accumulate even more capital, ultimately amplifying the income effect.

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