## Orbit and Positioning Accuracy for New Generation Beidou Satellites during the Earth Eclipsing Period

Xiaojie Li<sup>1,2,3</sup>, Xiaogong Hu<sup>2,4</sup>, Rui Guo<sup>1</sup>, Chengpan Tang<sup>2,4</sup>, Shanshi Zhou<sup>2,4</sup>, Shuai Liu<sup>1</sup>, and Jianbing Chen<sup>5</sup>

<sup>1</sup>(Beijing Satellite Navigation Center, Beijing 100094, China) <sup>2</sup>(Shanghai Key Laboratory for Space Positioning and Navigation, Shanghai 200030, China)

<sup>3</sup>(State Key Laboratory of Geodesy and Earth's Dynamics, Wuhan 430077, China) <sup>4</sup>(Shanghai Astronomical Observatory, Shanghai 200030, China) <sup>5</sup>(China Top Communication Co., Ltd., Beijing 100088, China)

(E-mail: lxjant1984@126.com)

The Beidou System (BDS) started functioning at the end of 2012. The Yaw-Steering (YS) attitude mode for Inclined Geosynchronous Orbit (IGSO) and Medium Earth Orbit (MEO) satellites in BDS ensures that the solar panels face the Sun. The orbit radial accuracies for IGSO/MEO satellites are 0.5 m and the User Equivalent Range Errors (UERE) are 1.5 m in YS mode. BDS-2 satellites adopt Orbit-Normal (ON) mode to meet the power supply and thermal control requirements of the satellite during deep Earth eclipse periods. In ON mode, long-term orbit ephemeris accuracy monitoring in the Operational Control System (OCS) of BDS indicates that the orbit accuracies for IGSO/MEOs are reduced to a few hundreds of metres, seriously affecting the positioning accuracy and navigation service capability of the BDS system. Solar Radiation Pressure (SRP) is difficult to model in ON mode. Continuous Yaw-Steering (CYS) mode is available for new generation Beidou satellites launched since 2015. The orbit accuracies for these new generation Beidou (BDS-3) satellites were estimated based on BDS monitoring station data and SRP models including ECOM 9/5/3. The evaluation method consisted of four steps, namely, orbit internal consistency analysis, UERE calculation, Satellite Laser Ranging (SLR) data fitting Root Mean Square (RMS) determinations and positioning performance analysis; the data gathering period lasted for more than 60 days and included two CYS periods and one ON period. The experiments showed that the orbit accuracy of the radial component in CYS mode for the BDS-3 satellites degrades by 2 to 3 cm and positioning accuracy degrades only by 1 cm over that in YS mode which is just a small reduction in accuracy compared with the decimetre-level BDS orbit accuracy and the metre-level single point positioning accuracy with BDS pseudorange data. This overcomes declining orbit and positioning accuracy issues in ON mode for BDS-2 satellites. Other results also show that the reliability of BDS has been improved.

## KEYWORDS

 1. New generation Beidou satellites.
 2. Earth eclipsing period.
 3.Continuous yaw-steering mode.

 4. Global satellite laser ranging.

Submitted: 10 August 2017. Accepted: 16 February 2018. First published online: 26 March 2018.

1. INTRODUCTION. The Beidou System (BDS) started providing services at the end of 2012. In terms of the constellation, the regional BDS deploys Geostationary Orbit (GEO), Inclined Geosynchronous Orbit (IGSO), and Medium Earth Orbit (MEO) satellites (Li et al., 2014). The yaw attitude of IGSO/MEO satellites in the Beidou regional satellite navigation system (BDS-2) can be divided into nominal attitude and yaw angle at zero regimes. Generally, the satellite is in the nominal attitude regime, and this involves the use of Yaw-Steering (YS) mode. When these satellites are in the deep Earth eclipsing period, the yaw angle is always zero and the Orbit-Normal (ON) mode is employed. The yaw attitude mode of the GEOs is always in ON mode (Li et al., 2015). The orbit accuracy in the YS mode is stable (Steigenberger et al., 2013). Global Satellite Laser Ranging (SLR) Precise Orbit Determination (POD) has been carried out for BDS-M1 by Hauschild et al. (2012), and the mean orbit accuracy of the radial component of seven-day arcs was found to be better than 0.5 m. Application of POD by using SLR data and two-way C-band transfer ranging yielded a radial orbit accuracy of 0.13 m (Guo et al., 2015). Experiments performed with data from the Beidou regional stations have shown that with the Multi-satellite POD (MPOD) method, one can obtain orbit radial accuracies for IGSO/MEO satellites better than 0.5 m and User Equivalent Range Errors (UERE) including orbit error, satellite clock offset error, and ionosphere parameter error better than 1.5 m (Root Mean Square (RMS)) (Chen et al., 2016; Zhou et al., 2013).

The ON mode for IGSO/MEOs in BDS-2 lasts 8-15 days every year and varies with the satellite orbit. Long-term orbit ephemeris accuracy monitoring in the Operational Control System (OCS) of BDS indicates that the orbit accuracies for these satellites can be reduced to a few hundred metres in several hours, which seriously affects the positioning accuracy and navigation service capability of the BDS system (Guo et al., 2016). GNSS positioning relies on accurate satellite orbit and clock products whose errors, either from the system or by meaconing, would adversely affect positioning accuracy. This understanding is fundamental to GNSS applications (Ahmed, 2018; Cao et al., 2014; Hamad and Ahmed, 2007; Wang et al., 2011). Research has shown that Solar Radiation Pressure (SRP) is difficult to model in ON mode, and the SRP model and POD method in YS mode are not suitable for ON mode. Using BDS two-way frequency and time transfer between the Beidou satellites and Beidou Time (BDT), which is maintained at the master control station, Tang et al. (2016) proposed a new MPOD method supported by time synchronisation. One additional constant acceleration in the along-track direction was added to the Center for Orbit Determination in Europe (CODE) SRP model to improve the POD accuracy for IGSO/MEOs in ON mode (Guo, 2014); however, the orbit accuracy still declined to about 2 m, positioning accuracy with BDS pseudo-range data degrades by 1-2 m.

The orbit accuracies for other Global Navigation Satellite Systems (GNSS) satellites declines to different extents in the deep Earth eclipsing period. Urschl et al. (2007) showed the global SLR residuals for GPS PRN G05 and 06 respectively increased by 10 cm and 5 cm by the ROCK (designed by the Rockwell organisation) (Fliegel et al., 1992) and CODE (Springer et al., 1999) SRP models in the deepest shadow. Steigenberger and Montenbruck (2016) presented that the orbit accuracy for Galileo-101/102/103 satellites declined by 5 to 10 cm in the deepest shadow using the extended Empirical CODE Orbit Model (ECOM-2). This work showed that the SLR residuals for QZS-1 satellite increased by 40 cm using the ECOM model in deep shadow (Montenbruck et al., 2017; Steigenberger and Montenbruck, 2017).

Coverage of BDS GEO/IGSO satellites only includes the Asian-Pacific region, and thus MEO satellites have become the most important component of the constellation in the Beidou global navigation system (BDS-3); given this, the declining navigation and positioning accuracy issue for MEO satellites during the deep Earth eclipsing period must be solved. To meet the requirements of the satellite's power supply and thermal control, Continuous Yaw-Steering (CYS) mode has been improved for new generation Beidou satellites launched since 2015. Like the ON mode, CYS mode is employed not only to meet the power supply and thermal control requirements of the satellite, but also to avoid rapid yaw-slews near Sun–spacecraft–Earth collinearity.

The manner of realisation for POD for Beidou satellites in CYS mode and ways to ensure high-precision and high-stability navigation and positioning service are topics of the greatest concern while the BDS-3 system is under construction. At present, there is no research on POD and positioning in CYS mode for BDS-3 satellites that we are aware of. We will research this problem in detail.

2. ATTITUDE CONTROL MODE FOR THE NAVIGATION SATELLITES. The BDS navigation satellites have three attitude control modes, namely, YS mode, ON mode, and CYS mode. Attitude control of navigation satellites is dictated by two requirements or constraints: first, the transmitting antenna always points toward the Earth, and second, the solar panels are generally oriented perpendicular to the Sun-direction to ensure that the panels are facing the Sun. These requirements necessitate that the satellites constantly rotate (yaw) along the antenna axis, which points toward the Earth. The nominal yaw attitude control mode is the YS mode (Bar-Sever, 1996).

The  $\beta$  angle is the acute angle between the Earth-Sun direction and the orbit plane. When the satellite is within the deep Earth eclipsing period, the lower the  $\beta$  angle, the higher the hardware yaw rate. The nominal yaw attitude has two singularities that decompose when the satellite-Earth and satellite-Sun vectors are collinear, which results in two 180° discontinuities. The collinear and nearly collinear vectors cause so-called "noon" and "midnight" rapid turn manoeuvres, which exceed the maximum hardware yaw rate. The noon turn is at the closest point to the Sun and the midnight turn is at the farthest point from the Sun, when a satellite is in Earth's shadow. The ON mode is employed not only to meet the power supply and thermal control requirements of the satellite, but also to avoid rapid yaw-slews near Sun-spacecraft-Earth collinearity for IGSO/MEOs in BDS-2 (Guo et al., 2017; Dai et al., 2015). Melachroinos et al. (2017) have developed a model in which it makes more sense for the Attitude Determination and Control System (ADCS) system to follow a  $\beta^{\circ}$ -fixed law for its yaw angle than a 0°-fixed law. In reality, the switch points from YS to ON for BDS-2 IGSO/MEOs are as follows:  $|\beta| < 4^{\circ}$  and yaw angle  $|\varphi| \le 5^{\circ}$ , the yaw angle is always zero in ON mode. So, the ADCS will perform sudden rump-up and rump-down "jumps" to 0° yaw angle at the switch points from YS to ON and ON to YS. Figure 1 shows the yaw angle from YS to ON and ON to YS by the telemetry data for C08, C11 and C12 satellites in the BDS-2 system. The ON mode begins and ends at  $\varphi = 5^{\circ}$  and  $\varphi = -5^{\circ}$ . The interruption of the yaw angle means that the satellite cannot be monitored by regional BDS monitoring stations. ON mode does not experience noon-turn and midnight-turn manoeuvres.

Figure 2 shows the declining orbit User Ranging Error (URE) accuracy for the C10 satellite during February 2013 in ON mode as operated by the Beidou ground control system.



Figure 1. Yaw angle from YS to ON and ON to YS by the telemetry data in the BDS-2 system.



Figure 2. Orbit URE accuracy for the C10 satellite in ON mode.

A straight line represents the beginning of ON mode, and the orbit accuracy declines to more than  $70 \,\mathrm{m}$  over  $10 \,\mathrm{h}$ .

The CYS mode is adopted not only to solve the problem of limited hardware yaw rate during the "noon" and "midnight" rapid turn manoeuvres, but also to meet the power supply



Figure 3. Yaw angle in YS and CYS mode for BDS-3 satellites.

and thermal control requirements of the IGSO/MEOs in BDS-3. Sun azimuth  $\alpha$  is the angle between Earth-satellite vector and Earth-"noon" vector on the orbit plane. "Noon" turn and "midnight" turn start when  $|\beta| < 3^{\circ}$ ,  $|\alpha| \le 10^{\circ}$  or  $|\alpha \pm 180^{\circ}| \le 10^{\circ}$  and the solar sensor can no longer control the yaw attitude. The satellites start to yaw with estimated (BDS and Galileo) or maximum (Global Positioning System (GPS) and GLONASS) hardware yaw rates to make the yaw angle transform  $180^{\circ}$ ; at this time, the yaw attitude departs from the nominal values and it can take up to 30 min to 1 h to correct. Figure 3 shows the yaw angle in YS and CYS modes for BDS-3 satellites. The nominal yaw angle is followed in YS mode and the estimated yaw angle is followed in CYS mode.

CYS mode is similar to the attitude control mode in "noon" and "midnight" rapid turn manoeuvres for GPS satellites. The noon and midnight turn problems for the GPS Block IIF satellites are due to insufficient hardware yaw rates, which cause the estimated yaw angle to temporarily lag behind the nominal yaw attitude (Dilssner et al., 2011a).

For the new generation BDS satellites, the estimated yaw angle  $\varphi$  is as follows:

$$\varphi = \begin{cases} \operatorname{atan2}(\tan\beta, \sin\mu) & |\beta| \ge \beta_0\\ \operatorname{atan2}(\tan\beta^*, \sin\mu) & |\beta| < \beta_0, \ |\alpha| \le 10^\circ \quad \text{or} \quad |\alpha \pm 180^\circ| \le 10^\circ \end{cases}$$
(1)

where  $\beta_0 = 3$ .  $\beta^*$  is a virtual function of  $\alpha$  and  $\mu$  is the satellite's angle on the orbit plane (that is, orbital angle). When  $\alpha = 0^\circ$  or  $\alpha = \pm 180^\circ$ ,  $\beta^*(\alpha) = \text{sign}(\beta) \cdot \beta_0$ , when  $|\alpha| \le 10^\circ$  or  $|\alpha \pm 180^\circ| \le 10^\circ$ ,  $\beta^*$  is expressed in the form of an exponential function of  $\alpha$ .

In the BDS-3 system, IGSO/MEO satellites adopt the YS mode when  $\beta > 3^{\circ}$  and the CYS mode when  $\beta < 3^{\circ}$ . For the BDS GEO satellites, the ON mode is continuously maintained. The attitude mode and "noon" and "midnight" rapid turn manoeuvre modes for GNSS satellites are listed in Table 1.

When  $\beta$  is large, the nominal yaw angle and YS mode are adopted, and attitude modes are different when  $\beta$  is small or during the deep eclipsing period. For "noon" and "midnight" turn modes, the eclipsing yaw attitude control consists of the following two distinct regimes: (1) ON mode,  $\varphi = 0$  and (2) CYS mode, where the estimated yaw angle replaces the nominal yaw angle. BDS-2 and Quasi-Zenith Satellite System (QZSS) satellites adopt the ON mode within the deep Earth eclipsing period, whereas BDS-3, GPS, GLONASS, and GALILEO satellites adopt the CYS mode throughout this time, but there are small differences among the functions of the estimated yaw angle.

3. ANALYSIS OF THE CHARACTERISTICS OF THE SRP MODEL. The modelling accuracy of dynamic models affects the orbit accuracy, and SRP is the most difficult to model for Beidou satellites. In particular, an SRP model will depend on the satellite attitude, relative position between the satellite and Sun, area-mass ratio of the satellite, radiation intensity of the Sun, satellite geometry, surface material quality, and so on. Significant milestones in the history of SRP model development include the ROCK model, T10/T20/T30 model, Empirical CODE Orbit model (ECOM), GSPM.97/GSPM.04 model, and Adjustable Box-wing SRP model (Wu et al., 2015).

At present, BDS does not have its own SRP model. The ECOM model is the most widely adopted empirical SRP model for GPS Block II, Block IIA, and Block IIR applications. The ECOM model expresses the SRP acceleration in the (B, Y, D) frame where the satellite-Sun vector is along the D-axis, the Y-axis lies along the solar panel rotation axis direction, and the B-axis completes the right-handed coordinate system. It uses an optimal parameterisation of SRP, which has been shown to be in the order of centimetres in magnitude for GPS satellites (Steigenberger and Montenbruck, 2016). Thus, we conducted experiments on PODs for Beidou satellites in CYS mode based on the ECOM model. The formula is as follows:

$$\vec{a}_{SPR} = \vec{a}_{ROCK} + D(u) \times \vec{e}_D + Y(u) \times \vec{e}_Y + B(u) \times \vec{e}_B$$

$$D(u) = D_0 + D_c \cdot \cos u + D_s \cdot \sin u$$

$$Y(u) = Y_0 + Y_c \cdot \cos u + Y_s \cdot \sin u$$

$$B(u) = B_0 + B_c \cdot \cos u + B_s \cdot \sin u$$
(2)

where  $\vec{a}_{SPR}$  is the acceleration of SRP;  $\vec{a}_{ROCK}$  is the acceleration of the ROCK model; *u* is the argument of the ascending node; and  $D_0$ ,  $D_c$ ,  $D_s$ ,  $Y_0$ ,  $Y_c$ ,  $Y_s$ ,  $B_0$ ,  $B_c$  and  $B_s$  are constant parameters, which are estimated in the orbit determination.

The accuracy of the ECOM 9 model is closely related to the quantity and quality of observation data. With low amounts of data, the accuracy of the ECOM 9 model results will be relatively low. The visibility arc for MEOs in Beidou is about 8 h every day because of the structure of the regional monitoring net, and the accuracy of the corresponding ECOM 9 model results is comparatively low. In regard to IGSO/MEOs in Beidou, there are not obvious periodic terms in the Y- and B-axis, and only a reduced set of five parameters ( $D_0$ ,  $D_c$ ,  $D_s$ ,  $Y_0$ ,  $B_0$ ) is usually estimated, namely, through the application of the ECOM 5 model; the correlation of these parameters is low, and hence, the orbit accuracy and stabilisation for IGSO/MEOs can be improved based on the ECOM 5 model. There are only  $D_0$ ,  $Y_0$ ,  $B_0$  in the ECOM 3 model. The relevant experiments follow.

4. EXPERIMENT AND DISCUSSION FOR GNSS SATELLITES IN THE EARTH ECLIPSING PERIOD. For navigation satellites, SLR represents a unique high precision measurement independent of radio carrier phase measurements, and it is an important

	BDS-2	BDS-3	GPS Block II/IIA	GPS Block IIR	GPS Block IIF	GLONASS-M	GALILEO	QZSS
Attitude mode "Noon" turn	YS/ON ON mode: $ \beta  < 4^{\circ}, \\ \varphi < 5^{\circ}, \\ lasting 8 to \\ 15 d.$	YS/ON/CYS CYS: $ \beta  < 3^{\circ}$ , Sun azimuth $ \alpha  < 10^{\circ}$ , lasting 40 min	YS/CYS $ \beta  < 3.6^{\circ} - 4.9^{\circ}$ , rotate with maximum hardware yaw rate	YS/CYS $ \beta  < 2.4^{\circ}$ , rotate with constant hardware yaw rate of 0.20°/s, lasting about 15 min	YS/CYS Rotate with constant hardware yaw rate of about 0·11°/s, lasting about 27 min	YS/CYS $ \beta  < 2^{\circ}$ , rotate with maximum hardware yaw rate, lasting about 12 min	YS/CYS Same as BDS-3 except with the function of estimated yaw angle	$\begin{array}{l} \mathrm{YS/ON} \\  \beta  < 20^{\circ}, \mathrm{ON} \\ \mathrm{mode} \end{array}$
"Midnight" turn	"Noon" turn and "Midnight" turn do not exist.	Same as "noon"	Rotate with maximum hardware yaw rate, lasting 90 min including the "midnight" manoeuvre and recovery after shadow	Same as "noon"	$ \beta  < 8^\circ$ , rotate with constant hardware yaw rate of about $0.06^\circ/s$ , lasting about 54 min	Rotation at the full rate until the nominal attitude is resumed, lasting about 54 min		
Post-shadow recovery	-	-	Yes. Yaw angle possibly inverse after exiting a shadow	-	-	_	-	_
Research	Tang et al. (2016) and Guo (2014)	None	GYM94/GYM95; Bar-Sever (1995, 1996)	Bar-Sever and Kuang (2004); Kouba (2009)	GYM95; Dilssner et al. (2011a)	Dilssner et al. (2011b)	Montenbruck (2012) and Steigenberger and Montenbruck (2016)	Steigenberger et al. (2012)

Table 1	Attitude	mode for	GNSS	satellites
raule r	. Aunuuc	moue for	OINDD	satemites.



Figure 4. SLR residual for the GPS PRN G06 satellite in the deep Earth eclipsing period.

endpoint to assess in the orbit validation approach (Montenbruck et al., 2013; Urschl et al., 2007).

GPS satellite PRN G06 is a Block IIA satellite. Orbit accuracy for GPS satellite PRN G06 during the Earth eclipsing period was analysed. In this paper, the POD experiment for 32 GPS satellites was completed by using 20 International GNSS Service (IGS) monitoring stations distributed evenly throughout the world and applying the five-parameter ECOM SRP model. The G06 satellite was in the deep Earth eclipsing period from 30 December 2012 to 11 January 2013, and the satellite attitude control mode was CYS. Nominal YS law is adopted to model the yaw attitude of G06. Data in the post-shadow yaw manoeuvre is not adopted in orbit determination according to the research of Bar-Sever (1996). The global SLR residuals are shown in Figure 4; the grey shaded areas indicate time in the deep Earth eclipsing period. The SLR residual RMS values in no eclipse seasons and eclipse seasons were 4.96 cm and 11.56 cm, respectively. Thus, the orbit accuracy in terms of the radial component for GPS G06 in the deep Earth eclipsing period was 6.6 cm lower than that in the no eclipse seasons. The experiment did not use all IGS stations, and while the orbit accuracy in this experiment was lower than that of IGS orbit products, it was enough to illustrate the difference of orbit accuracy between the deep Earth eclipsing period and no eclipsing period. This problem exists for IGS precise orbit products. Figure 5 shows global SLR residuals for GPS PRN G06 obtained by IGS precise orbit products from the years 2010–2014. Notably, the orbit accuracy decreases by about 0.3 m in the Earth eclipsing period.

5. EXPERIMENT AND DISCUSSION FOR BEIDOU SATELLITES IN THE EARTH ECLIPSING PERIOD. The MPOD method is an orbit determination strategy using L-band code and phase measurements for GEO/IGSO/MEOs collected at regional BDS monitoring stations (Zhou et al., 2013) which was similar to the orbit determination strategy used by IGS for GPS. Seven monitoring stations including Beijing station, a station in Hainan, two stations in Xinjiang, a station in Sichuan, a station in Heilongjiang and a station in Guangdong were used and these are shown in Figure 6. Xinjiang1, Xinjiang2,



Figure 5. SLR residual for the GPS PRN G06 satellite from years 2010–2014 obtained from IGS precise orbit products.



Figure 6. Distribution of BDS regional monitoring stations.

Heilongj, Gudong in Figure 6 respectively present two stations in Xinjiang, a station in Heilongjiang and a station in Guangdong

Clock offset parameters of all satellites/receivers for each epoch and orbit parameter (initial orbital elements, SRP parameters, and empirical acceleration parameters), as well as site-dependent atmospheric zenith delay parameters and phase ambiguity, were estimated simultaneously. The perturbation modelled forces in the MPOD are shown in Table 2.

The POD for the new generation Beidou satellites in YS and CYS mode is based on the MPOD method. Specifically, the POD for BDS-2 satellites in ON mode builds on the new MPOD method supported by time synchronisation (Tang et al., 2016), and in this method,

Perturbation	Model/parameter
N body gravitation	Solar and planetary perturbation (DE403)
SRP	EIGEN-GRACE02S $10 \times 10$ ECOM 9, ECOM 5, ECOM 3
Solid Earth tide	IERS-Conventions 1996

Table 2. Dynamic model information.

high-precision satellite clock offsets were directly measured, instead of estimated, with a two-way time transfer between the satellites and the ground master station of the BDS. Those satellite clock offsets were then fixed to reduce the statistical correlations between other estimated parameters; consequently, the accuracy of the orbit determination was less susceptible to data quality issues than that from previous approaches. Additionally, one further constant acceleration in the along-track direction was added to the CODE SRP model to improve the POD accuracy for IGSO/MEOs in ON mode, according to the work of Guo (2014).

The evaluation method consisted of four steps, namely, analysis of the orbit internal consistency, calculation of the UERE, global SLR data fitting, RMS determinations and positioning performance analysis. The arc of the POD was 3 d. An orbit determination was made in a one-hour sliding window over a 72-hour session. Figure 7 shows the strategy of the orbit internal consistency with one-hour sliding windows; there are 24 POD solutions in each day, if the experiment lasts n days, there will be  $24 \times n$  POD solutions altogether. The internal consistency of satellite orbits can be evaluated by a two-day orbit fit through two consecutive one-day orbits. The red line represents the overlapping arc in Figure 7.

The orbit errors in the radial, along-track, and normal directions are obtained by the differences of overlapping orbits. The URE and Three-Dimensional (3D) position errors are then estimated, which serve as quality indicators (Steigenberger et al., 2015). Equations (3) are  $URE_i$  for different Beidou satellites in an i-hour experiment and Equations (4) are the RMS of URE and 3D position errors in n-day experiments, which is the final result of orbit internal consistency.

$$\begin{cases} GEO/IGSO : URE_{i} = \sqrt{1.0 \times \Delta R_{i}^{2} + (0.09 \times \Delta T_{i})^{2} + (0.09 \times \Delta N_{i})^{2}} \\ MEO : URE_{i} = \sqrt{(0.99 \times \Delta R_{i})^{2} + (0.14 \times \Delta T_{i})^{2} + (0.14 \times \Delta N_{i})^{2}} \\ URE_{RMS} = \sqrt{\sum_{i=1}^{24^{*}n} URE_{i}^{2}/24^{*}n} \\ POS_{RMS} = \sqrt{\sum_{i=1}^{24^{*}n} POS_{i}^{2}/24^{*}n} \end{cases}$$
(3)

where  $\Delta R_i$ ,  $\Delta T_i$ ,  $\Delta N_i$ ,  $URE_i$  are respectively the orbit errors in the radial, along-track, normal directions and URE in an i-hour experiment.

The UERE is an important index parameter for evaluating the service capability of a navigation system, as it summarises the total errors of the space segment (satellite orbits and clock offsets), the propagation segment (ionospheric and tropospheric delay) and the



Figure 7. Strategy of POD with one-hour sliding window.

Satellites	C31 (IGSO)	C33 (MEO)	C34 (MEO)
Start time of CYS	2016-2-12, 12:02:57	2015.12.18, 00:15:00	2015-12-18, 10:19:00
End time of CYS	2016-2-23, 01:59:57	2015.12.25, 06:14:00	2015.12.25, 16:26:00
Lasting time	10 d, 14 h	7 d, 6 h	7 d, 6·2 h
Satellites	C08 (IGSO)	C11 (MEO)	C12 (MEO)
Start time of ON	2015-12-21, 20:26:00	2015-12-16, 20:17:00	2015.12.16, 14:07:00
End time of ON	2015.12.31, 00:48:00	2015.12.27, 00:36:00	2015.12.26, 21:52:00
Lasting time	9 d, 4 h	10 d, 4 h	10 d, 7·8 h

Table 3. Times of different attitude control modes for Beidou satellites.

user segment (multipath and random errors) (Li et al., 2015). When the precision of every error source except for that of the orbits is acceptable, UERE can be adopted to evaluate the precision of the orbits. For a receiver with known coordinates and a clock synchronous with BDT, the UERE is as follows:

$$UERE = \rho - (R(t_k - \delta t_r - \tau, t_k - \delta t_r) + C\delta t_r - C\delta t_s + \tau_r + \tau_s + \Delta D_{trop} + \Delta D_{iono} + \Delta D_{rel} + \Delta D_{ant}^r + \Delta D_{ant}^s + \Delta D_{tide}$$
(5)

where  $\rho$  is the pseudo-range measurement; *R* is the geometric range between the satellite and receiver;  $\delta t_r$  is the receiver clock offset (which is zero in this case);  $\delta t_s$  is the satellite clock offset in the navigation message;  $\tau_r$  and  $\tau_s$  are the equipment time delay of the receiver and satellite, respectively and  $\Delta D_{trop}$ ,  $\Delta D_{iono}$ ,  $\Delta D_{rel}$ ,  $\Delta D_{ant}^r$ ,  $\Delta D_{ant}^s$ , and  $\Delta D_{tide}$ respectively represent the tropospheric delay, ionospheric delay, relativistic effects delay, antenna phase centre delay of the satellite and receiver and tidal effects delay (Guo et al., 2015).

The attitude control modes of the new generation Beidou satellite C31 in December 2015 and C33 and C34 in February 2016 were the CYS mode, and those of BDS-2 satellites C08, C11, and C12 in December 2015 were the ON mode. The POD experiments were conducted every hour so that 24 results were obtained every day. The experiment lasted for more than 60 d and included two CYS periods and one ON period. Table 3 shows the times of the different attitude control modes. In fact,  $\beta = 4^{\circ}$  and  $\varphi = 5^{\circ}$ , the orbit angle  $\mu$  is about 90° (Guo et al., 2017; Dai et al., 2015) at the moment of switch from YS to ON.

5.1. *Analysis of the orbit internal consistency.* The orbit accuracies for GNSS satellites declined to different extents in the deepest shadow, which for certain types of satellites



Figure 8. Overlapping arc accuracy based on three SRP models for new generation Beidou satellites.

were different for different SRP models. Use of an appropriate SRP model could make the orbit accuracy in the deep Earth eclipsing period match that in the no eclipse seasons. Therefore the experiments for new generation Beidou satellites in CYS mode were based on the ECOM 9, ECOM 5 and ECOM 3 models. The experiments lasted 30 d, so there are 720 ( $24 \times 30d$ ) POD solutions altogether. The RMS of 720 POD solutions was the final result. Figure 8 shows the orbit internal consistency for C31, C32, C33 and C34, in which the radial directions based on the ECOM 9, ECOM 5 and ECOM 3 models were 0.62 m, 0.21 m and 0.21 m, respectively, the URE results were 0.65 m, 0.26 m and 0.29 m, respectively, and the 3D positions were 2.09 m, 1.78 m and 1.87 m, respectively. The orbit internal consistency based on the ECOM 5 model was the best, and improvements of 0.03 m and 0.39 m were achieved compared with the ECOM 3 and ECOM 9 model results. The URE of the orbit internal consistency was 0.26 m in CYS mode.

5.2. *Analysis of the UERE*. The orbits and clock offsets were from broadcast messages of a receiver with known coordinates and clock times in Beijing. The SRP model results for ECOM 3 and UERE data for C31, C32, C33 and C34 in CYS and C08, C11 and C12 in ON mode are shown in Figure 9. The grey shaded areas indicate time periods with CYS or ON mode.

Figure 9 shows that (1) UERE values for C31, C33 and C34 in CYS mode matched those for the normal period of the YS mode and (2) UERE values for C08, C11 and C12 declined to about 4 m in the ON mode from about 2 m in the YS mode. Table 4 shows the UERE RMS results of the different attitude control modes.

The data in Table 4 show that the average UERE RMS for C31, C33 and C34 in CYS mode was 1.31 m, which only declined by 2 cm in comparison with those for the same satellites in YS mode. The UERE RMS values for C08, C11 and C12 in ON mode declined by 0.6 m, 0.51 m and 0.46 m, respectively, and the average value was 1.78 m. However, the orbit accuracy did not decline to 70 m during the ON mode based on the new results from the MPOD method supported by time synchronisation.

The orbit accuracies based on different SRP models in CYS mode were estimated and the results are shown in Table 5.



Figure 9. UERE for Beidou satellites based on different attitude control modes.

Satellite	YS	ON	Satellite	YS	CYS
C08	1.29	1.89	C31	1.38	1.39
C11	1.24	1.75	C33	1.29	1.32
C12	1.24	1.70	C34	1.20	1.23
Average	1.26	1.78	Average	1.29	1.31

Table 4. UERE RMS results of different attitude control modes for Beidou satellites (unit: m).

Table 5. Orbit accuracies based on different SRP models in CYS mode (unit: m).

Satellite	ECOM 9	ECOM 5	ECOM 3
C31	1.85	1.28	1.39
C33	1.79	1.23	1.32
C34	1.60	1.15	1.23
Average	1.75	1.22	1.31

The data in Table 5 show that the average UERE RMS values for C31, C33 and C34 based on the ECOM 9, ECOM 5 and ECOM 3 models were 1.75 m, 1.22 m and 1.31 m, respectively. The orbit accuracy based on the ECOM 5 model was the best, and the results showed respective improvements of 0.09 m and 0.53 m compared to the results with the ECOM 3 and ECOM 9 models. The same conclusion was reached with the data based on overlapping arc accuracy.

The ECOM model expresses the SRP acceleration in the (B, Y, D) frame, which is suitable for describing the SRP for a satellite. The pressure from the direct light of the Sun is a major component of SRP, and the D-axis is right along the satellite-Sun vector. However, the orbit accuracy of the ECOM 9 model was low and the correlation of SRP parameters was high because of the limited data for IGSO/MEOs. Correlation of ECOM 3 parameters was lower and the orbit stability was higher than those of ECOM 9. However, ECOM 3 parameters only contained constant terms in the D/Y/B directions, not periodic



Figure 10. SLR residuals for different attitude control modes.

terms; the orbit accuracy when applying ECOM 3 was lower than that when applying ECOM 5. The ECOM 5 model only contains five optimal parameters, and hence it is more suitable for IGSO/MEOs in CYS mode.

5.3. Orbit accuracy analysis based on global SLR data. Several satellites in the BDS have been employed in international SLR monitoring work. In particular, relatively large amounts of SLR tracking data have been collected for one Beidou GEO (C01), four Beidou IGSOs (C08, C10, C31 and C32), and four Beidou MEOs (C11, C33, C34 and C35) since 2012. The current global International Laser Ranging Service (ILRS) tracking network consists of around 40 ground stations. For BDS, the Australian Yarragadee and Chinese Changchun stations have been used to provide most of the observation data, and this data accounts for more than 90% of the global sum (Zhao et al., 2016).

In the process of SLR validation, the "theoretical" station-satellite distance is derived after the effects of solid tides, ocean tide loading, tectonic motion, station eccentricity, tropospheric delay, general relativity correction, and centre-of-mass correction have been eliminated from the SLR measurements. The corresponding L-band distance can be obtained from the L-band orbit by Chebyshev interpolation. The difference in the "theoretical" distance and L-band derived distance at the same time point is the SLR residual. Here, the cut-off elevation was set to 20° and the orbit accuracy according to the ECOM 5 model was evaluated by SLR measurements taken in December 2015 and February 2016. The SLR residuals for Beidou satellites are shown in Figure 10, and the corresponding statistics are shown in Table 6. The specific results for C33, C34 and C31 in CYS mode are shown in subgraphs 1 and 2 of Figure 10, and the specific results for C08 and C11 in YS mode and ON mode are shown in subgraphs 3 and 4 of Figure 10. The grey shaded areas indicate time periods with CYS or ON mode.

The main findings of this analysis were as follows.

(1) As indicated in Figure 5 and Table 6, the quantities of SLR tracking data were limited and the data were distributed unevenly. As the echo amplitude of SLR is inversely proportional to the fourth power of distance, and additionally, the meteorological conditions will affect the SLR observations greatly, tracking Beidou satellites is relatively difficult.

Satellite	Attitude control mode	SLR residual (cm)			
		Mean	Standard deviation	RMS	
C08	ON	85.38	77.55	115.87	
	YS	38.30	24.84	46.69	
C11	ON	9.23	29.59	31.04	
	YS	0.69	22.15	22.25	
C31	CYS	-14.25	27.81	31.13	
	YS	6.25	25.12	28.61	
C33	CYS	-2.24	19.42	20.21	
	YS	-6.03	15.62	17.83	
C34	CYS	-3.05	17.04	17.57	
	YS	-2.96	13.28	15.14	

Table 6. SLR residual statistics for different attitude control modes.

(2) The SLR residuals for C31, C33 and C34 in CYS mode matched those in YS mode. The SLR residual RMS values for C31, C33 and C34 were 0.31 m, 0.20 m and 0.17 m, respectively, and the standard deviation was better than 0.3 m. Orbit accuracy in the radial component declined by 2 to 3 cm compared with that in YS mode.

(3) The SLR residual RMS for C08, C11, and C12 in ON mode was 1.15 m, which declined by 0.69 m compared with that in YS mode. The new MPOD method supported by time synchronisation and optimised SPR model were effective in avoiding an orbit accuracy decline of a few hundred metres over several hours in ON mode.

Although several publications (Guo et al., 2014; Guo et al., 2016; Mao et al., 2014; Mao et al., 2015; Melachroinos et al., 2017; Montenbruck et al., 2017; Zhao et al., 2018) have discussed the question of why it is more difficult to model BDS satellites' dynamics in ON than in YS, the assumption is that it has a lot to do with the heat radiation panels at the -xside of the satellite bus. The solar panel axis is not perpendicular to the Sun direction with a small misalignment between 0° and 4°. The SRP model suitable for the YS mode does not do a good job of reflecting the characteristics of the SRP on the -X bus and coping with a small misalignment of the solar panels, thus the orbit accuracy declines in ON mode. Even if a priori analytical radiation models such as the ones from Tang et al. (2016) and Guo (2014) are employed, the orbit accuracy still declined to about 2 m. To avoid this problem, the new generation BDS satellites have all been upgraded with CYS capabilities. The -X bus is not illuminated by the Sun in CYS mode, similar to YS mode, and there are only about 40 minutes near "noon" and "midnight" where the CYS mode is required; at other times, a satellite will still adopt YS mode and the differences in SRP on the satellite will be small. Therefore, the differences in orbit accuracy will be small between YS mode and CYS mode.

5.4. Positioning performance analysis. To further validate the quality and consistency of orbit products in CYS mode, single point positioning accuracies with BDS pseudo-range data in YS, ON and CYS mode were analysed. The monitoring receiver was in Beijing, with data from 10 December 2015 to 28 January 2016 selected and processed, when the C08, C11 and C12 satellites were in ON mode and the C33 and C34 satellites are in CYS mode as shown in Table 3. In data processing, the ionosphere-free combination of B1I/B3I pseudo-range data recorded at 300 s intervals are used due to the 300 s clock products provided by BDS and orbit products in this paper. The static position



Figure 11. Positioning accuracy in Beijing by the first group of satellites. The grey shaded areas indicate time periods in ON mode of the C11 and C12 satellites, the light red shaded areas indicate time periods in ON mode for the C08 satellite.



Figure 12. Positioning accuracy in Beijing by the second group of satellites. The grey shaded areas indicate time periods in CYS mode for the C33 and C34 satellites.

coordinates and receiver clock offset are simultaneously estimated. The precise position coordinate is obtained by static Precise Point Positioning (PPP), which is used as the reference coordinate to evaluate the positioning accuracy. Two groups of satellites are used in the positioning analysis. The first group includes C01-C12 and C14, the difference between the second group and the first group is that C08,C11 and C12 in ON mode are substituted by the C31,C33 and C34 satellites in the second group. The positioning accuracies at the Beijing station from the two groups of satellites are shown in Figures 11 and 12 respectively. Table 7 lists the positioning accuracy in East, North and Up directions and overall position in YS, ON and CYS modes respectively.

Figures 11 and 12 and Table 7 show that the positioning accuracy is 4.29 m, 4.49 m and 4.30 m respectively in YS, ON and CYS modes, which degrades by 0.2 m in ON

Attitude control mode	North	East	Up	Pos
YS	1.61	1.17	3.80	4.29
ON	1.74	1.18	3.97	4.49
CYS	1.61	1.18	3.81	4.30

Table 7. Positioning accuracy in different attitude control modes (unit: m).

mode over that in YS mode, and by only 1 cm in CYS mode over that in YS mode. GNSS positioning accuracy is generally the product of UERE and Position Dilution Of Precision (PDOP) (CSNO, 2013; DoD, 2018). The larger the orbit error, the larger the positioning error. So, the improvement of orbit accuracy will bring an improvement of the positioning accuracy in CYS mode compared with that in ON mode. Therefore, the design of CYS mode has been successful, and the positioning and navigation performance of BDS should be improved.

6. CONCLUSION. Attitude control modes for navigation satellites were summarised and we then analysed the orbit accuracy in different attitude control modes. The evaluation method consisted of four steps, namely, analysis of the orbit internal consistency, UERE calculation, SLR data fitting, RMS determinations and positioning performance analysis; the experiment lasted for more than 60 d and included two CYS periods and one ON period. The main conclusions are as follows:

(1) The orbit accuracies for GPS, Galileo and QZSS satellites decline to different extents in the deep Earth eclipsing period. The orbit accuracy in the radial component for GPS satellite PRN G06 by global SLR data in a deep shadow is 11.56 cm, which declined by 6 cm compared with 4.96 cm in the no eclipse season. UERE and global SLR residuals for new generation Beidou satellites in deep shadow declined by 2 to 3 cm, which can be neglected compared to the 0.5 m of the current BDS orbit radial accuracy and 1.5 m of UERE RMS in the no eclipse season. Furthermore, positioning with BDS pseudo-range data are performed to validate the orbit accuracy, positioning accuracy degrades by only 1 cm in CYS mode over that in YS mode, which is just a small reduction in accuracy compared with the metre-level single point positioning accuracy with BDS pseudo-range data.

(2) BDS-2 satellites adopt ON mode in deep Earth eclipsing periods. After optimising the measurement model and SRP model, the orbit accuracy for BDS-2 satellites in ON mode still declined to 2 m, positioning accuracy degrades by 0.2 m over that in YS mode.

(3) New generation Beidou IGSO/MEO satellites adopt CYS mode in deep Earth eclipsing periods. The orbit accuracy for these satellites in CYS mode by the ECOM 5 model was the best. The orbit URE was 0.26 m, the UERE for 2-h orbital predictions was 1.22 m, and SLR data fitting RMS was better than 0.31 m.

(4) The analysis shows that new generation IGSO/MEO satellites can adopt CYS mode during the deep Earth eclipsing period and that the ECOM 5 model is suitable for these satellites in YS and CYS mode. In comparison, it is difficult to adopt the same SRP model to describe the SRP in ON mode for Beidou regional satellites. The orbit accuracy still declined to about 2 m by a proper analytical radiation model as for example the ones from Tang et al. (2016) and Guo (2014). The satellite's design, especially in regard to the thermal design, could be the main reason for this difficulty. The experiments with long-term Beidou

data show that CYS mode solves the declining navigation and positioning accuracy issue for deep Earth eclipsing periods. In the future, new generation IGSO/MEO satellites could provide high-precision and high-stability orbit products by using the CYS mode and the ECOM 5 mode, and this has important significance to MEOs, which are the most important component of the constellation in the Beidou global satellite navigation system.

## ACKNOWLEDGMENTS

The authors would like to thank the International Laser Ranging Service (ILRS) for providing the SLR data used in this study. This work was supported by the National Natural Science Foundation of China (Grant Nos. 41704037, 41574029, 41204022, and 61603397), the Youth Innovation Promotion Association CAS (Grant No. 2016242), and the foundation of the State Key Laboratory of Geodesy and Earth's Dynamics (SKLGED2017-3-3-E).

## REFERENCES

- Ahmed, E. (2018). Real-Time Precise Point Positioning Using Orbit and Clock Corrections as Quasi-Observations for Improved Detection of Faults. *The Journal of Navigation*, 5 February 119. https://doi.org/ 10.1017/S0373463317001023.
- Bar-Sever, Y.E. (1995). A new model for yaw attitude of Global Positioning System satellites. *TDA Progress Report*, 15 November, 37–46.
- Bar-Sever, Y.E. (1996). A new model for GPS yaw attitude. Journal of Geodesy, 70, 714–723.
- Bar-Sever, Y.E. and Kuang, D. (2004). New empirically derived solar radiation pressure model for Global Positioning System satellites. *IPN Progress Report* 42-159, 15 November, 1–11.
- Cao, F., Yang, X.H., Su, M.D., Li, Z.G., Chen, L., Li, W.C., Sun, B.Q., Kong, Y., Wei, P. and Feng, C.G. (2014). Evaluation of C-Band Precise Orbit Determination of Geostationary Earth Orbit Satellites based on the Chinese Area Positioning System. *The Journal of Navigation*, **67**, 343–351.
- Chen, J.P., Hu, X.G., Tang, C.P., Zhou, S.S., Guo, R., Pan, J.Y., Li, R. and Zhu, L.F. (2016). Orbit determination and time synchronization for new-generation Beidou satellites: Preliminary results. *SCIENTIA SINICA Physica*, *Mechanica & Astronomica*, 46, 119502, doi: 10.1360/SSPMA2016-00281 (in Chinese).
- CSNO (2013). Beidou Navigation Satellite System Signal in Space Interface Control Document Open Service Signal (Version 2.0). *China Satellite Navigation Office*. 26, December, 2013.
- Dai, X., Ge, M., Lou, Y., Shi, C., Wickert, J. and Schuh, H. (2015). Estimating the yaw-attitude of BDS IGSO and MEO satellites. *Journal of Geodesy*, 89, 1005–1018, doi: 10.1007/s00190-015-0829-x.
- Dilssner, F., Springer, T. and Enderle, W. (2011a). GPS IIF yaw attitude control during eclipse season. American Geophysical Union, Fall Meeting, San Francisco, CA, 9 December, 1–23.
- Dilssner, F., Springer, T., Gienger, G. and Dow, J. (2011b). The GLONASS-M satellite yaw-attitude model. Advances in Space Research, 47, 160–171, doi:10.1016/j.asr.2010.09.007.
- DoD. (2018). Global Positioning System Standard Positioning System Service Performances Standard. Department of Defense, USA.
- Fliegel, H.F., Gallini, T.E. and Swift, E.R. (1992). Global positioning system radiation force model for geodetic applications. *Journal of Geophysical Research*, 97(B1), 559–568.
- Guo, J. (2014). The impacts of attitude, solar radiation and function model on precise orbit determination for GNSS satellites. *GNSS Research Center Wuhan University*, **10**, 74–80 (in Chinese).
- Guo, J., Chen, G., Zhao, Q.L., Liu, J.N. and Liu, X. (2017). Comparison of solar radiation pressure models for BDS IGSO and MEO satellites with emphasis on improving orbit quality. *GPS Solutions*, 21(2), 511–522.
- Guo, J., Xu X.L., Zhao, Q.L. and Liu, J.N. (2016). Precise orbit determination for quad-constellation satellites at Wuhan University: strategy, result validation, and comparison. *Journal of Geodesy*, **90**, 143–159.
- Guo, R., Zhou, J.H., Hu, X.G., Liu, L., Tang, B., Li, X.J. and Wu, Sh. (2015). Precise orbit determination and rapid orbit recovery supported by time synchronization. *Advances in Space Research*, 3, 2889–2898, doi:10.1016/j.asr.2015.03.001.
- Hamad, Y., and Ahmed, E. (2007). Assessment of Several Interpolation Methods for Precise GPS Orbit. The Journal of Navigation, 60, 443–455.

- Hauschild, A., Steigenberger, P. and Rodrihuez-Solano, C. (2012). Signal orbit and attitude analysis of Japan's first QZSS satellite Michibiki. GPS Solutions, 16, 127–133.
- Kouba, J. (2009). A simplified yaw-attitude model for eclipsing GPS satellites. GPS Solutions, 13, 1–12.
- Li, X.J., Zhou, J.H. and Guo, R. (2014). High-precision orbit predication and error control techniques for COMPASS navigation satellite. *Chinese Science Bulletin*, 59(23), 2841–2849.
- Li, X.J., Zhou, J.H., Hu, X.G., Liu, L., Guo, R. and Zhou, S.S. (2015). Orbit determination and prediction for Beidou GEO satellites at the time of the spring/autumn equinox. *Science China Physics, Mechanics and Astronomy*, 58(8), 089501.
- Mao, Y, Song, X, Wang, W, Jia, X.L., and Wu, X.B. (2014). IGSO satellite orbit determining strategy analysis with the yaw-steering and orbit-normal attitude control mode switching. *Geomatics and Information Science* of Wuhan University, 39(11), 1352–1356 (In Chinese).
- Mao, Y., Song, X., Wang, W., Jia, X.L. and Wu, X.B. (2015). Beidou IGSO and MEO navigation satellites' yaw steering and orbit normal attitude control modes and solar radiation pressure difference analysis. *Science of Surveying and Mapping*, 40(8), 129–134 (In Chinese).
- Melachroinos, S., Tseng, T. and Papanikolaou, T. (2017) A new yaw attitude algorithm for BDS MEO and IGSOs, 2017 IGS poster.
- Montenbruck, O. (2012). ANTEX considerations for multi-GNSS work. *Antenna WG Meeting, IGS Workshop*, 25 July 2012.
- Montenbruck, O., Steigenberger, P. and Darugna, F. (2017). Semi-analytical solar radiation pressure modeling for QZS-1 orbit-normal and yaw-steering attitude. *Advances in Space Research*, 59, 2088–2100.
- Montenbruck, O., Steigenberger, P. and Kirchner, G. (2013). GNSS satellite orbit validation using satellite laser ranging. Proceedings of the 18th ILRS Workshop on Laser Ranging, Fujiyoshida, Japan.
- Springer, T.A., Beutler, G. and Rothacher, M. (1999). A new solar radiation pressure model for GPS. Advances in Space Research, 23(4), 673–676.
- Steigenberger, P. and Montenbruck, O. (2016). Galileo status: orbits, clocks, and positioning. *GPS Solutions*, **21**, 319–331, doi:10.1007/s10291-016-0566-5.
- Steigenberger, P. and Montenbruck, O. (2017). Precise orbit modeling of GNSS satellites. Report CSNC2017, Shanghai.
- Steigenberger, P., Hauschild, A. and Montenbruck, O. (2012). Orbit and clock determination of QZS-1 based on the CONGO Network. *Proceedings of the 2012 International Technical Meeting of the Institute of Navigation*, Newport Beach, CA.
- Steigenberger, P., Hugentobler, U., Hauschild, A. and Monteubruck, O. (2013). Orbit and clock analysis of Compass GEO and IGSO satellites. *Journal of Geodesy*, 87, 515–525.
- Steigenberger, P., Hugentobler, U., Loyer, S., Perosanz, F., Prange, L., Dach, R., Uhlemann, M., Gendt, G. and Montenbruck, O. (2015). Galileo orbit and clock quality of the IGS Multi-GNSS Experiment. *Advances in Space Research*, 55(1), 269–281, doi:10.1016/j.asr.2014.06.030.
- Tang, C.P., Hu, X.G., Zhou, S.S., Guo, R., He, F., Liu, L., Zhu, L.F., Li, X.J., Wu, Sh., Zhao, G., Yu, Y. and Cao, Y.L. (2016). Improvement of orbit determination accuracy for Beidou Navigation Satellite System with Two-way Satellite Time Frequency Transfer. *Advances in Space Research*, 58, 1390–1400, http://dx.doi.org/10.1016/j.asr.2016.06.007.
- Urschl, C., Beutler, G., Gurtner, W., Hugentobler, U. and Schaer, S. (2007). Contribution of SLR tracking data to GNSS orbit determination. *Advances in Space Research*, **39**, 1515–1523.
- Wang, H.H., Chen, Z.G., Zheng, J.J. and Chu, H.B. (2011). A New Algorithm for Onboard Autonomous Orbit Determination of Navigation Satellites. *The Journal of Navigation*, 64, 162–179.
- Wu, Z.Q., Song, S.L. and Zhou, W.L. (2015). Research progress of solar radiation pressure model for navigation satellite (in Chinese). Advances in Earth Science, 30(4), 495–504.
- Zhao, G., Zhou, S.S., Zhou, X.H. and Wu, B. (2016). Orbit accuracy analysis for BeiDou Regional Tracing Network. *China Satellite Navigation Conference 2016 Proceedings*, 5, 235–244.
- Zhao, Q.L., Wang, C., Guo, J., Wang, B. and Liu, J.N. (2018). Precise orbit and clock determination for BeiDou-3 experimental satellites with yaw attitude analysis *GPS Solutions* **22**, 4–8.
- Zhou, S.S., Hu, X.G. and Zhou, J.H. (2013). Accuracy analyses of precise orbit determination and timing for COMPASS/BDS-2 4GE0/5IGSO/4MEO constellation. *Lecture Notes in Electrical Engineering*, 245, 89–102.