This identity holds for $0 \le x \le 1$ by the above argument. A careful calculus computation implies that it holds for each $x \ge -1$.

References

 M. Hassani, Proof without words, Math. Gaz. 105 (July 2021) p. 303.
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106.10 PWW: Trigonometric inequality

For each natural number n, $\sin\left(\frac{30}{n}\right)^{\circ} \ge \frac{1}{2n}$. Equality holds only for n = 1.



$$2ny \ge x \implies \sin\left(\frac{30}{n}\right)^\circ = \frac{y}{x} \ge \frac{1}{2n}$$

FIGURE 1

Note: This inequality is a particular case of the inequality $\sin \lambda x \ge \lambda \sin x$ that holds for each $x \in [0, \pi]$ and $\lambda \in [0, 1]$.10.1017/mag.2022.25 © The Authors, 2022VICTOR OXMANPublished by Cambridge University Press on
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