Evidence of strong contribution from neutral atoms in intense harmonic generation from nanoparticles

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Abstract

We show experimental evidence that, for the intense high-order harmonics from nanoparticles, there is a strong contribution from neutral atoms. We present the results of studies on the harmonics generated in laser-produced plasmas containing various nanoparticles, including Cr_2O_3 , In_2O_3 , Ag, MnTiO_3, Sn, Cu, and Au. These results are compared with the harmonics generated from plasma produced on the surface of bulk targets. The harmonic spectrum from nanoparticle and bulk In_2O_3 show that there is a lack in the resonant enhancement of the 13th harmonic for the former. Along with the relatively low cut-off for nanoparticle harmonics, these results show that it is the neutral atom in the nanoparticle that emits the intense harmonics. Structural studies of plasma debris confirm the presence and integrity of nanoparticles in the plasma plumes.

Keywords: Atomic/ionic media; Clusters; High-order harmonic generation; Nanoparticle

INTRODUCTION

Extensive studies in the past have advanced our understanding of the interaction of intense lasers with single atomic/ ionic media. In particular, this has led to high-order harmonic generation (HHG) and the generation of short wavelength coherent radiation (Hafeez *et al.*, 2008; Ozaki *et al.*, 2008). Meanwhile, the enhanced nonlinear optical response of multi-atomic particles induced by quantum confinement has attracted much interest, with novel applications in optoelectronics, optical switchers, and limiters, as well as in optical computers, optical memory, and nonlinear spectroscopy. High values of third-order nonlinear susceptibility, especially near the surface plasmon resonances of nanostructured materials, are the trademark of these media, in particular metal clusters.

Clusters subject to intense laser pulses produce strong loworder nonlinear optical response (e.g., nonlinear refraction and nonlinear absorption), and can also emit coherent radiation through high-order harmonic generation (Liao *et al.*, 1997; Shvetsov-Shilovski *et al.*, 2007; Mulser *et al.*, 2005). Such studies have shown that one can improve the harmonic generation efficiency by using cluster media. Meantime, previous studies on the harmonic generation in such objects were limited to exotic nanoclusters (Ar, Xe), which are formed in high-pressure gas jets *via* rapid cooling by adiabatic expansion.

High-order harmonic generation from atomic gas clusters has been observed with an increase in the cut-off order and harmonic intensity (Donnelly et al., 1996; Tisch et al., 1997; Vozzi et al., 2005), and tomographic measurement of high harmonic generation in a cluster jet has been demonstrated (Pai et al., 2006). Theoretical investigations on harmonic generation from clusters have also been performed (Hu & Xu, 1997; Tisch, 2000; Veniard et al., 2001; Vazquez de Aldana & Roso, 2001; Kundu et al., 2007; Tajima et al., 1999; Fomits'kyi et al., 2004; Fomichev et al., 2005). For example, the enhancement in the harmonic yield has been modeled using simulation (Hu & Xu, 1997), and it has been shown theoretically that one can use nanoparticles to improve phase matching conditions (Tisch, 2000). On the other hand, clusters have also been shown to have strong effects on low-order harmonics, such as the third-order harmonics from an expanding cluster (Shim et al., 2007). Recently, there has been a new approach to generate high-order harmonics using metallic nanoparticles, and in particular using laser plasma of targets rich in nanoparticles as the nonlinear medium (Ganeev et al., 2007a, 2008a, 2008b, 2008c).

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An important issue in laser ablation of nanoparticles is their integrity during evaporation from the target (Fazio *et al.*, 2009). One could expect fragmentation, melting, or aggregation of nanoparticles due to irradiation of the laser. To achieve harmonic generation from clusters, one should not over-excite the targets that are rich in nanoparticles when producing the plasma, where these species exist in their native neutral (or ionized) conditions.

In this paper, we demonstrate the high-order nonlinear optical properties of various nanoparticles. These HHG studies were carried out using the ablation of clustered media using sub-nanosecond laser prepulse, and subsequently irradiating the nanoparticle-rich plasma with a femtosecond pulse. The presence of nanoparticles in the plasma was carefully studied by analyzing the spatial characteristics of the debris of the ablated material deposited on a nearby substrate. We show that the nanoparticles maintain their integrity in the plasma plume under optimal conditions for exciting clusters. Moreover, through experimental results on harmonic generation using In₂O₃ nanoparticles and bulk, we show that it is the neutral atoms in the nanoparticle that emits the strong harmonic emission, which has been observed as an increased low-order harmonic yield for nanoparticle-rich plumes when compared with monoparticle-rich plasmas.

EXPERIMENTAL RESULTS AND DISCUSSION

High-Order Harmonic Generation from Nanoparticles

Experiments were carried out with the 10 Hz, 10 TW beam line of the Canadian Advanced Laser Light Source at the Institut national de la recherche scientifique (Ozaki et al., 2006). To create the ablation, a prepulse that was split from the uncompressed Ti:sapphire laser ($t_{pp} = 210 \text{ ps}$) was focused on a target placed in the vacuum chamber (see inset in Fig. 1). The intensity of the sub-nanosecond prepulse $(I_{\rm DD})$ on the target surface was varied between 2×10^9 and 1×10^{10} W cm⁻². After a proper delay (6–74 ns), the femtosecond main pulse ($t_{\rm fp} = 35$ fs, $\lambda = 800$ nm central wavelength, 35 nm full width at half maximum) was focused on the plasma from the orthogonal direction. Our HHG experiments were performed with laser intensities of up to $I_{\rm fp} = 7 \times 10^{14} \text{ Wcm}^{-2}$, above which the HHG efficiency decreased considerably due to several impeding processes in the laser plasma. The harmonics were spectrally dispersed by an extreme ultraviolet spectrometer, detected by a micro-channel plate, and recorded using a chargecoupled device camera.

In these studies, we used various nanosized powders (Cr₂O₃, In₂O₃, Ag, Cu, MnTiO₃, Sn, and Au; Alfa Aestar).



Fig. 1. (Color online) Harmonic spectra obtained from plasmas produced on the surfaces of (1) bulk Ag, and (2 and 3) Ag nanoparticle-rich target. The intensities of prepulse on the target surfaces were (1) 3×10^{10} Wcm⁻², (2) 7×10^{9} Wcm⁻², and (3) 2×10^{10} Wcm⁻². Inset: Experimental setup. MP: main pulse; PP: prepulse; DL: delay line; C: grating compressor; FL: focusing lenses; T: target; G: gold-coated grating; MCP: micro-channel plate; CCD: charge-coupled device.

The sizes of nanoparticles varied from 30 to 200 nm. The powder was glued on the glass substrate by mixing with epoxy. We also used bulk targets of the same materials to compare the HHG from the monoparticle-rich plumes.

These studies were concentrated on two issues: (1) comparison of the harmonic spectra generated in plasmas containing single atomic/ionic particles and nanoparticles, and (2) structural characterization of the plasma ingredients. First, we reproduced the harmonic generation in the plasmas produced from bulk targets, which has been reported in our previous studies (Elouga Bom *et al.*, 2007; Ganeev *et al.*, 2007*b*, 2007*c*). In particular, the Ag plasma showed harmonics up to the 47th order (Fig. 1, curve 1).

When we ablated the Ag nanoparticle-rich targets and generated the harmonics in the plasma plumes, the cut-off was shifted toward the longer-wavelength part of the plateau. At the same time, the intensity of these harmonics was considerably higher compared with those generated in the monoparticle-rich plasma created on the surface of bulk Ag (Fig. 1, curve 2). Moreover, the spectral widths of harmonics were three to four times broader compared with the narrow lines of the harmonics generated in monoparticle-rich plasma. The enhancement factor of the harmonic intensity generated in nanoparticle-rich plumes (compared with monoparticle plume) varied from five-times to 12-times, depending on the harmonic order and the excitation conditions. Note that this intensity enhancement of low-order harmonics was observed for moderate excitation of Ag nanoparticle-rich targets $[I_{pp} \sim (5-7) \times 10^9 \text{ Wcm}^{-2}]$. With further increase in the prepulse intensity, a dramatic change in the harmonic spectra was observed, which showed the disappearance of low-order harmonics and the appearance of high-order ones (Fig. 1, curve 3). The intensity of these harmonics was considerably weaker, when compared to the intensity of loworder harmonics for low prepulse intensities.

These observations demonstrate the dynamics of harmonic generation and point out the particles responsible for this process. At moderate prepulse intensities, the plasma contains predominantly neutral nanoparticles. In that case, the harmonic cut-off is defined by the interaction of femtosecond pulse with neutral clusters. The cut-off is low, and from the main pulse intensity used, we estimate a cut-off around the 13th to the 17th harmonics. Increasing the prepulse intensity led to both an increase in the nanoparticle density as well as their ionization. Ionization results in lower harmonic yield, while the conditions for higher cut-off become more favorable. We have also performed experiments with epoxy plasma without nanoparticles, which did not produce high-order harmonics. From this we can conclude that the HHG from epoxy molecules is negligible. The same can be said about HHG from the substrate plasma, which did not generate harmonics at these low prepulse intensities.

The harmonics from Cr_2O_3 nanoparticle-rich plume showed a featureless plateau with a cut-off at the 31st order (Fig. 2, curve 1), while harmonics generated from bulk



Fig. 2. (Color online) Harmonic spectra obtained from the (1 and 3) Cr_2O_3 nanoparticle-rich plasma and (2) Cr monoparticle-rich plasma.

chromium plasma demonstrated a resonantly enhanced 29th harmonic and a cut-off at the 35th order (Fig. 2, curve 2). Note that the latter harmonic spectrum with an enhanced single harmonic is similar to those observed in previous studies of HHG from chromium plasma (Ganeev, 2007*b*, 2005). As can be seen in Figure 2 (curve 2), the 29th harmonic intensity in that case was considerably higher than the nearest 27th and 31st harmonics. The extension of the harmonic cut-off for plasma produced from bulk chromium is attributed to the involvement of the Cr⁺ ions in harmonic generation, while for nanoparticles, the neutrals were dominant in the HHG process.

Indium Oxide Nanoparticle Harmonics

A clearer understanding of the reason behind strong highorder harmonics from nanoparticles can be obtained from our experimental results using In₂O₃ targets. Figure 3 shows the comparison of the harmonic spectra generated in the plasmas produced from In₂O₃ bulk target and In₂O₃ nanoparticle-rich target. One can see a strong 13th harmonic generated for bulk targets, which has also been reported for HHG from In plasma abundant with In⁺ ions (Ganeev et al., 2006). The conversion efficiency of the 13th harmonic for bulk In_2O_3 target was measured to be close to 10^{-4} . For In_2O_3 nanoparticle plasma, we see a plateau without any signs of enhancement of the harmonic (Fig. 3, curve 1). One can see that the intensities of the 9th to the 13th harmonics for In₂O₃ nanoparticle plasma are comparable with that of the intensity enhanced 13th harmonic generated from the In_2O_3 bulk target (Fig. 3, curve 1). Thus, one can estimate that the conversion efficiency of the plateau harmonics for In_2O_3 nanoparticle plasma to be about 10^{-4} . This is the highest conversion efficiency reported so far for multiple harmonics generated in the plateau region.



Fig. 3. (Color online) Harmonic spectra observed for HHG from plasmas containing (1) In_2O_3 monoparticles and (2) In_2O_3 nanoparticles.

Another important observation of Figure 3 is the cut-off. For In_2O_3 nanoparticle harmonics, the cut-off is at the 17th harmonic, whereas that for bulk targets extends to the 57th order (not shown in Fig. 3), which is similar to the cut-off observed using pure indium targets (Ganeev *et al.*, 2006). We should also note here that the optimum prepulse intensity for HHG from nanoparticles is much lower than for bulk targets. We have observed that we can extend the cut-off of nanoparticle harmonics, but only by increasing the prepulse intensity, which also results in a drastic decrease in the harmonic intensity.

The enhancement of a single harmonic in In_2O_3 monoparticle plasma was attributed, to the effect of strong ionic transitions that have large oscillator strengths (Ganeev *et al.*, 2007*b*). For neutral material, it is difficult to find transitions of neutral atoms or clusters with similarly large oscillator strengths at these shorter wavelengths. This results in the decrease or disappearance of the enhancement of single harmonic for neutral nanoparticle-rich media.

Note that by increasing the prepulse intensity, plasma of chromium oxide nanoparticle led to the appearance of strong 29th harmonic (Fig. 2, curve 3). This is a sign of the ionization of nanoparticles in the plasma, since enhanced single harmonic in this spectral range has previously been attributed to the giant $3p \rightarrow 3d$ ionic transitions of chromium ions (Ganeev *et al.*, 2007*b*).

Other nanoparticle-rich plasma plumes demonstrated the same features; that is, a considerable enhancement of loworder harmonic intensity and a lower harmonic cut-off, compared with results using monomer plasmas produced from bulk targets. Increasing the intensity of the femtosecond pulse did not lead to the extension of the harmonic cut-off generated in nanoparticle plumes, which is a sign of saturation of the HHG in these media. Moreover, at relatively high laser intensities, we observed a decrease of harmonic conversion efficiency due to several impeding factors (such as over-ionization, increased free electron density, and selfdefocusing). The same can be said about increasing the prepulse intensity for nanoparticle-rich targets over a specific optimal value. In that case, inefficient harmonic generation was attributed to the increase in the free electron density and a subsequent phase mismatch.

These observations give a rough pattern of the ablation and HHG from the nanoparticle-rich targets. The material directly surrounding nanoparticles is epoxy, which has a lower ablation threshold than the nanoparticles. Therefore, the epoxy starts to ablate at relatively low prepulse intensities, carrying the nanoparticle with it, resulting in the lower prepulse intensity required for evaporating the target. This feature allowed for easier creation of the optimum plasma conditions, which resulted in better HHG conversion efficiency from the nanoparticle-rich plume compared with the plume from the bulk target. In particular, it was found that the HHG from multi-atomic particles started to be efficient at considerably smaller prepulse intensities $((3-6) \times 10^9 \text{ Wcm}^{-2})$ compared with the case of bulk targets $((1-3) \times 10^{10} \text{ Wcm}^{-2})$.

The results with In₂O₃ targets provide evidence for a clear understanding of intense harmonics from nanoparticles. First, we recall that the intensity enhancement of the 13th harmonic from indium plasma is due to the wavelength matching between the 13th harmonic and a strong radiative transition of the In⁺ ion (Ganeev et al., 2007b). From the experimental results in this section, we see that (1) there is no enhancement of the 13th harmonic for In₂O₃ nanoparticles at relatively low prepulse intensities; (2) one can obtain enhancement of the 13th harmonic even with nanoparticles, but one needs to increase the prepulse intensity. In this case, the overall harmonic yield is reduced; (3) the cut-off for harmonics from In_2O_3 nanoparticles is much lower than that for bulk targets. From these observations, we can conclude that the intense highorder harmonics from In₂O₃ nanoparticles are generated from neutral atoms in the nanoparticles. Stronger harmonic emission from neutrals is reasonable, since neutral atoms are larger in size compared with their ions, and so in the three-step model, the returning electron has a larger target to recombine to. We would like to note that harmonics from nanoparticles are most probably also affected by their size. However, the important finding of this work is that we also need to take into account the effects of neutral atoms.

STRUCTURE OF NANOPARTICLES IN THE PLASMA

The presence of nanoparticles in the plasma plumes was confirmed by analyzing the ablated material deposited on a nearby glass or aluminum substrates. It was shown that, at optimal excitation conditions, the nanoparticles remain intact in the plasma plume until the main femtosecond pulse arrives at the interaction area. Below we present the results of our studies on the nanoparticle structures deposited on nearby substrates by the laser ablation from the surfaces containing initial clustered powders.



Fig. 4. The SEM images of deposited (1) Cr_2O_3 , (2) Au, (3) Cu, and (4) Ag clusters during laser ablation of nanoparticle-rich targets. The length of lines corresponds to 1.5 μ m.

Under optimal conditions for harmonic generation, the scanning electron microscope (SEM) images of the deposited material revealed that the nanostructures remain roughly the same as the initial powders. The sizes of the deposited Cr_2O_3 nanoparticles were from 30 to 200 nm (Fig. 4.1). The same can be said about Au (40 to 250 nm, Fig. 4.2), Cu (60 to 180 nm, Fig. 4.3) and other deposited nanoparticles. The intensity of prepulse laser for the nanoparticle-rich targets in these experiments was kept in the range of 3×10^9 to 8×10^9 Wcm⁻². Increasing the prepulse intensity above a certain level led to the appearance of aggregated clusters with much bigger sizes (for example, the SEM image of deposited Ag clusters under these conditions, Fig. 4.4).

These SEM studies have demonstrated that the harmonics generated under optimal prepulse conditions are the result of the interaction of the femtosecond pulse with the cluster. Some additional supporting confirmation of this conclusion is as follows. For HHG in cluster plasma, we did not observe an extension of the cut-off, which could be associated with the involvement of ionized particles in the HHG process. The harmonic cut-off for the nanoparticle-rich plumes should be in the range of 13th-17th harmonics, considering the saturation intensity at which the neutral nanoparticles ionize ($\sim 1 \times 10^{14}$ Wcm⁻²). In most cases, high-order harmonics decreased or even disappeared with an increase in excitation and ionization of plasma. This is because the phase mismatch prevented the generation of harmonics above the cut-offs.

CONCLUSIONS

Our studies have shown that, for the nanoparticle-rich plumes investigated, there were no improvements in the extension of the harmonic cut-off. However, we have demonstrated an enhancement of the harmonic yield in the low-energy plateau range for the nanoparticle-rich plumes. The enhancement factor of the harmonics generated in nanoparticle-rich plumes (compared with the monoparticle-rich plasma plumes) varied from five-times to 12-times, depending on the harmonic order and the excitation conditions. Experimental results with In_2O_3 nanoparticles show that the intense harmonics from these targets are attributed to the contribution from neutral atoms in the nanoparticles.

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