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Influencers in design teams: a computational framework to study their impact on idea generation

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Abstract

It is known that wherever there is human interaction, there is social influence. Here, we refer to more influential individuals as "influencers", who drive team processes for better or worst. Social influence gives rise to social learning, the propensity of humans to mimic the most influential individuals. As individual learning is affected by the presence of an influencer, so is an individual's idea generation . Examining this phenomenon through a series of human studies would require an enormous amount of time to study both individual and team behaviors that affect design outcomes. Hence, this paper provides an agent-based approach to study the effect of influencers during idea generation. This model is supported by the results of two empirical experiments which validate the assumptions and sustain the logic implemented in the model. The results of the model simulation make it possible to examine the impact of influencers on design outcomes, assessed in the form of exploration of design solution space and quality of the solution. The results show that teams with a few prominent influencers generate solutions with limited diversity. Moreover, during idea generation, the behavior of the teams with uniform distribution of influence is regulated by their team members' self-efficacy.

List of symbols

$f(x)$ A multi-dimension function that computationally represents the design problem, where each dimension denotes a design variable " x " is an n -dimensional array $(x_1, x_2, x_3,, x_n)$. M The size of a matrix (in this case 2D) that represents asolution space. D The distance between the random point (x_1, x_2) and the nearest best solutions on a solution space. $O(z')$ An agent's energy to explore solution space, where z' is the normalized length of the session. σ The shape parameter that affects the overall shape of the curve that governs an agent's energy to explore solution space. c The energy value when the session starts $S(d')$ The magnitude of the learning vector from a positive event, where d' is the normalized value of the similarity between the recalled and current agent's solution. α Position of the peak when learning from the positive experience E E Agent domain-expertise level τ τ The height of the peak when learning from the positive experience Δt n The current session number of an agent S_n S_n The session number of an agent S_n N' The given number of sessions in a project \vec{v}_s'
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\vec{v}_s The learning from positive experience vector
\vec{v}_k The initial knowledge state vector of an agent
$\vec{v_n}$ The resultant learning vector from the $\vec{v_s}$ and the $\vec{v_k}$
I The Influence value
SE The self-efficacy of an agent
ΔSE The difference in the self-efficacies of the two agents
T Trust between the two agents
$w_1, w_2, w_3,$ The weights that were decided after the empirical studies
w_4 , and w_5

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R	The reputation of an agent
N _a	The number of solutions of an agent that
	wereaccepted by the controller agent
Np	The total number of the solutions proposed
1	by an agent
f	The familiarity between the two agents
\vec{v}_I	The total amount of learning by an agent
	from its peers
$\vec{v}_{n'}$	The amount of learning an agent does
	while generating solutions
EI	Exploration index
solns _{lowr}	The unique number of solutions explored
	on a reduced resolution of the solution space
Area _{lowr}	The reduced resolution solution space area
EQI	Exploration quality index
t	Threshold taken to determine EQI
solns _r	The number of solutions generated that are
	greater than t on a reduced resolution
	solutionspace
totSoln _r	The total number of solutions that are
	present in the solution space that are
	greater than t

Introduction

Many companies and organizations rely on collaborative work for better project outcomes, and there is a need for workers to have adequate knowledge and skills related to design team collaboration that will give them a competitive edge. Several factors at the individual, project, or organizational level act as barriers in design team collaboration (Kleinsmann and Valkenburg, 2008). More and more emphasis is being given to study the design process at an individual level, and how social and cognitive factors could contribute to the final design output. One such social factor, social influence, gives rise to influencers who affect the cognition of other individuals during a collaborative activity. Thus, the study explores the impact of these influencers on design outcomes.

Often in teams where there are no appointed leaders, the "charismatic" individuals can make others follow them in their decisions, opinions, and judgements. Social influence is responsible for the imitation nature in humans or, in other words, humans learn from social experiences; in this paper, this is referred to as social learning. Though there are a variety of different types of social learning, the paper focuses only on imitation type (Whiten *et al.*, 2009). According to social learning theory, people learn from their social environment through interactions (Bandura, 1977a), while in social cognitive theory, they learn passively from the social environment by observing others (Bandura, 1986). Since both, the above-mentioned phenomena are considered for the study, social learning is used interchangeably with social influence (as an individual imitates and learns most from those who influence them most).

Collaborative design teams can be viewed as social networks, but the role of influencers in small teams is still underexplored. While it is important to study the interactions in such collaborative teams (Paulus, 2000) and it requires a tremendous amount of time and effort (Becattini *et al.*, 2019). Therefore, the current work investigates the effect of influencers on design outcomes through agent-based modeling. Specifically, the current work deals with an agent-based approach for simulating idea generation in collaborative design teams (flat teams where participants contribute as equals without an overt hierarchical structure). Besides investigating the effect of influencers on individual thinking during idea generation, it also provides a novel approach to simulate learning in multi-agent systems. The effect of influencers in design teams has not been studied in past, thus the work could provide initial steps toward team management strategies to project managers, leaders, scrum masters, and others in similar roles.

The structure of the paper consists of the introduction section comprising the related work, identified research questions, and related hypotheses followed by the contribution of the current work. The section is followed by the model description along with the past theories and work on which the model is grounded are mentioned. The empirical study section briefly describes the real-world experiments and the results obtained from them, used for further tuning the model. The results from the model simulation show and discuss how influencers affect design outcome in terms of quality and exploration of ideas. The paper ends with a conclusion that provides a summary of the paper along with the limitations and future goals.

Background

Interaction between individuals in a collaborative activity gives rise to social influence (Myers, 1982). Social influence is the process where individuals change their behavior, attitudes, and opinions in the presence of social interaction. It is already known that social influence affects group brainstorming (Paulus and Dzindolet, 1993) and the magnitude of social influence is not evenly distributed across members of a team (Brown and Pehrson, 2019). In social network research, "influencers" is defined as "key individuals who have many people following them, they promote companies' product and are motivated to adopt new information or product" (More and Lingam, 2019). Similarly, in the context of the paper, influencers are individuals who have more capacity to influence their teammates than others (Aries *et al.*, 1983).

Cognitive processes occurring during brainstorming are known to be affected by social influence (Paulus and Dzindolet, 1993). Nowak *et al.* (1990) simulated a population of individuals having different opinions. These simulated individuals affect each other (based on social impact theory) and at the end of the simulation, a stable configuration of opinion was obtained. Another dynamic model of social factors in brainstorming was presented by Brown and Paulus (1996), where the model was based on idea generation, idea memory and idea output, taking into account the effects that group member exerts on each other's idea generation. Moreover, it was found that individuals tend to mimic the performance of their co-workers due to social comparison (Paulus and Dzindolet, 2008). Though it is clear that social influence affects creativity, the effect of the unequal distribution of social influence observed in practice is still unclear.

The dynamic nature of the influence arising from the interaction among individuals in a collaborative activity can be challenging to study using traditional human subject research. Agent-based modeling has been used in many other domains to infer and predict the behavior of complex systems as in the domains of social sciences, biology, air traffic, and many more (Abar *et al.*, 2017). Therefore, one of the broader contributions of this agent-based model would be to assist future researchers by providing a faster approach to study the design collaboration process. The use of agent-based modeling in the design team domain is a relatively new computational approach to model the dynamic phenomenon. It is used to model human behavior and interactions quickly and conveniently, where each agent models a human being, and they exhibit characteristics such as memory, learning, and adaptation (Bonabeau, 2002). The agents in the model behave according to the pre-defined rules to fulfill the purpose of the model. Simulating artificial humans in a collaborative idea generation session involves many parameters (Salas et al., 2005). Considering all the parameters may be costly (in terms of computational time and resources) and complicates the model, therefore researchers in the past including the current work (Singh et al., 2019) have considered the ones that contribute directly to their goals. While some authors focused their computational models on the conceptual design phase (Green, 1997; Cvetković and Parmee, 2002; Ehrich and Haymaker, 2012), others created models to study distributed team coordination (Carley, 1996; Carley and Gasser, 1999; Lee and Lee, 2002) and multidisciplinary teams (Maher et al., 2007; Hulse et al., 2019). Researchers have studied and simulated specific aspects of design activity, such as problem-solving (McComb et al., 2015, 2017) and team-related attributes (Gero and Kannengiesser, 2004; Singh et al., 2011; Perišić et al., 2018). Although many studies have considered individual attributes, such as the choice of partners or cognitive style (Hinds et al., 2000; Lapp et al., 2019) and social attributes like mental models have been modeled in the past (Singh, 2009), the effect of social influence on idea generation outcomes has not been explored.

Unlike the current trend toward studying the influencers in social media, the aspect of influence that occurs during design team collaboration has not been given much attention. Though the effect of social influence on brainstorming has been studied, its uneven distributed nature in the teams where some individuals tend to be more influenced or influential than others is still not explored. The study in this paper would investigate how the magnitude and distribution of influence affect idea generation outcomes. Specifically, the workseek to answer this research question:

What is the effect of influencer(s) on idea generation outcomes (exploration and quality)?

The idea generation outcomes include the quality (i.e., utility or usefulness) of the solutions (Shah *et al.*, 2003) and exploration (i.e., the number of unique alternative solutions agents generate before communicating to others in the team) of the design space (Ball *et al.*, 2001; Dorst and Cross, 2001). The explored values are also evaluated based on the diversity in them, referred to as variety, and explored solution quality called the exploration quality index (these metrics are explained more in the section "Model results and discussion").

However, before addressing the research question, it is first crucial to determine what makes an influencer. Although researchers have studied the characteristics of social media influencers, little is known about the characteristics of influencers in design teams. The work examined the past studies on group behavior, leadership studies, and team dynamics, to hypothesize some underlying influencer characteristics. Baker (2015) claimed that individuals' personality, skills, and communication could result in such a phenomenon. Since communication is often influenced by one's confidence state, *self-efficacy* was one of the individual attributes that were considered. This assumption was made based on the common observation where the more confident individuals are the ones governing the team (Bandura 1977b). It is known that self-efficacy is one of the important factors that

are responsible for transformational leadership improving team performance (Pillai and Williams, 2004), it is unclear how it might affect the degree of influence in teams. The other intrapersonal attribute that was chosen was *trust*, which arises from how well the two individuals have known each other previously that could also contribute to influencing power (Granovetter, 1973). Therefore, for this investigation, it was believed that self-efficacy (an individual's belief in his or her capacity to achieve goals) and trust could contribute to the influencer effect. Considering these two factors (self-efficacy and trust), an assumption was made to identify the influencers to address the above research question.

Assumption: Self-efficacy and trust are characteristics that determine how individuals' perceived degree of influence by others in the team.

To summarize, the main contribution of the work lies in the attempt to build a computational framework that could simulate social influence in collaborative design activities. Besides, providing insights into the popular approach of collaborative group design, the work would also assist researchers and practitioners with a faster method to study collaborative processes. Moreover, the uneven distribution of social influence that gives rise to influencers in the design team has been studied neither empirically nor computationally before. The characteristics and qualities, which give rise to the influencer effect in design teams, are investigated here. Additionally, the work provides a novel approach in stimulating learning in design teams (by considering appropriate model features such as design task, learning from past experience and influencer) is described in the next section. Lastly, the work also presents fresh a way to measure artificial creativity (especially in terms of exploration as explained in the "Model results" section).

The flow of the research is provided in Figure 1. The empirical studies were done after the initial model development was completed based on literature and assumptions. The computational model approximates the real-world system due to which it needs verification and validation. The empirical study section provides an overview of how some of the logics used in the model were verified as well as the assumption was validated. From the results of the empirical studies, the general idea of the results clarifying the assumptions and variable relationships were implemented in the model and not the exact coefficients (since the experiments were done in different settings, implementing exact results would not be appropriate).

Model description

The design project schema used in this paper is shown in Figure 2 (Singh *et al.*, 2019). As shown in Figure 2, a design collaboration activity starts in the form of a project. Each project has a set of design agents and a controller agent (analogous to a project leader, manager, or others in a similar role) who is responsible for assigning the task, evaluating the solution quality and providing feedback to the team. The project consists of several sessions of idea generation and idea selection before receiving feedback on their proposed solution from the controller agent for that session. Each idea generation event consists of several cognitive steps before proposing a solution to the team. These steps are analogical to the designer exploring alternative solutions (Ball *et al.*, 2001): moving from one point (solution) to another on a design space forms a step. Inspired by this notion, the work in this paper focuses on idea generation.



The design task

The definition of the design task is critical as it drives many aspects of the simulation while having a resemblance to the real world. Design teams are often not immediately aware of the quality of their solution and proceed by trial and error; this is especially true when the designers start working and they have no past experience. In this aspect, design tends to resemble a search task with a fixed design space and variables rather than a mathematical optimization problem. A design task typically has a certain number of design variables for which values are selected and combined to generate unique solutions. Furthermore, it is often the case that the quality of these solutions varies with changes to the constituent variable values. Generally, there are many below-average solutions with a few solutions that have the highest value. These characteristics of real-world design tasks were emulated in the construction of the computational design task solved within the model. Agents interact with the task through trial and error, searching for a solution with high quality. The design variables are continuous in nature and result in a continuous definition of solution quality.

The computational representation of a design problem has been adopted in many design research (Green, 1997; Cvetković and Parmee, 2002; Gero and Kannengiesser, 2004; Ehrich and Haymaker, 2012; McComb *et al.*, 2015). Some of the design tasks used in previous work are represented as binary functions (Schreiber *et al.*, 2004). Design tasks that are represented as binary

Fig. 2. The focus of the study is shown in the green box.

functions often have extreme solution values (i.e., immediately next to the best solution, there is the worst solution). This is an inaccurate representation of the more stable design tasks seen in the real world. This was taken into account while mathematically representing the solution space for this work. The design solution space is modeled in such a way that there is a gradual slope between the best and worst solutions, hence the subtle decrease in the hues around the best solution values (examples can be seen from Fig. 3). Similar to the real-world design problems, some noise was added to the objective function so that the probability of having the best and the worst solution next to each other is not completely eliminated and the design problem could have multiple best solution. The design problem can be computationally represented in multi-dimension that is composed of a landscape function f(x) [see Eq. (1)] and the given number of best solutions (maxima or peaks). The landscape function draws the desired shape around the given number of maxima. Here, x in f(*x*) is an *n*-dimensional array $(x_1, x_2, x_3, ..., x_n)$ of design variables. The landscape function f(x) constructs the slopes around the given number of peaks. The following general assumptions were made regarding the design solution space for this model.

• There is a limited number of n design variables each ranging within a definite interval (unknown to the agents). The design space is represented by all the combination of values of these n variables. For initiation, simplification, and visualization

 $\begin{array}{c} 0 & 20 & 40 & 60 & 80 \\ 20 & 40 & 60 & 80 \\ 20 & 40 & 60 & 80 \\ 40 & 40 & 60 & 80 \\ 40 & 40 & 60 & 80 \\ 40 & 40 & 60 & 80 \\ 40 & 40 & 60 & 80 \\ 40 & 40 & 60 & 80 \\ 40 & 60 & 60 & 60 \\ 40 & 60 & 60 &$

Fig. 3. Examples of design solution space with a different number of best solutions (peaks in lighter hue) and a side bar showing solution values. The last image shows an example of a 3D projection of a design space with five peaks.

purposes, two variables (n = 2) are chosen to represent the design problem. However, for future work, it could be extended to multiple dimensions.

• Each point on the *n*-dimensional surface defines a potential solution to the design problem and can be evaluated to yield a quality value. The agents do not know the values of f(x) for any solution of the design space before the start of the project; however, they are aware of the limits of the solution space.

The design space could be changed with relatively small effort based on the shape (gradient around the maxima), the number of peaks (number of maxima), and the distance between the peaks. The results of the design outcome presented in the paper are related to five peaks. The design solution space has a maximum value of 1 (lightest hue) and a minimum of 0 (darkest hue), as shown in an example in Figure 3 with several local maxima and minima.

$$f(x) = \frac{1}{\left(1 + e^{\left((1/\sqrt{M})D - 2\right)}\right)},\tag{1}$$

where *M* is the size given to represent the solution space in a 2D matrix. In this case, M = 100, such that the solution space was represented as a 100×100 matrix. *D* represents the distance between the random point (x_1, x_2) and the nearest best solutions. The number of best solution or the peaks are specified at the beginning of the simulation.

A similar design problem representation was used by Lapp *et al.* (2019) when simulating teamwork based on a different cognitive style where the amplitude of their objective function (peaks) affected exploration. Other studies in problem-solving like Dionne *et al.* (2010) and Sayama *et al.* (2010) also used a similar 1D and 2D representation of the problem with peaks and valleys.

Generating solutions

In order to simulate artificial humans, learning is an important feature to implement in the model. For example, studies have been done where agents learn collectively (Wu and Duffy, 2004), socially using mental models (Singh, 2009), or to simulate curiously in agents (Saunders and Gero, 2004). Most of the models described in the literature deal with some form of learning in their agents to accomplish the purpose of their work. The most common logic implemented in many models listed above is in the form of learning from experience (McComb, 2016; Lapp *et al.*, 2019). However, while simulating learning it is often assumed that the agents are aware of the design solution space and they thrive for the optimal solution (McComb *et al.*, 2017).

This works perfectly when the goal of the model is to find the optimal solution depending on the configuration of its parameters. On the other hand, the model presented in this paper aims at mimicking a collaborative idea generation session where the design solution space is unknown to the agents in a way that is similar to a real brainstorming scenario, but at the same time, the individuals (agents in the model) are aware of the boundary conditions. To model thinking in design teams, the authors have taken inspiration from Stempfle and Badke-Schaub (2002), where the basic thinking model consisted of exploration, generation, comparison, and selection. Keeping this in mind, the design agents explore the design space, generate solutions, compare it with the solutions they generated in the past and eventually select one to propose to the team. When an agent moves from one point to another in a design solution space, it is analogous to an individual formulating consequent thought during idea generation. The trajectory formed by connecting these points (thoughts) represents the overall process followed by an agent.

In order to learn, the agents explore the design solution space. Every time an agent stops at a point on the design solution space, that point is treated as the agent's selected solution. As mentioned before, the paper only deals with the results related to individual thinking during idea generation in design teams, however, the team interaction (proposing ideas, combining, and decision-making) that are occurring in the backend are not described in the paper and do not impact the results presented here. Idea generation is simulated in agents based on the following features, each of which is explained in more detail in the subsequent sections:

- Agent'sway to explore solution space
- Memory to store past experiences
- Recall capability
- Ability to learn from failure and successful past experience
- Influence of the influencer(s) (as explained in the "Background" section)

Exploring the solution space

The way agents explore the solution space in the model depends on their energy because individuals during the initial ideation phase are slower in exploring the solutions as they get warmed up in the beginning by triggering memory search. This is followed by more exploration by recalling past solutions from their memory. However, at some point, this recalling process becomes tiring, and the rate of exploration of the solution space drops toward the end of the session (Goucher-Lambert *et al.*, 2019) (illustrated in Fig. 4). This behavior is modeled mathematically as shown in Eq. (2). Changing the shape parameter of the curve (σ) makes it possible to generate different energy curves, hence different



Fig. 4. An example plot of an agent's energy to explore solution space.

exploration styles could be assigned to agents. The curve is personalized and kept constant for an agent throughout a session. It does not change with respect to other team member nor depends on factors such as motivation to solve a problem.

$$O(z') = \frac{1}{\sigma\sqrt{2\pi}} e^{(-\ln(z')/2\sigma^2)} + c.$$
 (2)

The exploration of the solution space depends on the length of the idea generation session (i.e., the number of the steps), in the given Eq. (2), z' is the normalized length of the session. The value of σ lies between $0 < \sigma \le 1$, it represents the shape parameter that affects the overall shape of the curve. c is the energy value when the session starts where 0.0 < c < 0.5 is randomly assigned to the agents as it was assumed that there is a certain amount of energy in individuals when the session starts (maximum energy was 1 and minimum was 0).

Memory

Taking inspiration from the constructive memory concept (Liew and Gero, 2004), the model constructed here implements a simplified version of memories in agents where memory is created based on design agents' past experience.

Different agents have different memory storage and store experience after working on the design task at the end of a session. These experiences are in the form of feedback from the controller agent. The experiences that are not utilized in the agent's current situation and are not recalled for a long time are forgotten from the memory. The forgetting in agents is based on the Decay Theory, which suggests that "If there was no attempt to recall an event, the greater the time since the event, the more likely it would be to forget the event" (Oberauer and Lewandowsky, 2008). Accordingly, agents in the model exhibit the behavior that suggests that memories are not permanent.

Recall capability

Recalling here refers to the act of bringing a past event back into one's mind. When an agent is unable to recall, it does not mean that the information is permanently removed from its memory but rather that it is unable to be retrieved from its memory for that situation. An individual in real situations might not be able to recall any similar experience from the past while approaching a problem in its current situation. Similarly, in the model, an agent has its feedback from the controller agent stored in its memory. This feedback is in the form of positive (successful experiences) or negative (failed experiences) events, but an agent might not be able to recall them while solving the problem.

An agent could recall the stored events in any order and the recalled events from the past alter the way it approaches the solution (Murdock, 1962). The recalling ability in agents depends on the intensity of the solution value and the time of recall as explained by Banaji (1986) and varies from agent to agent. Identical to the real-world situation where individuals recall their worst and best events results more clearly than their mediocre outcomes, this phenomenon of recency and primacy effect is simulated in the model as given by Murdock (1962). This means that the events that are either first or most recent are recalled more often than the events in-between. Likewise, the events that are extreme (i.e., best and the worst) are more easily recalled. An example of the events being recalled is shown in Figure 5. The red path is the trajectory that each agent takes before selecting the final solution. This red path is made of several steps that are analogous to a designer moving from one solution to another in a design space during an idea generation session. The set of recalled memories (shown as **R** in Fig. 5) could be of a positive (gray cross) or a negative event (orange cross).

Learning from experience

The most common form of simulating learning in agents is in the form of reinforcement learning, where the agents use feedback from the environment to determine their action for the current state (Eliassi-Rad and Shavlik, 2003; Hulse *et al.*, 2019) (seen as



Fig. 5. An example showing an agent recalling events while exploring solutions.



Fig. 6. An agent learning (explained more in the sections "Learning from experience" and "Effect of the influencers").

arrow 2 in Fig. 6). Similarly, in the model, agents learn about the solutions space gradually as they receive feedback from the controller agent present in their environment. The behavior resembles the one described by Cagan and Kotovsky (1997), where the agents move randomly when they start their search but become more regulated as they learn about their problem. According to the feedback (a numerical value) received by an agent at the end of a session, the event is broadly classified as positive (successful) and negative (failure) which are stored in its memory. The event is said to be in a positive category when the feedback value is above a certain threshold and in a negative category when it is below, it could be seen from the example shown in Figure 5 (as black and orange crosses). The learning from the past, which could be positive or negative experience, is different and have a different impact on the current situation (Wimmer and Shohamy, 2012) are described below:

Learning from a positive experience ($\vec{v_s}$) and how it affects an agent on its current solution depends on threefactors (Fig. 7):

• The magnitude of learning from the positive experience $(|v_s| = S (d'))$ depends on the similarity between an agent's current solution in "mind" and the recalled positive event (Read and Grushka-Cockayne, 2010). If the recalled event is similar (closer on solution space) to the solution "in mind", the agent is more influenced by its previous experience than those that are far in distance (not so similar) (Gentner, 1989). On the other hand, if



Fig. 7. Different amount of learning from one's own positive experience.

the recalled positive event is too similar (i.e., too close) as the solution in mind, the agent's learning is less influenced by it. This assumed that an individual will not apply the exact same (or slightly different) knowledge from the past event to their current situation, hence compelling it to produce different solutions. The similarity is represented as the distance between the recalled and current agent position (d).

- The amount of learning from a positive experience also depends on the expertise level of an agent. It means that when an agent has a lower domain-expertise level, it will learn slower therefore a less steep slope than the agent who is more expertise (Ball *et al.*, 2004). It is seen in Figure 7 as the position of the peak of the learning curve. This is represented in Eq. (3.1), as α that depends on an agent's expertise (*E*) level, where *E* was randomly assigned to the agents when the session starts.
- Lastly, learning from a positive experience depends on the time when the recalled event occurred (Δt). It is shown as the height of the learning curve in Figure 7 where more is the height; greater is the learning when the positive experience is recent. Its height is represented in Eqs (3.2) and (3.3) where τ is the adjusted value of Δt so that the value of the curve in Eq. (3) is normalized.

The amount of learning from the positive experience recalled (magnitude of the learning vector as shown in Fig. 8) can be represented by S(d') and is given in the following equation:

$$S(d') = \tau \left(\frac{\frac{1}{d' \alpha^{\sqrt{2\pi}}} e^{(-((\ln (d'))/2\alpha^2))}}{0.7} \right),$$
 (3)

 $d' = 4.0 \cdot d + 0.1$. Here, d' is the adjusted value of d such that $0 \le S$ $(d') \le 1$.

In computational terms, d is the distance between the current agent (solution) position in session n and recalled success (solution) position of session S_n . d is the similarity between the current design task and recalled positive experienced as explained above



Fig. 8. The updated position on an agent after learning from a positive experience.

that similarity is one of the factors on which learning magnitude depends. In Eq. (3), S(d') is divided by 0.7 to normalize it. The other variables in the above equation (on which learning magnitude depends) are explained as follows:

$$\alpha = 0.8 - (0.2 \cdot E), \tag{3.1}$$

$$\tau = 1 - (0.7 \cdot \Delta t), \tag{3.2}$$

$$\Delta t = n - \frac{S_n}{N'},\tag{3.3}$$

where *n* is the current session number of an agent and S_n is the session when the recalled success occurred. N is the number of sessions in the equation 3.3.

The learning from positive experience vector, $\vec{v_s}$, is summed to the initial knowledge state vector of an agent $\vec{v_k}$ to get the resultant learning vector $(\vec{v_n})$ from the two learning states (arrows 1) and 2 shown in Fig. 6) for an idea generation session given as Eq. (4).

$$\vec{v}_n = \sum_{i=1}^N \vec{v}_{s_i} + \vec{v}_k,$$
(4)

where in the equation 4, N is the number of positive experiences recalled in a session n and i is the initial starting index.

Learning for a negative experience is different from a positive experience as humans try to avoid the failures they have committed in the past and tend to follow the path that led to previous success (Wimmer and Shohamy, 2012). Similarly, learning from negative experiences is done in the form of avoiding the areas where previous failures have occurred. An agent avoids the negative experiences by forming a circle around the point where the recalled failure had occurred. Like the real scenario where an individual remembers the failure zones on the solution space while exploring new solutions. The radius of this circle differs from agent to agent and depends on the severity of the recalled negative event (Fig. 9). The maximum failure radius is chosen to be five units for a 100×100 . The radius or the size of the circle denotes the learning capacity from a failure of an agent, and it will avoid the circle area around the recalled failure (Fig. 10).

5 1

Fig. 9. Failure radius depends on the value of the recalled failure (where five units are the max radius for a 100 × 100 units of solution space).

Effect of the influencers

To investigate the factors that could give rise to the influencer effect in design teams, self-efficacy and trust (resulting from the mutual knowledge of each other) were chosen as initial parameters to begin the investigation. Self-efficacy is implemented in the model as a dynamic feature in agents that changes based on its intrinsic and extrinsic motivation (Rvan and Deci, 2000). Like self-efficacy, trust also changes throughout the simulation as in real situations where it depends on the interacting individual's familiarity and reputation (Mui et al., 2002; Costa, 2003). To model the "influencing effect", each agent has an influencing value from other agents in the team and it depends on the factors shown in Figure 11. The influence value I (same magnitude of the social learning vector $|\vec{v}_i|$), for an agent *i* of agent *j* is computed as Eq. (5) (an example in Fig. 12). Here, j varies until the total number of agents present in a team and $j \neq i$.

$$I_i^{j}(\Delta SE, SE, T) = w_1(\Delta SE_{i-j})^{1.5} + w_2(SE^{j}) + w_3(T_i^{j}), \quad (5)$$

 Δ SE in the equation 5 is the difference in self-efficacy of agent *i* and agent j, T is the degree of trust of agent i has on agent j. SE is the self-efficacy of an agent *j*. The weights w_1 , w_2 , and w_3 were decided in after the empirical studies, presented in the next section.

$$T(R, f)_i^j = w_4(R^j) + w_5(f_i^j).$$
(5.1)

The amount of trust an agent i has an agent j depends on Rand f (Costa, 2003). R is the reputation of an agent j and f is the familiarity (i.e., how well does an agent i knows agent j). Familiarity, f between two agents, is calculated as the number of sessions agent *i* and *j* have worked together, therefore familiar with each other. Reputation, on the other hand, is given as Eq. (5.2), where N_a is the number of solutions that are accepted by the controller agent and $N_{\rm p}$ is the total number of the solutions proposed by an agent. Familiarity and reputation, in reality, may not be fully independent but here they are modeled as mutually independent parameters (Hinds et al., 2000). In the model, familiarity between the two agent increases with the number of idea generation sessions they have in common, as the agents at this point are not being shuffled (replaced, removed, or added), the familiarity is the same for all of them. Thus, familiarity being constant, reputation is the only factor that is affecting trust.

The weights in Eqs (5) and (5.1), w_1 , w_2 , w_3 , w_4 , and w_5 were decided after the empirical studies presented in the next section.

$$R = \frac{N_a}{N_p},\tag{5.2}$$

$$\vec{v}_{n'} = \sum_{i=1}^{N} \vec{v}_{I_i} + \vec{v}_n,$$
(6)

where \vec{v}_{I_i} is the total amount of learning by an agent *i* from its peers (arrow 3 as shown in Fig. 6) given in Eq. (6.1) and $\vec{v_n}$ is as calculated in Eq. (4). The resultant vector $\vec{v}_{n'}$ is the total amount of learning an agent does while generating solutions to the design problem.

$$\vec{v}_{I_i} = \sum_{\substack{j=1\\j\neq i}}^N I_i^j, \tag{6.1}$$

339





Fig. 12. The updated position on an agent is the sum of the vectors of its resultant learning vector from recalled success and the influence value vector.

Empirical studies

The development of the model presented in the previous section was guided by phenomena demonstrated in the psychology, sociology, and design literature. This section presents empirical studies that were conducted to improve the model in several ways:

Fig. 10. An example where an agent (in red) encounters a failure at session n-k, which is being recalled in session n, an area around the failure is avoided.



0

0

20

40

60

80

Fig. 11. Determining influence value.

In the equation 6.1, N is the number of agents in a session n with the agent i and j is the initial starting index for its peers.

Studies show that an individual proposes more ideas when the team accepts their ideas and high self-efficacy individuals get lesser change in their self-efficacies (increase and decrease) than the ones with lower self-efficacies (Pearson $\rho = -0.717$, *p*-value < 0.001) (Singh *et al.*, 2020). Similarly, an agent's change in its self-efficacy is simulated in the model. Figure 11 also shows that self-efficacy depends on an individual's motivation, which is impacted by an appreciation by team members or rewards (in terms of positive feedback) given by the superiors. Computationally, appreciation based motivation happens for an agent when other agents select its solution and reward-based when the controller agent provides good feedback (Ryan and Deci, 2000). Both of these forms of motivation contribute to the individual's change in self-efficacy. Despite the fact that these two phenomena have different mechanisms, they are modeled similarly.

- Validate the assumption: The work assumes that self-efficacy and trust could be the individual characteristics responsible for the influencer effect. Due to insufficient work done in the past to reveal the qualities of an influencer(s) in design teams, the experiments were conducted to get some initial insights.
- Determining the weights of the model equations: The additional insights were gained regarding the relationship among the model parameters that were used to estimate weights $(w_1, w_2, w_3, w_4, \text{ and } w_5)$ for Eqs (5) and (5.1) (given in the above section).
- Verify the model logic: The model logic such as the lower selfefficacy agents perceiving a greater number of influencers than higher self-efficacy was verified by the empirical study.

These two experiments presented here were observational in nature. Data collection from these experiments was done mainly through survey questionnaires. It was not mandatory for the participants to take part in the surveys.

Observation Experiment 1

Data collection

The experiment was set up to monitor design teams working on semester-long design task given by a company for a master's degree course of Methods and Tools for Systematic Innovation. There were 10 teams with 4–5 mechanical engineering graduate students in each of them.

The data werecollected twice in the form of online surveys (the link to the sample questionnaires is provided in Appendix B). Initial data collection was conducted when the course started and was related to collecting information about their self-efficacy (Carberry et al., 2010) and problem-solving attitudes. The questions for determining self-efficacy were taken from Carberry et al. (2010), but the scale was changed from 10 to 4-point to match the scale of problem-solving questions. The questions related to the problem-solving attitude aimed to capture an individual's approach when handling a design problem. The same set of questions were used by Becattini and Cascini (2016) to assess characteristics of creative instruments for problem-solving in students. The questionnaire and the scales employed here have already been validated and used by other researchers in the past (Carberry et al., 2010; Becattini and Cascini, 2016). The second data collection was conducted after the students had started working in their respective teams on the given task. In order to map the difference in their problem-solving attitudes and self-efficacy, the questions used in the initial data collection survey were repeated besides some additional questions related to trust, familiarity and influencers on a 5-point Likert scales (5 being maximum) where Ohland et al. (2012) was used as a reference.

Results obtained

It was found that the difference in an individual's self-efficacy with respect to their peers could be responsible for perceived degree of influence from its peers . In other words, a positive correlation was found between the difference in the self-efficacy of an individual and its team member at the beginning of the experiment and the perceived influence value entered by the individual after they started working in teams (Pearson $\rho = 0.41$, *p*-value = 0.014).This means that individuals with low self-efficacy have more tendency to be influenced by others with higher self-efficacies. The impact of the difference in individuals' self-efficacy is not new as studies have shown that it affects team's social



Fig. 13. Linear regression between delta self-efficacy and influence. Regression coefficient: 0.41. Mean squared error: 0.04. Variance score: 0.30.

attributes like group identification and conflicts (Desivilya and Eizen, 2005). Secondly, it was validated that trust plays an important role in determining influencers. It was found that trust between an individual and other individual team member after they started working in teams was positively correlated with its perceived degree of influence (Kendall $\tau = 0.6$, *p*-value < 0.001). Thus, it conforms to the studies that have stated that trust affects individual relationships and team processes (Costa, 2003). The linear regressions between the perceived degree of influence and the difference in self-efficacies and trust could be seen in Figures 13 and 14 where the data set was shuffled and divided into training (67%) and test set (33%). Hence, the results of observation experiment 1 helped in supporting the assumption. As the data was collected using 4- and 5-point Likert scale, plots in Figures 13 and 14 show normalized values and show many overlapping data points.

Observation Experiment 2

Data collection

The second experiment was conducted to collect information related to decision-making during idea selection, but a minor portion of the experiment aimed at finding out the number of perceived influencers in a team. The experiment was set up during the EU's Erasmus+ project called ELPID,¹ where five teams of eight students from four different universities worked on a design task for a period of 3 days. The workshop was a sprint to introduce students to ideation techniques.

Though the teams were under observation throughout the workshop, the data collection was only performed on the second day of the workshop. The collection was done in the form of a short survey where the question related to their self-efficacy (similar to the one given in Appendix B) was measured on a 5-point Likert scale (5 being very self-confident in doing the engineering design activity). The question related to identifying the perceived number of influencers in a team was open-ended. The other questions that are out of the scope of this paper were mainly related to decision making during idea selection.

¹ELPID: E-learning Platform for Innovative Product Development. Available at: http:// www.elpid.org/.

The model, which has now been verified through two empirical studies, is now used to conduct several computational experiments. Specifically, to test the effect of influencers on design thinking during idea generation, a few parameters were varied while keeping the others constant. In this case, the self-efficacy of each agent was allotted at the beginning of the simulation to control the number of influencers in the team. Trust, which is the other parameter to determine influencer(s), depends on the reputation of an agentsand was dynamic as itchanged with each session. Familiarity, at the beginning of the simulation was same for all the agents and was increased with every sessions that agents had in common. Other parameters, which could be relevant, such as team size, design task, the number of idea generation sessions, and the length of the session, were kept constant. All the agents begin without any previous experience of working on the same task. The detailed table of the status of the model parameters could be found in Appendix A. To check the functionality of the model, two scenarios were framed and tested. The first scenario tested the situation when the team has a high variationin the selfefficacy of its agents. Three subscenarios here were:

- 1. One agent with high self-efficacy and others with low (1 influencer)
- 2. Two agents with high self-efficacy and others with low (2 influencers)
- 3. Three agents with high self-efficacy and others with low (3 influencers)

The second scenario tested the situation when the team has low variationin the self-efficacy of its agents (i.e., all agents either have high or low self-efficacy initially). Two sub-scenarios here were:

- 1. All with low self-efficacy (i.e., no influencer)
- 2. All with high self-efficacy (i.e., all influencers)

This was done to understand the effect of influencers on design output due to the presence of an unequal distribution of influence in design teams. To see the functionality of the model, some of the findings are related to (1) difference in



	Observation Experiment 1	Observation Experiment 2
Validating the assumption	Difference in an individual's self-efficacy with respect to its teammates is responsible for its perceived degree of influence. $I \propto \Delta SE$ (l is the perceived degree of influence and ΔSE is the difference between the self-efficacies), hence further supporting the validation of the assumption.	High self-efficacy individuals also had an influence on other high self-efficacy individuals hence, it conforms to Singh <i>et al.</i> (2020). It further supports the assumption that self-efficacy could be one of the factors affecting the $l \propto$ SE.
	The amount of trust between two individuals is also responsible for the influence they perceive from each other. $I \propto T$ (I is the perceived degree of influence and T is the Trust), validating the assumption.	
Determining the weights of the model equations	The correlation between the parameters showed that the relationship between trust and influence is stronger than self-efficacy and difference in self-efficacies. Therefore, from Eq. (5), $w_1 = 0.3$, $w_2 = 0.3$, and $w_3 = 0.4$. The relationship between trust and familiarity was weaker than originally thought, hence in Eq. (5.1), $w_4 = 0.7$ and $w_5 = 0.3$.	
Verify the model logic		Individuals with high self-efficacy perceive fewer influencers than those with lower.



Fig. 14. Linear regression between trust and influence. Regression coefficients: 0.61. Mean squared error: 0.01. Variance score: 0.62.

Results obtained

A slightly negative correlation (Kendall $\tau = -0.3$, *p*-value = 0.03) was found between the individuals' self-efficacy and the number of perceive influencers in their team. The low correlation could be because individuals with high self-efficacy are more likely to perceive others with high self-efficacy as influencers. This could be supported by the other findings such as the relationship between individuals' self-efficacy and the degree of influence by them. A positive correlation (Kendall $\tau = 0.32$, *p*-value = 0.013) was found between the individuals' self-efficacies and their degree of influence as perceived by others. This means that those who had high self-efficacy were also perceived to have more influence value. Similar results were obtained by Singh et al. (2020), where individuals who had high self-efficacy, also perceived high influence from the influencers (Pearson $\rho = 0.55$, *p*-value < 0.001). Hence, further supporting that perceived influence could depend on selfefficacy and the difference in self-efficacy of two individuals.

Implementation of the empirical results

A summary of outcomes from the two observation experiments presented in this paper is given in Table 1.

learning are presented while the other findings answer the research question are related to (2) quality of the solutions (Shah *et al.*, 2003) and (3) exploration of design space (Dorst and Cross, 2001). As defined earlier in the "Model Description" section that the quality of the solution is the value of a point on a design solution space. The exploration of the agents is quantified in three different ways as given below. These three different measures were chosen as it would be useful to see how much the agents explore the design space while considering the quality and diversity of these explored solutions.

Exploration index (EI) is the number of points (solutions) explored when generating solutions on a lower resolution solution space (soln_{lowr}) to the area of this lower resolution space (Area_{lowr}) [Eq. (7)]. The lower resolution of solution space means that the original solution space (100×100 units) is decreased in size by a factor (5 in this case) so that the resultant is a smaller space (20×20 units). This means that if an agent explores solutions within five units of neighboring cells, it is counted as one unit of exploration. This simplification was done to avoid potential logical inconsistencies which could arise when an agent explores immediate neighbor cells to an agent exploring five cells at a larger unit distance.

$$EI = \frac{\text{soln}_{\text{lowr}}}{\text{Area}_{\text{lowr}}}.$$
(7)

Exploration quality index (EQI) is the ratio of the number of solutions explored on a lower resolution solution space (solns_r) with solution quality above a certain threshold, t (in this case, t is above 0.5, where 0 is a minimum and 1 is a maximum solution quality value) to the total number of solutions (totSoln_r) available on the design solution space greater than the threshold value [Eq. (8)]. This means that if an agent explores solutions within five

units of neighbouring cells, the EQI will be the mean of the solution values of these 5 cells. Similar to EI, this simplification helped in evaluating the quality of the explored solutions while avoiding the inconsistencies which could arise when an agent explores immediate neighbour cells to an agent exploring five cells at a larger unit distance.

$$EQI = \frac{\text{solns } r}{\text{totSoln}_r}.$$
(8)

Spread is the dispersion of the solutions from the centroid of the solutions. The spread of the solutions obtained was calculated to see how different the solutions were from each other (i.e., variety of the solutions).

The agent idea generation results are related to the exploration and quality of the solution. The results are from five peak design space (i.e., five best solutions) to get an insight into how different compositions of influencer(s) affect idea generation in this design task setting. The results are calculated based on the Monte Carlo logic to reduce the effect of randomness; hence, the results below are based on 200 simulations.

The results related to different learning styles:

Figure 15b shows how low and high self-efficacy agents behave during idea generation based on Figure 15a shows the flowchart of the extraction of the required data from the simulation. The figure shows the distance between the solutions of a low and high selfefficacy agent with respect to an influencer (here the maximum sessions were 20). It could be inferred that a high self-efficacy agent (but lesser than the self-efficacy of an influencer) explores solutions differently than an Influencer, while a low self-efficacy agent (is the one with the lowest self-efficacy in the team) generates solutions closer to that of an influencer. This aligns with expectations on the nature of influence in design teams and



Fig. 15. (a) A flowchart showing the steps taken to plot 15b. (b) An example showing the distance between the low and high self-efficacy agents from the influencer (for maximum sessions = 20).

corresponds to Brown and Pehrson (2019), where it was stated that some individuals are more influenced by the influencer(s) than others.

The learning modeled in this work could be associated with Associative Learning that states that ideas and experiences reinforce each other and can be mentally linked to one another (Paivio, 1969). This type of learning is a form of conditional learning that is based on the theory, which states that an individual's behavior could be modified or learned based on a stimulus and a response (Paivio, 1969). For example, if an agent's solution was bad (i.e., it got poor feedback from the controller agent) (stimulus), it will not produce similar solutions (response) (i.e., avoiding that area on the solution space). Based on the relationship between the two stimuli (current and recalled events), associative memory can be called (Paivio, 1969). The agent uses both the positive and negative reinforcers (stimuli used to change behavior), to modify the way they generate their current solution. Figures 16 and 17 show agents with the lowest self-efficacy in teams with a varying number of influencers learn from their successes and failures for a design task with five best solutions. Learning from success and failure has been explained in the Model description, where agents avoid the failures they have committed in the past and tend to follow the path that led to previous success. The curves obtained in the results shown in Figure 16 are similar to the learning curves described in Leibowitz et al. (2010). There is not much difference in the success learning curves (Fig. 16), with the lowestself-efficacy agents in teams of all influencers learning slightly more from their success than other team combinations. The failure learning results shown in Figure 17 are more divergent and agents in the teams when all agents start at high self-efficacy (all influencers) have the least ability to learn from failure than the other combinations tested. Concerning learning from failure, all the lowest self-efficacy agents in the team with no influencer, 1 influencer, and 3 influencers, learn more from their failures toward the end of a project. In general, it could be seen from Figure 17 that the learning from failure becomes steady toward the end of a project. The slope of the failure learning curves (failure rate) exhibit somewhat similar behavior to the "early failure" phase (widely used in reliability engineering) (Wilkins, 2002), where the rate of failure decreases with time, hence the system improves (Proschan, 2012).

Social influence, which leads to the imitation in individuals to modify opinions, attitudes, and behavior similar to the others they



Fig. 17. Learning from failure.

are interacting with, is referred to as social learning. As it could be seen from Figure 18, the influence of individuals is unevenly distributed in a team, consequently, is social learning. The amount of social learning in the teams where the ratio of influencers to non-influencers (i.e., low self-efficacy agents) was half and agents in teams with all influencers, social learning could be seen high throughout the project, while minimum when all agents have low self-efficacy when they start working (Fig. 18). Social learning curves are similar to the ones obtained in other domains of study such as online gaming (Landfried *et al.*, 2019) or during diffusion of innovation (O'Brien and Bentley, 2011).

The results related to the quality of the solutions:

The results related to design quality for a 5-peak configuration of a design task with respect to different influencer/noninfluencer team compositions could be seen in Figure 19 (ANOVA F = 34.02, p < 0.001). The pairwise (*post hoc T*-test) comparisons of the generated solution quality were also statistically significant for all the cases except two (i.e., teams with 1 and 2 influencers, and teams with 1 and 3 influencers solution quality). Agents in the all influencer team, on average had better solution quality than other team compositions. In general, the quality of solutions increases with the idea generation sessions with minor divergence. This shows that all agents in the model are learning (from different modes as shown in Fig. 6). One possible reason for this could be because the individuals in teams



Fig. 16. Learning from success.

Fig. 18. Social learning.



Fig. 19. Mean solution quality for all the agents in a team.

compare their performance with the others in the teams, hence converge in their solution quality (Larey and Paulus, 1999). They are storing the events in their memory and recalling the ones associated with their current situation (explained in the "Model description" section). Recalling these events and associating them to the current situation enhanced idea generation (Dugosh and Paulus, 2005). The quality results of the model are consistent with the study done by Brown et al. (1998) and Paulus (2000), where it was shown that exposure to others' ideas may increase the quality of ideas generated. By narrowing down, one could observe that agents in the teams of no influencer produced better quality ideas after the second half of the project while the opposite could be seen in teams of all influencers. Figure 20 shows the quality of solutions of the lowest self-efficacy agent in different team compositions (Kruskal–Wallis H = 4.75, p = 0.31). It shows that agents with the lowest self-efficacy in teams behave similarly when generating solutions, irrespective of the influencer team composition.

The results related to exploration values:

In general, it can be seen from Figure 21(top) that the teams with well-defined influencers and all influencers have a lesser exploration index (EI) than no influencer teams. The exploration of solutions on the design space by all the teams differs



Fig. 20. Mean solution quality for the lowest self-efficacy agent in a team.

significantly (Kruskal–Wallis H = 18.70, p < 0.001). The pairwise comparison (post hoc Conover's test) further confirmed that agents in all and well-defined influencer teams behave significantly different from no influencer team composition. This could mean that due to a lesser number of influential agents, agents in the team keep exploring new areas on the design solution space. The quality of solutions explored (EQI) by the individual agents during idea generation could also be seen in Figure 21 (middle). Even though it seems that few influencer teams (like 1 and 2 influencers) had better EQI, the compositions did not differ significantly in their EQI values (ANOVA F = 1.53, p = 0.19). Teams with or without well-defined influencers had similar EQI. A weak positive correlation was found between EI and EQI (Kendall $\tau = 0.2$, *p*-value < 0.001), which suggests that as the agents explore more, they have a better chance of generating an above-average solution. This model behavior does not explicitly contradict the studies that state that exploring a greater percentage of design space does not explicitly guarantee to find better alternatives (Ehrich and Haymaker, 2012; McComb et al., 2015). As well as it does not explicitly, conforms to the studies that state that larger exploration has more possibility to have high quality solutions (Danes et al., 2020). One main reason could be the configuration of the design space with five peaks. As the number of best solution peaks were more, hence a greater probability of finding higher quality solutions on exploring.

The diversity in the generated solutions as seen from Figure 21 (bottom) in all the cases differs significantly (Kruskal–Wallis H =84.78, p < 0.001). After conducting a pairwise comparison (*post* hoc Conover's test), it was found that agents in the teams with few well-defined influencers (1 and 2 influencers) behave similarly when generating solution (i.e., follow the influencer). Agents with all low self-efficacy (no influencer) also behaved similar to the 1 and 2 influencer team agents. While agents in teams with half influencers and all agents with high self-efficacy generate more diversity in the solutions as seen from Figure 15b that high self-efficacy agents are not afraid to explore on their own. Social influence is a dynamic in nature, as the influencers influence others in the team, they become is influential and the former start becoming more influential (Brown and Pehrson, 2019), this phenomenon is more prominent in the teams of no influencer as they had least variety. It could be inferred that fewer influencers influence others in the team to imitate them in their solution. One influencer means exploring the solutions close to that influencer, this increases when the influencers become 2 and so on. As all agents have low self-efficacy, so when an influencer emerges among them, they blindly explore areas near the influencer, thus low spread. Paulus and Dzindolet (2008) stated that due to social comparison, individuals tend to move toward the direction of the social comparison referent (influencer(s)) and mimic the performance of their co-workers. As there are fewer influencers (either intentionally assigned or emerge) in 1 influencer and no influencer teams, the other noninfluencers follow one agent, hence lesser spread than the other team compositions. The other explanation could be that the EI value that gives an idea about the exploration while spread shows the dispersion of the solutions from the centroid of the solutions. This could mean that the agents in the no influencer teams explored more the design space while the explored solutions were at a somewhat equal distance from the centroid, hence low dispersion value. In the case of all influencers, agents have high self-efficacy hence more capability to explore other than the solutions of an "emerged influencer(s)". A general trend in the exploration (EI)



Fig. 21. Exploration values (EI, EQI, and spread).

and diversity in the generated solution could be seen where higher exploration was correlated to higher diversity in the generated solutions (Kendall $\tau = 0.4$, *p*-value < 0.001).

The behavior of teams without well-defined influencers (i.e., no and all influencers) differed from each other, as in no influencer team behavior tended toward teams with a few defined influencers (like 1 or 2 influencers). The influencer(s) might have emerged in the no influence team as the team moved from one session to another. Since there were fewer influencers (either intentionally assigned or emerge) in 1, 2, and no influencer team, the other non-influencers follow them, hence lesser spread than the other team compositions with more influencers (like 3) or all with high self-efficacy (all influencer). In the case of all influencers, agents have high self-efficacy hence more capability to explore than no influencer team where an influencer might have emerged, and agents had low self-efficacy.

The exploration rate, which is the number of solutions in a design space explored during a session, without considering the ones in the previous session could be seen in Figure 22. In general, the exploration rate during sessions three to five is lower than in other sessions in teams of no to a few prominent influencers. This could suggest that the effect of the influencers on exploration is maximum somewhat in the early middle of the project, as it is known from Agars *et al.* (2008) where group-creativity is a "function of the extent to which social influences affect individuals within the group at earlier stages". On the contrary teams with all influencers, which have the least exploration rate initially, dramatically increase their exploration rate than other teams after four to five sessions.

Summary

Like any other collaborative design session, the simulation starts with a design task given to a team of agents who must produce solutions. Agents generated solutions based on the learning



Fig. 22. Session-wise exploration rate.

rules assigned to them. The effect of the influencers on idea generation was simulated and the results were discussed as the answers to the research question. However, before investigating the research question, it was crucial to gain insights into the characteristics that give rise to an influencer in a design team, therefore an assumption was made that *self-efficacy and trust are characteristics that determine how individuals perceive the degree of influence by others in the team.*

The assumption was validated by the results from the empirical studies where it was found that self-efficacy and trust could be some of the characteristics resulting in the perceived degree of influence in design teams. It was found that if an individual had lesser self-efficacy than the other, the difference in their selfefficacies was responsible for the perceived degree of influence by the individual with less self-efficacy. Trust between the two individuals was highly positively correlated to the perceived degree of influence. This means that if an individual trusts the other, they also perceive the other individual as influential. Lastly, individuals with high self-efficacy might perceive fewer influencers than those with lower.

The insights for the empirical studies were used to tune the model, and subsequently, a series of simulations were used to explore the relationship between influence distribution and design outcomes. The simulation results show that both low and high self-efficacy agents were affected by influencers. A low selfefficacy agent explored solutions closer to that of an influencer than a high self-efficacy agent. Agents also learnt from past positive or negative events throughout the project. As learning from positive experience increased, learning from the negative events became stable. The quality of the solutions increased with the number of idea generation sessions as the agents learnt from their past events and others in the team. The generated solution quality values of teams with well-defined influencers differed significantly from the teams without well-defined influencers. This shows that the agents in the teams are affected by the presence of influencers in teams when generating solutions. Teams with one prominent influencer have a similar effect on their team agents' solution quality as of teams with multiple influencers (in this case 2 or 3 influencers). Despite the second half of the project where agents in no influencer teams produced better quality ideas, all influencers on average had better quality than all the team compositions.

Agents in teams with well-defined influencers and all with similar high self-efficacy (all influencers) had lesser exploration (EI) than teams where all agents had low similar self-efficacy (no influencer). The quality of the explored solutions (EQI) by individual agents during idea generation was not affected by the presence of influencers. However, the dispersion of the solutions (spread) or variety in the generated solution was lesser for the teams with no or few defined influencers than teams with more influence (3 and all influencers). The exploration rate was lower during the first few sessions in the teams of no influencers and a few prominent influencer teams. Agents in teams with one prominent influencer had less exploration rate toward the end of a project. Overall, all high self-efficacy agents (all influencers) start exploring more and more somewhat after the middle of the project. The impact of the influencers on session-wise exploration was found to be stronger somewhat in the early middle of the project.

Conclusion

Many factors could affect the outcomes of collaborative design activity. Here, a computational model was constructed to facilitate the study of these factors. Specifically, this model was capable of exploring the effect of social influence in the team. Social influence (which give rise to imitation behavior called social learning) is known to affect brainstorming and hence design outcomes like quality and exploration values but has not been studied in detail. The initial model was constructed from the existing literature. The results are thought-provoking and could be used to deduce patterns in individual and team behavior due to the unequal distribution of influence in design teams. They help in recognizing individuals' and team outcomes, which would assist in taking appropriate action and thus more control over managing design activity for better results. The results clearly demonstrate that the presence of a few prominent influencers affects design outcome by limiting variety (spread) and enhancing quality (especially when all the agents have low self-efficacy), thus

addressing the research question that is, what is the effect of influencer(s) on idea generation outcomes (exploration and quality)? The social influence or in other words individuals with high social influence called influencers positively or negatively influence brainstorming of others in the team, depends on the cognitive state of the brainstormer (Brown et al., 1998) (i.e., the self-efficacy levels of the team members) as well as on the desired nature of design output (i.e., whether the higher variety is required or quality). However, the results mentioned above should be considered as insights instead of actual understandings, as they would vary with the complexity of the task modeled, the number of agents and learning rules. Although authors have also analyzed results related to 1, 3, and 12 peaks design space configuration, to enhance clarity and space limitation, the results presented here are confined to 5 peaks. Although the strength of this research is the simplification of the experimental scenarios, it is important to be explicit on how far one can take the results presented in the model. Although the results are applicable in their respective settings, they still need validation from the real experiments. They are not indicating the exact behavior of influences, but rather they could be interpreted as indications of how influencers are affecting design teams. Undoubtedly, more work needs to be done to see how influencers in the design team affect team and organization creativity. This includes (1) the assumed relationship between trust, self-efficacy, and influence, (2) the mutual relationship between trust and familiarity, (3) the design space representation, (4) a richer representation of communication and collaboration, (5) a more nuanced model for the effect of influence based on agent traits, and (6) the representation of the other forms of social learning.

The adherence of many of the results from the simulation to patterns shown in the literature provides partial validation of the model. However, further validation using additional empirical experiments should be a major focus of future work. The wider purpose of the work is to provide a computational approach that focuses on representing the collaborative process, underlying its results on project outcomes. The key advantage of this computational approach lies in providing suggestions on patterns (related to design outcome) of design team activity. This model may provide useful insights for building suitable strategies for team building and team performance.

References

- Abar S, Theodoropoulos GK, Lemarinier P and O'Hare GM (2017) Agent based modelling and simulation tools: a review of the state-of-art software. *Computer Science Review* 24, 13–33.
- Agars MD, Kaufman JC and Locke TR (2008) Social influence and creativity in organizations: A multi-level lens for theory, research, and practice. In Mumford MD, Hunter ST and Bedell-Avers KE (eds), Multi-Level Issues in Creativity and Innovation (Research in Multi-Level Issues, Vol. 7). Bingley: Emerald Group Publishing Limited, pp. 3–61. https://doi.org/ 10.1016/S1475-9144(07)00001-X.
- Aries EJ, Gold C and Weigel RH (1983) Dispositional and situational influences on dominance behavior in small groups. *Journal of Personality and Social Psychology* 44, 779–786.
- Baker SJ (2015) Exploration of equality and processes of non-hierarchical groups. Journal of Organisational Transformation & Social Change 12, 138–158. doi:10.1179/1477963315Z.00000000039.
- Ball LJ, Lambell NJ, Reed SE and Reid FJM (2001) The exploration of solution options in design: a 'naturalistic decision making' perspective. In Lloyd P and Christiaans H (eds), *Designing in Context*. Delft, The Netherlands: Delft University Press, pp. 79–93.

- Ball LJ, Ormerod TC and Morley NJ (2004) Spontaneous analogising in engineering design: a comparative analysis of experts and novices. *Design Studies* 25, 495–508.
- Banaji RM (1986) Affect and Memory: An Experimental Investigation. Columbus, OH: The Ohio State University.
- Bandura A (1977a) Social Learning Theory. Englewood Cliffs, NJ: Prentice-Hall.
- Bandura A (1977b) Self-efficacy: Toward a unifying theory of behavioural change. Psychological Review 84, 191–215.
- Bandura A (1986) Social Foundations of Thought and Action: A Social Cognitive Theory. Englewood Cliffs, NJ: Prentice-Hall Inc.
- Becattini N and Cascini G (2016) Improving self-efficacy in solving inventive problems with TRIZ. In Corazza G and Agnoli S (eds), Multidisciplinary Contributions to the Science of Creative Thinking. Creativity in the Twenty First Century. Singapore: Springer, pp. 195–213.
- Becattini N, Cascini G, O'Hare JA and Morosi F (2019) Extracting and analysing design process data from log files of ICT supported co-creative sessions. Proc. Int. Conf. Engineering Design ICED'19. Delft, The Netherlands: The Design Society, Cambridge University Press.
- Bonabeau E (2002) Agent-based modeling: methods and techniques for simulating human systems. *Proceedings of the National Academy of Sciences* (PNAS) 99, 7280–7287.
- Brown V and Paulus PB (1996) A simple dynamic model of social factors in group brainstorming. *Small Group Research* 27, 91–114.
- Brown R and Pehrson S (2019) Innovation and changes in groups: minority influence. In Brown R and Pehrson S (eds), Group Processes: Dynamics Within and Between Groups. New Jersey: Wiley-Blackwell, pp. 85–100.
- Brown V, Tumeo M, Larey TS and Paulus PB (1998) Modeling cognitive interactions during group brainstorming. Small Group Research 29, 495– 526.
- Cagan J and Kotovsky K (1997) Simulated annealing and the generation of the objective function: a model of learning during problem solving. *Computational Intelligence* 13, 534–581.
- Carberry AR, Lee H-S and Ohland MW (2010) Measuring engineering design self-efficacy. Journal of Engineering Education 99, 71–79.
- Carley KM (1996) A comparison of artificial and human organizations. Journal of Economic Behavior & Organization 31, 175–191.
- Carley KM and Gasser L (1999) Computational organization theory. In Weiss G (ed.), Multiagent Systems: A Modern Approach to Distributed Artificial Intelligence. Cambridge, MA: MIT Press, pp. 299–330.
- Costa AC (2003) Work team trust and effectiveness. *Personnel Review* 32, 605–622. doi:10.1108/00483480310488360.
- Cvetković D and Parmee I (2002) Agent-based support within an interactive evolutionary design system. Artificial Intelligence for Engineering Design, Analysis and Manufacturing 16, 331–342.
- Danes JE, Lindsey-Mullikin J and Lertwachara K (2020) The sequential order and quality of ideas in electronic brainstorming. *International Journal of Information Management* 53, 1–5.
- Dionne SD, Sayama H, Hao C and Bush BJ (2010) The role of leadership in shared mental model convergence and team performance improvement: an agent-based computational model. *The Leadership Quarterly* **21**, 1035–1049.
- Dorst K and Cross N (2001) Creativity in the design process: co-evolution of problem-solution. Design Studies 22, 425–437.
- Dugosh KL and Paulus PB (2005) Cognitive and social comparison processes in brainstorming. *Journal of Experimental Social Psychology* 41, 313–320.
- Ehrich AB and Haymaker JR (2012) Multiattribute interaction design: an integrated conceptual design process for modeling interactions and maximizing value. *Artificial Intelligence for Engineering Design, Analysis and Manufacturing* **26**, 85–101.
- Eliassi-Rad T and Shavlik J (2003) A system for building intelligent agents that learn to retrieve and extract information. User Modeling and User-Adapted Interaction 13, 35–88.
- Gentner D (1989) The mechanisms of analogical learning. In Vosniadou S and Ortony A (eds), *Similarity and Analogical Reasoning*. Cambridge, England: Cambridge University Press, pp. 199–241.
- Gero JS and Kannengiesser U (2004) Modelling expertise of temporary design teams. *Journal of Design Research* 4, 1–13.

- Goucher-Lambert K, Moss J and Cagan J (2019) A neuroimaging investigation of design ideation with and without inspirational stimuli understanding the meaning of near and far stimuli. *Design Studies* **60**, 1–38.
- Granovetter MS (1973) The strength of weak ties. American Journal of Sociology 78, 1360–1380.
- Green G (1997) Modelling concept design evaluation. Artificial Intelligence for Engineering Design, Analysis and Manufacturing 11, 211–217.
- Hinds PJ, Carley KM, Krackhardt D and Wholey D (2000) Choosing work group members: balancing similarity, competence, and familiarity. *Organizational Behavior and Human Decision Processes* **81**, 226–251.
- Hulse D, Tumer K, Hoyle C and Tumer I (2019) Modeling multidisciplinary design with multiagent learning. Artificial Intelligence for Engineering Design, Analysis and Manufacturing 33, 85–99.
- Kleinsmann M and Valkenburg R (2008) Barriers and enablers for creating shared understanding in co-design projects. *Design Studies* 29, 369–386.
- Landfried GA, Fernández DS and Mocskos E (2019) Faithfulness-boost effect: loyal teammate selection correlates with skill acquisition improvement in online games. *PLoS ONE* 14, e0211014.
- Lapp S, Jablokow K and McComb C (2019) KABOOM: an agent-based model for simulating cognitive styles in team problem solving. *Design Science* 5, 1–32.
- Larey TS and Paulus PB (1999) Group preference and convergent tendencies in small groups: a content analysis of group brainstorming performance. *Creativity Research Journal* **12**, 175–184.
- Lee KH and Lee K-Y (2002) Agent-based collaborative design system and conflict resolution based on a case-based reasoning approach. *Artificial Intelligence for Engineering Design, Analysis and Manufacturing* 16, 93–102.
- Leibowitz N, Baum B, Enden G and Karniel A (2010) The exponential learning equation as a function of successful trials results in sigmoid performance. *Journal of Mathematical Psychology* **54**, 338–340.
- Liew P-S and Gero JS (2004) Constructive memory for situated design agents. Artificial Intelligence for Engineering Design, Analysis and Manufacturing 18, 163–198.
- Maher ML, Rosenman M and Merrick K (2007) Agents for multidisciplinary design in virtual worlds. Artificial Intelligence for Engineering Design, Analysis and Manufacturing 21, 267–277.
- McComb C (2016) Designing the Characteristics of Design Teams via Cognitively Inspired Computational Modeling. Pittsburgh, PA: Carnegie Mellon University.
- McComb C, Cagan J and Kotovsky K (2015) Lifting the Veil: drawing insights about design teams from a cognitively inspired computational model. *Design Studies* 40, 119–142.
- McComb C, Cagan J and Kotovsky K (2017) Optimizing design teams based on problem properties computational team simulations and an applied empirical test. *Journal of Mechanical Design* 139, 041101-1–041101-12.
- More JS and Lingam C (2019) A SI model for social media influencer maximization. Applied Computing and Informatics 15, 102–108.
- Mui L, Mohtashemi M and Halberstadt A (2002) A Computational Model of Trust and Reputation. Hawaii: IEEE.
- Murdock BB (1962) The serial position effect of free recall. Journal of Experimental Psychology 64, 482–488.
- Myers DG (1982) Polarizing effects of social interaction. In Brandstatter H, Davis JH and Stocker-Kreichgauer G (eds), *Group Decision Making*. London: Academic Press, pp. 125–161.
- Nowak A, Szamrej J and Latané B (1990) From private attitude to public opinion: a dynamic theory of social impact. *Psychological Review* 97, 362–376.
- **Oberauer K and Lewandowsky S** (2008) Forgetting in immediate serial recall: decay, temporal distinctiveness, or interference? *Psychological Review* **115**, 544–576.
- **O'Brien MJ and Bentley RA** (2011) Stimulated variation and cascades: two processes in the evolution of complex technological systems. *Journal of Archaeological Method and Theory* **18**, 309–335.
- Ohland MW, Loughry ML, Woehr DJ, Bullard LG, Felder RM, Finelli CJ, Layton RA, Pomeranz HR and Schmucker DG (2012) The comprehensive assessment of team member effectiveness: development of a behaviorally anchored rating scale for self- and peer evaluation. Academy of Management Learning & Education 11, 609–630.
- Paivio A (1969) Mental imagery in associative learning and memory. Psychological Review 76, 241–263.

Paulus PB (2000) Groups, teams, and creativity: the creative potential of ideagenerating groups. Applied Psychology: An International Review 49, 237–262.

- Paulus PB and Dzindolet MT (1993) Social influence processes in group brainstorming. Journal of Personality and Social Psychology 64, 575–586.
- Paulus PB and Dzindolet M (2008) Social influence, creativity and innovation. Social Influence 3, 228–247.
- Perišić MM, Štorga M and Gero JS (2018) Exploring the effect of experience on team behavior: a computational approach. *International Conference on Design Computing and Cognition*'18. Lecco, Italy, pp. 595–612.
- Pillai R and Williams EA (2004) Transformational leadership, self-efficacy, group cohesiveness, commitment, and performance. Journal of Organizational Change Management 17, 144–159. doi:10.1108/ 09534810410530584
- Proschan F (2012) Theoretical explanation of observed decreasing failure rate. Technometrics 5, 375–383.
- Read D and Grushka-Cockayne Y (2010) The similarity heuristic. Journal of Behavioral Decision Making 24, 23–46.
- Ryan RM and Deci EL (2000) Intrinsic and extrinsic motivations: classic definitions and new directions. *Contemporary Educational Psychology* 25, 54–67.
- Salas E et al. (2005) Modeling team performance: the basic ingredients and research needs. In Rouse WB and Boff KR (eds), Organizational Simulation. Hoboken, NJ: Wiley, pp. 185–228.
- Saunders R and Gero JS (2004) Curious agents and situated design evaluations. Artificial Intelligence for Engineering Design, Analysis and Manufacturing 18, 153–161.
- Sayama H, Farrell DL and Dionne SD (2010) The effects of mental model formation on group decision making: an agent-based simulation. *Complexity* 16, 49–57.
- Schreiber C, Singh S and Carley KM (2004) Construct A Multi-Agent Network Model for the Co-evolution of Agents and Socio-Cultural Environments. Pittsburgh, USA: CASOS – Center for Computational Analysis of Social and Organizational Systems, Carnegie Mellon University.

- Shah JJ, Smith SM and Vargas-Hernandez N (2003) Metrics for measuring ideation effectiveness. *Design Studies* 24, 111-134.
- Singh V (2009) Computational Studies on the Role of Social Learning in the Formation of Team Mental Models (PhD thesis). Design Lab Faculty of Architecture, Design and Planning the University of Sydney, Sydney.
- Singh V, Dong A and Gero JS (2011) How important is team structure to team performance? Proceedings of the 18th International Conference on Engineering Design (ICED 11). Copenhagen, Denmark.
- Singh H, Cascini G, Casakin H and Singh V (2019) A computational framework for exploring the socio-cognitive features of teams and their influence on design outcomes. Proceedings of the 22nd International Conference on Engineering Design (ICED19). Delft, The Netherlands: The Design Society.
- Singh H, Cascini G and McComb C (2020) Analysing the effect of self-efficacy and influencers on design team performance. *Proceedings of the Design Society: DESIGN Conference.* Dubrovnik, Croatia: The Design Society.
- Stempfle J and Badke-Schaub P (2002) Thinking in design teams an analysis of team communication. *Design Studies* 23, 473–496.
- Syna Desivilya Helena and Eizen Dafna (2005) CONFLICT MANAGEMENT IN WORK TEAMS: THE ROLE OF SOCIAL SELF-EFFICACY AND GROUP IDENTIFICATION. International Journal of Conflict Management 16, 183–208. http://dx.doi.org/10.1108/eb022928
- Whiten A, McGuigan N, Marshall-Pescini S and Hopper LM (2009) Emulation, imitation, over-imitation and the scope of culture for child and chimpanzee. *Philosophical Transactions of the Royal Society B* 364, 2417–2428.
- Wilkins DJ (2002) The Bathtub curve and product failure behavior, part one: The Bathtub curve, infant mortality and burn-in. *Reliability Hotwire: The eMagazine for the Reliability Professional* (21). Available at https://www.weibull.com/hotwire/issue21/hottopics21.htm
- Wimmer EG and Shohamy D (2012) Preference by association: how memory mechanisms in the hippocampus bias decisions. *Science* 338, 270–273.
- Wu Z and Duffy AH (2004) Modeling collective learning in design. Artificial Intelligence for Engineering Design, Analysis and Manufacturing 18, 289–313.

Appendix A

Table A1

Table A1. The values of model parameters that were assigned when an idea generation activity starts

Model parameter	Value	Status
Number of agents	6	Constant
Agent self-efficacies	Low self-efficacies between 0.1 and 0.2	
	Changes (increases or decreases) with the sessions	
	High self-efficacies between 0.4 and 0.5	
Agent expertise level	1-10	Increases with sessions
Agent work experience	0	Constant
Familiarity	0	Increases with sessions (as the same team of agents are working together in all the sessions)
Number of design peaks	5	Constant
Number of sessions	10	Constant
Number of steps taken to generate the final solution (or the length of idea generation activity)	10	Constant
Number simulations	200	Constant

Appendix B

Link to the questionnaires:

Part 1: https://forms.office.com/Pages/ResponsePage.aspx?id=K3EXCvNtX UKAjjCd8ope6-5WK7zPMwFMqdi9F2m40mJUMTdYWE1QRjI3VVNJVDZ LWloyNDJTN1lMVy4u

Please answer the following set of questions by expressing your agreement in reference to the proposed sentences. It is necessary to check just a box per each question.* I completely disagree | partially disagree | partially agree | completely agree I am very good at problem solving tools are of vial importance I am never intimidate by the unknown problems I am unable at tackling unfamiliar tasks So far have been able to neosher every problem I face I am certain that I am able to recolve every problem I face

Please answer the following set of questions by expressing your agreement in reference to the proposed sentences. It is necessary to check just a box per each question. *

	I completely disagree	I partially disagree	I partially agree	I completely agree
WHEN I AM SOLVING A PROBLEM I always take into account similar problems in different fields of technique				
WHEN I AM SOLVING A PROBLEM I always neglect all the elements that are not directly involved in the problem				
WHEN I AM SOLVING A PROBLEM I never follow a predefined strategy				
WHEN I AM SOLVING A PROBLEM I always consider the best desirable solution even if not technically feasible				
WHEN I AM SOLVING A PROBLEM I always consider the impact of design choices on all the requirements				
WHEN I AM SOLVING A PROBLEM The focus is always on the structure/layout of the technical system				
WHEN I AM SOLVING A PROBLEM It is necessary to find the best compromise among system requirements				
WHEN I AM SOLVING A PROBLEM I always try to modify the system as less as possible				

Rate your degree of confidence now (i.e. belief in your current ability) to perform the following tasks *

	Not confident at all	Poorly confident	Moderately confident	Fully confident
Identify a design need				
Research a design need				
Develop design solutions				
Select the best possible design				
Construct a prototype				
Evaluate and test a design				
Communicate a design				
Redesign				

Rate how motivated you are now to perform the following tasks *

	Not motivated at all	Poorly motivated	Moderately motivated	Fully motivated
Identify a design need				
Research a design need				
Develop design solutions				
Select the best possible design				
Construct a prototype				
Evaluate and test a design				
Communicate a design				
Redesign				

Rate how successful you think you would be in performing the following tasks now *

	Not successful at all	Poorly successful	Moderately successful	Fully successful
Identify a design need				
Research a design need				
Develop design solutions				
Select the best possible design				
Construct a prototype				
Evaluate and test a design				
Communicate a design				
Redesign				

Rate your degree of anxiety now (how apprehensive you would be) in performing the following tasks *

	Extremely anxious	Moderately anxious	A little anxious	Not anxious at all
Identify a design need				
Research a design need				
Develop design solutions				
Select the best possible design				
Construct a prototype				
Evaluate and test a design				
Communicate a design				
Redesign				

Part 2 additional: https://forms.office.com/Pages/ResponsePage.aspx?id= K3EXCvNtXUKAjjCd8ope6-5WK7zPMwFMqdi9F2m40mJUOEdTVEpZTlJK SkgyM1o1NkVRQVJVNFBPMC4u

nate your team mem	vers and yours	en according	y to then con	in bution to	the team	s non, miere.
5 = he/she does more improve the team's w	or higher-qui ork. Helps to c	ality work th omplete the	an expected. work of tea	Makes impo mmates who	ortant con are havin	tributions that g difficulty.
4 = he/she exhibits so	me behaviour	from 5 and	some from 3	i.		
3 = he/she completes commitments and cor important	a fair share of npletes assign	the team's ments on tir	work with ac ne. Fills in fo	ceptable qua r teammates	ality. Keep when it is	s s easy or
2 = he/she exhibits so	me behaviour	from 3 and	some from 1			
1= Does not do a fair deadlines. Is late, unp the work becomes dif	share of the te repared, or ab ficult	eam's work. I sent for tean	Delivers slop n meetings. I	py or incom Does not ass	plete work ist teamm	r. Misses ates. Quits if
Not applicable= if the	team membe	r does not e	xist *			
	1	2	3	4	5	not applicable
yourself	1	2	3	4	5	not applicable

Rate your team member	rs and yourself	f according t	to their inter	action with t	teammate	s, where:		Rate ONLY your team m where:	embers acco	ording to	the extent	t this team	n member	has influ	enced you,	
5 = he/she asks for and communication among ceammates for feedback	shows an inte teammates. Pr and uses thei	rest in team rovides enco ir suggestior	mates' ideas iuragement ns to improv	and contrib or enthusiasr e.	utions. Im m to the t	proves eam. Asks		5 = You follow his/her to keep into account his/h You agree to him/her m	chniques ar proposed ost of the tir	nd actions I solution i me	of genera nto accou	ating inno Int while g	ovative sol generating	utions. \ your ov	/ou always vn solutions.	
4 = he/she exhibits som	e behaviour fr	om 5 and so	ome from 3					4 = You were influenced	comewhat	like the n	nints ment	tioned in 9	5 and som	na in 3		
3 = he/she listens to tea thares information with responds to feedback fr	immates and r teammates. P om teammate	espects thei articipates fu s	r contributio ully in team a	ons. Commun activities and	nicates cle d respects	arly and and		3 = You sometimes follo sometimes consider his, You agree to him/her so	w his/her te her propose metimes	echniques ed solutio	and action	ns of gene ount while	erating in e generati	novative ng your	solutions. Yo own solutior	9U 15.
2 = he/she exhibits som	e behaviour fr	rom 3 and so	ome from 1					4 = You were influenced	somewhat	like the n	oints ment	tioned in 3	3 and son	na in 1		
I = he/she interrupts, ig without their input. Doe with teammates. Accept	nores or make s not share inf s no help or a	s fun of tear formation. C dvice.	nmates. Taki omplains, m	es actions the akes excuses	at affect ti s, or does	eammates not interact		1 = You never follow his, consider his/her propos agree to him/her	her techniq ed solution	ues and a into accou	ctions of g int while g	generating generating	g innovati g your ow	ve solutio n solutio	ons. You nev ns. You neve	er F
Not applicable= if the te	eam member o	does not exis	st *					Not applicable= if the te	am membe	r does no	t exist *					
	1	2	3	4	5	not applicable			1	3	3		4	5	not applical	hia
yourself								team member 1	0	0	0		6	0	not apprica	
team member 1								ceant member 1					~		0	
track, where: 5 = he/she watches co that teammates are m constructive feedback 4 = he/she exhibits so 3 = he/she exhibits so should be doing and r success is threatened 2 = he/she exhibits so 1= he/she is unaware teammates' progress. Not applicable= if the	nditions affec aking appropr me behaviour anges that infli notices probler me behaviour of whether the Avoids discuss team membe	ting the tear iate progres from 5 and uence the te ms. Alerts te from 3 and e team is me sing team pr r does not e	m and moni is. Gives tear some from : ammates or some from seting its go roblems, eve xist *	tors the tean mmates spec 3 is. Knows wh suggests so 1 als or not. Di n when they	n's progre cific, timel nat everyo lutions wi oes not p. y are obvio	ess. Makes sure y, and ne on the team hen the team's ay attention to ous.		5 = You always trust 4 = You trust him/he 3 = You trust him/he 4 = You trust him/he 1= You never trust h Not applicable= if th team member 1	him/her c r between er partially r between nim/her wit e team me 1	omplete in 5 and with his/ in 3 and th his/he ember do	y with hi 3 'her prop 1 r propose es not es 2	s/her pro posed sol ed solution xist * 3	oposed s lutions ons	4	s 5 ()	not applicable
	1	2	3	4	5	not applicable		Rate ONLY your team	n members	s on the	basis of I	how fam	niliar you	were w	ith this me	mber before
yourself								working on this activ	ity, where:							
team member 1								5 = You knew him/h	er very wel	ll before	you start	ted this a	activity			
. Rate your team memt work, where: 5 = he/she motivates even if there is no add 4 = he/she exhibits so 3 = he/she encourage to perform well enoug responsibilities	the team to d ditional reward ome behaviou is the team to gh to earn all	self accordin do excellent d. Believes t r from 5 and o do good w available re	ng to the eff work. Cares hat the tear d some fron work that me wards. Belie	fort spent in s that the tea m can do exc n 3 rets all requi wes that the	am does o cellent wo irements. team car	ing the quality o outstanding worl ork. Wants the team o fully meet its	-	4 = You know him/h 3 = You somewhat k 4 = You know him/h 1= You were comple Not applicable= if th	er betweer new him/h er betweer tely unfam e team me	n in 5 an ner befor n in 3 an niliar with ember do	d 3 e d 1 him/he pes not e	er before exist *	e you sta	rted thi	s activity	
2 = he/she exhibits so	me behaviou	r from 3 and	d some fron	n 1					1		2	3		4	5	not applica
1= he/she is satisfied	even if the te	am does no	t meet assid	aned standa	rds. Want	ts the team to								0		nos applica
avoid work, even if it l	hurts the team	n. Doubts th	hat the team	n can meet it	ts require	ments.		team member 1	0	2	0	9		0	Ú.	0

Not applicable= if the team member does not exist *

	1	2	3	4	5	not applicable
yourself						
team member 1						

Rate your team members and yourself according to the relevant knowledge, skills and abilities,

5 = he/she demonstrates the knowledge, skills, and abilities to do excellent work. Acquires new knowledge or skills to improve the team's performance. Able to perform the role of any team member if necessary.

4 = he/she exhibits some behaviour from 5 and some from 3

3 = he/she has sufficient knowledge, skills, and abilities to contribute to the team's work. Acquires knowledge or skills needed to meet requirements. Able to perform some of the tasks normally done by other team members

2 = he/she exhibits some behaviour from 3 and some from 1

1= he/she is missing basic qualifications needed to be a member of the team. Unable or unwilling to develop knowledge or skills to contribute to the team. Unable to perform any of the duties of other team members

Not applicable= if the team member does not exist *

	1	2	3	4	5	not applicable
yourself						
team member 1						

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not applicable

for

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