Uniform-momentum zones in a turbulent pipe flow

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The characteristics and dynamics of the uniform-momentum zones (UMZ) and UMZ interfaces in a fully developed turbulent pipe flow are studied using direct numerical simulation at $Re_{\tau} = 500$. The multiple UMZs detected from the probability density functions of the instantaneous streamwise velocity following de Silva et al. (J. Fluid Mech., vol. 786, 2016, pp. 309-331) showed similarities to both turbulent channel and boundary layer flows (TBL): the hierarchical structural distribution of thinner UMZs with thinner interfaces nearer the wall, accompanied with sharper and larger jumps in the streamwise velocity at the UMZ interface. The conditional average results indicate that channel and pipe are very similar quantitatively whereas pipe and TBL display significant discrepancies. The innermost UMZs in pipe flow exhibit different behaviours to the other UMZs in pipes. The contortion of the UMZ interface representing the meandering of coherent motions with high- and low-momentum streaks is examined three-dimensionally. The meandering of UMZ in both two and three dimensions intensifies away from the wall and is always wavier in the azimuthal direction than the streamwise direction. The UMZs in the near-wall region capture the small-scale velocity fluctuation of the near-wall cycle and show asymmetric modulation of Q2 ejections over Q4 sweeps. The asymmetric modulation of ejections over sweeps decreases from the wall towards the pipe centre and the opposite trend of elevated O4 sweeps is observed for the innermost UMZs. Near the wall, the ejection regions are very spiky compared to the flat sweep regions whereas, in the pipe centre, the large-scale ejections are relatively flat and the sweep regions are spikier.

Key words: pipe flow boundary layer, turbulent boundary layers

1. Introduction

1.1. The existence and detection of UMZ

The uniform-momentum zone (UMZ) is an instantaneous phenomenon that has been found in the presence of wall-bounded flows. The existence of the UMZ was first found in the experiment of a turbulent boundary layer (TBL) by Meinhart & Adrian (1995) who observed large regions of relatively uniform streamwise velocities.

This enables the detection of the UMZ from the probability density functions (PDF) of the instantaneous streamwise velocity. Distinct peaks on the PDFs represent large regions of the flow developing downstream at relatively constant velocities, namely the zone modal velocities. Kwon *et al.* (2014) and Yang, Hwang & Sung (2016) studied the innermost UMZ in a turbulent channel flow, called the quiescent core region. The UMZ/core boundary was defined by a fixed threshold velocity at 95 % of the centreline velocity ($u_{\kappa}/U_{CL} = 0.95$), suggested by the PDF of the modal velocities over time. Kwon *et al.* (2014) reported that the quiescent core of the channel is very large, and can occupy approximately $\frac{3}{4}$ of the channel height on average. The channel core exhibited significant thinning, thickening and meandering behaviour; it occasionally extended very close to the channel walls and left the centreline outside the core (≈ 7 % of the time overall). A recent study by Fan *et al.* (2019) proposed a new method to identify the internal shear layers bounding the UMZs. The method does not require user-defined parameters as for the PDF approach to UMZ identification and is insensitive to the streamwise domain length.

The UMZ interface demarcates the neighbouring UMZs with strong shear originated from concentrated patches of spanwise vortices observed by Meinhart & Adrian (1995) and Adrian, Meinhart & Tompkins (2000). These organised vortical structures at the UMZ interface were responsible for ejections (Q2 events) and sweeps (Q4 events) around the interface (Tomkins & Adrian 2003; Ganapathisubramani, Longmire & Marusic 2003). The retrograde vortices frequently appeared at the backbone of the prograde vortices, matched the experimental observation of Adrian et al. (2000) and Yang, Meng & Sheng (2001). In Yang et al. (2016), the population of prograde and retrograde spanwise vortices showed a local maximum and minimum in the vicinity of the interface respectively. Across the UMZ interface, an abrupt jump in the streamwise velocity accompanied by local maximum spanwise vorticity and decay of turbulent intensity was observed in the channel (Kwon et al. 2014; Yang et al. 2016), pipe (Kwon 2016; Yang, Hwang & Sung 2017) and TBL (de Silva et al. 2017).

de Silva, Hutchins & Marusic (2016) investigated multiple UMZs in TBL and found the number of UMZs increasing log-linearly with the Reynolds number. The thickness of the UMZs was found to be increasing as a function of the distance from the wall, forming a hierarchical distribution of UMZs in the boundary layer. The hierarchical structural arrangement matched the scaling model by Perry & Chong (1982) described in Marusic & Monty (2019). de Silva et al. (2017) found the velocity jump at the interfaces as a function of the wall-normal distance, being larger nearer the wall. The thickness of the UMZ interface themselves was also a function of the distance from the wall, being thicker further away from the wall. The hierarchical scaling of the UMZs with thinner zones and larger velocity jumps across the sharpened interface nearer the wall was used by Bautista et al. (2019) for their UMZ-vortical fissure model in TBL. Turbulence statistics were largely reproduced using a discrete step-like initial velocity profile modelled from the UMZ hierarchical distribution. Laskari et al. (2018) investigated the evolution of the UMZ and showed that when the number of UMZ increases, all existing UMZs become thinner and move away from the wall with a higher modal velocity to compensate for the new zones.

The UMZ interface folds intensively with bulges and valleys similar to the large-scale engulfment of the turbulent/non-turbulent interface (TNTI) (Kwon *et al.* 2014). The contortion of the UMZ interfaces, which are iso-surfaces of the streamwise velocity, is a manifestation of the large-/very-large-scale motions (LSM/VLSM) in wall turbulence (Saxton-Fox & McKeon 2017; Yang *et al.* 2017). Saxton-Fox & McKeon (2017) reconstructed the velocity field of TBL using an LSM model and

recreated the classical characteristics of UMZs such as the large-scale bulges on the UMZ interface. Yang et al. (2016) measured the two-dimensional (2-D) contortion of the UMZ interface by comparing the length of the UMZ interface per unit length in the streamwise and spanwise direction of the channel. The UMZ interface was found, on average, to be longer in the spanwise direction, so that the interfaces are wavier and the LSMs meander with higher frequencies in the spanwise direction than in the streamwise direction. de Silva et al. (2017) found the streamwise length of the UMZ interfaces to be longer when departing from the wall, and they exhibited a power-law behaviour with fractal scaling at a constant exponent for all interfaces within the TBL. Recent statistical results by Kevin & Hutchins (2019) also reported that the meandering of the LSM/contortion of the UMZ interface intensifies with increasing distance from the wall. Multiple UMZs are demarcated by UMZ interfaces with similar large-scale engulfment from meandering/contortion and small-scale entrainment by local patches of vortices. The interface resembles the TNTI, forming a multi-layered structural arrangement with hierarchical scaling in wall turbulence (Perry & Chong 1982; Bautista et al. 2019; Marusic & Monty 2019).

To the authors' best of knowledge, the characteristics of multiple UMZs and their interfaces have been studied only in TBL (de Silva et al. 2016, 2017; Laskari et al. 2018). The first part of this study investigates many of these characteristics in the pipe flow via conditional averaging. The results are extensively compared with the multiple UMZs in TBL and the single quiescent core region in a channel to deduce differences and similarities in wall turbulence. The second part of this study investigates the UMZ interface in three dimensions. The attachment between UMZ interfaces and vortical structures are observed three-dimensionally and in the azimuthal direction of the pipe. The dynamical attachment is shown for the first time for its role in the contortion of UMZ interface. The 3-D contortion/meandering of the UMZ/LSM and its behaviour with wall distance is measured statistically. The bulges and valleys on the UMZ interface are investigated with the Q4 sweep and Q2 ejection events. The reported footprint of the LSM away from the wall (Rao, Narasimha & Narayanan 1971; Metzger & Klewicki 2001; Jiménez, del Álamo & Flores 2004) in the near-wall cycle is investigated in the UMZ aspect. Statistics are computed to show the modulation of the near-wall bursting events by the LSM in the centre region of the pipe (Hutchins & Marusic 2007a,b; Marusic & Hutchins 2008: Chung & McKeon 2010: McKeon & Sharma 2010: Baars, Hutchins & Marusic 2017). The asymmetry of the large-scale modulation (Agostini & Leschziner 2014, 2016) is measured along the wall-normal direction using the 3-D UMZ interfaces.

2. Numerical simulation

This study investigates the direct numerical simulation (DNS) data of a fully developed turbulent pipe flow at a friction Reynolds number of $Re_{\tau}\approx 500$. The DNS data are generated by a massively paralleled MPI (Message Passing Interface) code, Nek5000 (Fischer, Lottes & Kerkemeier 2008) using the spectral element method (SEM). The incompressible Navier–Stokes equations are solved in Cartesian coordinates to avoid the singularity issue associated with the cylindrical coordinates at the pipe centreline (Jung & Chung 2012; Wang et al. 2018). A semi-implicit time scheme solves the viscous terms implicitly using a third-order backward differentiation (BDF3) and the nonlinear terms by a third-order extrapolation (EXT3). The periodic boundary condition was applied in the streamwise direction and the no-slip condition at the pipe wall.

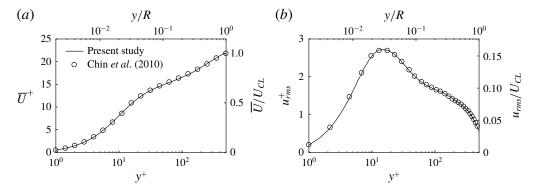


FIGURE 1. (a) Mean streamwise velocity U and (b) root-mean-square velocity fluctuation u of the present study and that by Chin *et al.* (2010), both for turbulent pipe flow at $Re_{\tau} = 500$.

In this study, the streamwise, radial and azimuthal directions of the pipe are denoted by x, r and θ respectively, with wall-normal distance y = R - r (R is the pipe radius). The velocity components U, V and W are in the streamwise, vertical and horizontal directions of the Cartesian coordinates. The wall-normal velocity in the radial direction is denoted as V_r . The computational domain of the 30R-long pipe has 2652 quadrilateral elements in the cross-stream planes and 314 in the streamwise direction. Each element with Gauss-Lobatto-Legendre nodes has a Lagrange polynomial order of N=7, resulting in a total of 4.26×10^8 grid points (El Khoury et al. 2013). On the orthogonal streamwise planes, the grid resolution in the radial direction varies between $\Delta y^+ = 0.16$ and $\Delta y^+ = 4.24$. The resolution in the streamwise direction varies between $\Delta x^+ = 3.06$ and $\Delta x^+ = 9.99$. A grid independence test for the pipe flow was reported in Wang et al. (2018). The mean streamwise velocity U and the root-mean-square velocity of streamwise fluctuation u_{rms} is shown in figure 1. The collapse of the profiles shows an excellent agreement between the present data and the previous DNS data using SEM by Chin et al. (2010) at the same Reynolds number for a pipe.

3. Results and discussion

3.1. The detection and grouping of UMZ

3.1.1. Detecting instantaneous UMZs

The detection of instantaneous UMZs follows the methodology used by Adrian *et al.* (2000), de Silva *et al.* (2016, 2017) and Laskari *et al.* (2018). The instantaneous UMZs are detected from the peaks on the PDFs of the instantaneous streamwise velocity U. These peaks correspond to large regions travelling at relatively uniform velocity, namely the zone modal velocity u_m . Each instantaneous PDF is computed using all the data points in a 3-D snapshot with a streamwise window size of 0.2R throughout the 30R-long pipe and for all the available snapshots over time. The PDFs have a uniform bin size of $1\%U/U_{CL}$ with 110 bins covering $U/U_{CL} \in [0, 1.1]$. Figure 2(a) shows an example of the instantaneous PDF of U from a 3-D snapshot. Three distinct peaks at three zone modal velocities u_m are detected from this snapshot and are marked by ' ∇ '. The peak detection scheme used here is similar to de Silva *et al.* (2016) and Laskari *et al.* (2018). For each instantaneous PDF of U, the local

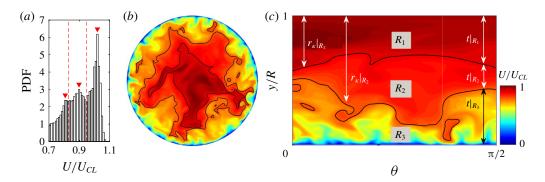


FIGURE 2. An example of the detection of instantaneous UMZs. (a) The PDF of the instantaneous streamwise velocity U computed from the 3-D domain of a snapshot with streamwise window size of 0.2R. (b) Corresponding contour of U on a cross-stream plane from the same snapshot as in (a). (c) The definition of zone rank R_i , zone thickness $t|_{R_i}$ and zone interface radius $r_{\kappa}|_{R_i}$ on the same contour as in (b), unwrapped for a quarter of the azimuthal span.

maxima are filtered by three constraints, F_d , F_h and F_s . Here, F_d is the minimum distance between each recognised peak, F_h is the minimum height of the peak on the PDF and F_p is the prominence of the peak compared to the five neighbouring bins on each side of the peak. Peaks are only recognised as u_m for $F_d > 3\%U_{CL}$ (3 bins), $F_h > 0.5$ and $F_p > 25\%$ which requires the recognised peaks to be 25% higher than the average bin height of its neighbouring $10\%U/U_{CL}$. The threshold velocity of the UMZ interface u_κ between each zone is defined at the minimum bin between each two neighbouring peaks of u_m . In figure 2(a), two u_κ are marked by the dashed lines between each of the two peaks. Figure 2(b) shows the contour of U on a cross-stream plane within the snapshot. The iso-contours of three threshold velocities u_κ separate the flow into three regions, each travelling with small velocity dispersion. The UMZ interface closest to the wall in figure 2(b) corresponds to the lowest $u_\kappa/U_{CL} \approx 0.8$ in figure 2(a).

The number of UMZ detected on each PDF, N_{UMZ} depends greatly on the constraints of the peak detection scheme. More strict detection with higher constraints can reduce N_{UMZ} significantly. Laskari et al. (2018) adjusted their peak detection constraints for a targeted average $N_{UMZ} \approx 4.5$, suggested by the Reynolds number dependency of N_{UMZ} in de Silva et al. (2016) for TBL. In the present study of pipe flow at $Re_{\tau} = 500$, a target $N_{UMZ} \approx 2.5$ estimated from the TBL results is found to be too low. Many non-trivial peaks are seen to be neglected. This could be because, for a pipe and TBL at a similar Reynolds number, there are potentially more UMZs in the pipe, being thinner on average and more refined due to the full circumferential wall confinement. Therefore, in the absence of knowledge on the Reynolds number dependency of N_{UMZ} in a pipe, no targeted N_{UMZ} is pre-defined. The constraints are chosen only for a robust combination that can fairly preserve all distinctive peaks on the PDFs. Figure 3 shows the PDF of N_{UMZ} over all available snapshots. The PDF peaks at $N_{UMZ} = 5$ and agrees with the normal distribution found by de Silva et al. (2016) and Laskari et al. (2018), indicating that a sufficient number of instantaneous UMZs have been obtained for statistical analysis and UMZ grouping.

Instead of peak detection on the histogram of U, Fan $et\ al.$ (2019) used the kernel density estimation (KDE) without the requirement of multiple user-defined constraints

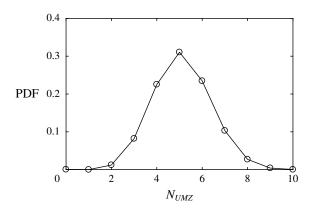


FIGURE 3. PDF of N_{UMZ} , the number of UMZs from detected peaks on each instantaneous PDF of U using all vectors in the 3-D snapshot with a streamwise window size of 0.2R.

but a single KDE bandwidth. In the Appendix, part of the statistical characteristics of the UMZs shown in the later sections are reproduced from using the KDE approach for UMZ detection.

3.1.2. Grouping of UMZs

Each instantaneous UMZ has an individual zone modal velocity u_m and threshold velocity u_{κ} at the interface separating it from its adjacent zones. These UMZs detected from all snapshots are classified into a few groups based on their zone modal velocities u_m . Two grouping methods are used in this study for different purposes. The first grouping method is by the magnitude of u_m . This is similar to the grouping used in de Silva et al. (2016, 2017) in which UMZs were grouped based on the zone momentum deficit $u_m - U_\infty$ (U_∞ is the TBL free-stream velocity). In the present study, six u_m groups denoted as M_i with uniform increments of u_m are defined by their u_m range, as listed in table 1 (left). UMZs in group M_6 are the closest to the wall with the lowest u_m within $M_{1:6}$ whereas group M_1 with $u_m/U_{CL} \in [1.0, 1.1)$ is the innermost UMZ of the pipe, travelling above the centreline velocity. Figure 4(a)shows the PDFs of the N_{UMZ} for each u_m group of $M_{1:6}$. The distribution of N_{UMZ} in each u_m group (bars) follows the time-averaged PDF of U (dashed line). Group M_2 includes the highest number of UMZ among $M_{1:6}$ and M_6 has the lowest UMZ count. The count in group M_1 of UMZs travelling beyond the centreline velocity is relatively low, as expected. The overlaid PDF of UMZ count in the TBL by de Silva et al. (2016) are shown by 'O'. The PDF distribution is very similar to the time-average PDF of U in a pipe whereas the peak of the PDF of TBL is at a lower $u_m/U_\infty = 0.9$ than a pipe at $U/U_{CL} = 0.98$.

The second grouping method follows Laskari *et al.* (2018) in which the UMZs are grouped based on the ranking of zone modal velocity u_m in each snapshot. For example, in figure 2(a), the zone with the highest u_m , which is the inner most UMZ in figure 2(b), is ranked as R_1 and the zone with the lowest u_m is ranked the last (R_3) . Figure 2(c) unwraps the first quadrant of the contour in figure 2(b). As illustrated, the three UMZs detected in this snapshot $(N_{UMZ} = 3)$ are ranked from the centre to the wall as R_1 to R_3 with descending u_m . If a snapshot has $N_{UMZ} = 6$, then the six UMZs will be ranked from R_1 to R_6 based on their ranking of u_m . Because of the nature of the wall-bounded flow, the R_1 zone will always be the innermost zone with the highest u_m in the region (see also Laskari *et al.* (2018)). Figure 4(b) shows the PDFs

Group M_i	u_m/U_{CL}	Symbol	Colour	Rank R_i	Symbol	Colour
1	[1.0, 1.1)	0	Blue	1	Δ	Blue
2	[0.9, 1.0)	Δ	Red	2	0	Green
3	[0.8, 0.9)		Green	3	∇	Cyan
4	[0.7, 0.8)	×	Magenta	4		Red
5	[0.6, 0.7)	\Diamond	Cyan	5	\triangleright	Yellow
6	[0.5, 0.6)	\triangleleft	Yellow	6	\triangleleft	Magenta
				7	\Diamond	Black

TABLE 1. (Left) The range of modal velocity u_m , symbols and colours for UMZ groups M_i grouped by u_m . (Right) The symbols and colours used for UMZ groups R_i grouped by zone rank on u_m .

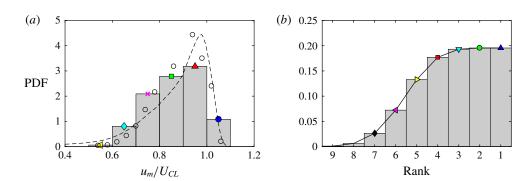


FIGURE 4. (a) PDF of N_{UMZ} , the number of UMZs in each u_m group M_i based on zone modal velocity u_m (bar); the time-average PDF of the streamwise velocity U: -----; and the PDF of u_m in turbulent boundary layer by de Silva *et al.* (2016) at $Re_{\tau} = 8000$: O. (b) PDF of N_{UMZ} in each ranking group R_i based on zone rank of u_m for $R_{1:9}$.

of N_{UMZ} in each ranking group of $R_{1:9}$. The ranks are plotted in reverse order since the lowest rank (R_9) includes the UMZs travelling at the lowest u_m in each snapshot. The count of UMZ continuously decrease from R_1 to R_9 .

In the following part of this study, UMZ groups based on the range of u_m are called u_m groups, denoted as M_i ; and UMZ groups based on the ranking of zone u_m are called the ranking groups, denoted as R_i . The symbols and colours for each group in the two grouping methods are consistent throughout this study and are listed in table 1.

3.2. Evolution of UMZs

The evolution of the UMZs is studied by the statistical distribution of the zone modal velocities u_m , zone thicknesses t and zone wall-normal locations $y_{\kappa} = 1 - r_{\kappa}$ (r_{κ} is the zone radial location from the centreline as shown in figure 2c) as functions of N_{UMZ} . In Laskari et al. (2018), both of the two grouping methods based on the magnitude of u_m and the ranking of u_m are used to compute the distribution of u_m , y_{κ} and t against N_{UMZ} . The results from using the two grouping methods agree with each other and the distributions showed clearer trends with the ranking groups, hence only results from the ranking groups of UMZ R_i are used to show the evolution of UMZs for a pipe in this section. Figure 5 shows the spread and the mean of u_m , y_{κ} and t for UMZs in

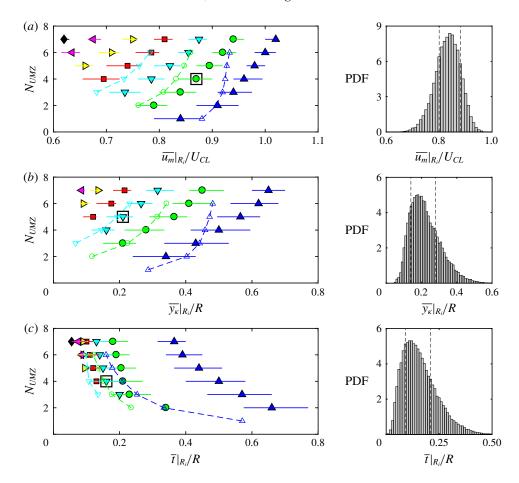


FIGURE 5. Conditional averages of UMZ groups R_i based on the zone rank of zone modal velocity u_m for different N_{UMZ} : (a) zone modal velocity, $u_m|_{R_i}$, (b) zone distance from wall, $1 - r_{\kappa}|_{R_i}$ and (c) zone thickness, $t|_{R_i}$. The bars are the span of the centred 50% of the data and the filled marker on each bar indicates the mean. The hollowed markers with dashed lines are results from a turbulent boundary layer by Laskari *et al.* (2018). The same symbols represent the same ranks in a pipe (filled) and TBL (hollowed). (Symbols and colours as in table 1 (left).) The PDFs on the right-hand side are shown for one rank group at a certain N_{UMZ} with its marker boxed in the left-hand side figures. The two dashed lines on the PDFs indicate the centred 50% (25% to 75%) of the data.

groups R_1 to R_7 against N_{UMZ} . The spread is defined as the centred 50% (25%–75%) of the data as shown by the right-hand side PDFs. The vertical dashed lines on the PDFs mark the centred 50% of the data. The PDFs are shown for one ranking group at a particular N_{UMZ} which has its symbol highlighted in a box on the left-hand side of the figures.

In figure 5(a), when $N_{UMZ} = 1$, only group R_1 (marked by ' \triangle ', blue) for the innermost UMZs at the highest u_m in each snapshot is present. As N_{UMZ} increases, more zones in lower ranking groups become available. The trend of u_m with increasing N_{UMZ} is very clear and similar for all existing zones: all the existing zones have increased u_m while the newly joined zone in a lower rank (R_i with $i = N_{UMZ}$) starts

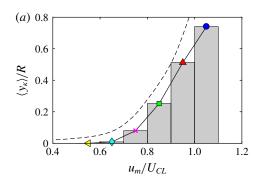
at the lowest u_m at that N_{UMZ} . As N_{UMZ} continues to increase, the recently joined zones exhibit similar increase in u_m and the UMZs in the newest/lowest rank start at an even lower u_m . This forms a triangular-shape distribution of u_m along N_{UMZ} in figure 5(a). Figure 5(b) shows the average wall-normal location of the UMZs in group $R_{1:6}$, y_{κ} . The wall-normal location of each UMZ is defined as the distance between the wall and the lower UMZ interface closer to the wall which bounds the UMZ and its adjacent zone with lower u_m (see figure 2c). The distribution and the trend of y_{κ} is very similar to u_m along N_{UMZ} . All the existing zones move towards the centre of the pipe when the new zones join near the wall with lower y_k . This matches the observation by Laskari et al. (2018) that when more zones are in presence, the zones are, on average, pushed to the centre to accommodate more UMZs in the region. This would result in all UMZs being thinner on average at higher N_{UMZ} which is shown in figure 5(c). When N_{UMZ} increases, the zone modal velocity u_m and wall distance y_k of the UMZs in each rank all increase with zone thickness t decreasing monotonically. This suggests that the UMZs are thinner and travelling faster when there are more UMZs in the flow region.

The TBL results from Laskari et al. (2018) for the first three ranking groups $R_{1:3}$ are overlaid on the left-hand side distributions in figure 5. The same symbol is used for the same ranking group in the pipe (colour filled) and TBL (hollowed with a dashed line along each rank). The trend of monotonically increasing u_m and y_k and decreasing t is very similar between pipe and TBL, especially for ranks R_2 and lower. However, the R_1 zones show marked differences between pipe (' \triangle ', blue) and TBL (' \triangle ', blue) in all three quantities. In figure 5(a), the modal velocity of the R_1 UMZs in TBL increases with N_{UMZ} more slowly than the other ranks whereas the R_1 zone in the pipe is similar to all the other ranks and $R_{2,3}$ of the TBL with a continuous increase in u_m all the way along N_{UMZ} . At $N_{UMZ} = 1$, the R_1 zones in TBL start at a u_m 5% higher than a pipe whereas at $N_{UMZ} = 6$, the R_1 zones in a pipe with faster increase than the TBL have u_m 14% higher than the TBL. In a TBL, the maximum u_m reached by R_1 is approximately $0.93U_{\infty}$ whereas in a pipe, the R_1 zones can reach beyond the pipe centreline velocity at $u_m/U_{CL} \approx 1.02$. A similar slower increase in wall distance y_{κ} of R_1 in a TBL compared to its other two ranks $R_{2,3}$ and all the ranks in a pipe is shown in figure 5(b). The most significant difference between the pipe and TBL is in the zonal thickness t in figure 5(c). The R_1 zones in a pipe are significantly thicker than the lower ranks, whereas the R_1 zones in the TBL did not show such a step change between $\Delta t|_{R_{1,2}}$ and $\Delta t|_{R_{2,3}}$. The R_1 zones correspond to the innermost zones in the pipe and the zones closest to the free stream in the TBL. The distribution of u_m , y_k and t for all ranks in the TBL is generally similar to a pipe for rank R_2 and below. This most centred UMZ is often referred to as the quiescent core of the pipe (and the channel) which can travel faster than the centreline velocity whereas in the TBL, all UMZs below the TNTI travel at velocities lower than the free-stream velocity. The significant differences observed in the R_1 zones of the pipe and TBL indicate that the first UMZ below the TNTI in a TBL does not correspond to the innermost zone in the pipe. Given the close similarity between the pipe and channel (Kwon et al. 2014; Kwon 2016; Yang et al. 2016), figure 5 suggests that the innermost UMZ in the pressure-driven wall turbulent flows behaves differently from the R_1 UMZ in the shear-driven TBL.

3.3. Characterisation of UMZ and UMZ interface

3.3.1. Wall-normal location of UMZ

The wall-normal location of the UMZs y_{κ} is averaged for UMZs in each group of the two grouping methods. Figure 6(a) shows $\langle y_{\kappa} \rangle$ for u_m groups $M_{1:6}$. The angle



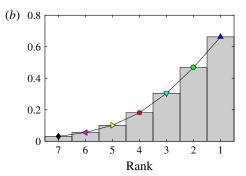


FIGURE 6. Conditionally averaged zone interface wall-normal location $y_{\kappa} = 1 - r_{\kappa}$ (r_{κ} is the radial location) for UMZs grouped by (a) zone modal velocity u_m , u_m groups $M_{1:6}$ and (b) by zone rank of u_m , ranking groups $R_{1:7}$. The dashed line in (a) is the mean velocity profile of \overline{U} plotted as $y(\overline{U})$.

brackets $\langle \rangle$ indicate conditional average for UMZs in each group. The UMZs in group M_6 with the lowest $u_m/U_{CL} \in [0.5, 0.6)$ are very close to the wall with $\langle y_{\kappa} \rangle$ almost equal to zero; y_{κ} gradually increases from M_6 to M_1 which has $\langle y_{\kappa} \rangle / R \approx 0.75$. The trend follows the mean profile of U plotted as $y(\overline{U})$ (dashed line). The change in y_{κ} is rather small near the wall for groups $M_{6:4}$ and becomes large for $M_{3:1}$ towards the pipe centre. In figure 6(b) for $\langle y_{\kappa} \rangle$ of UMZs in each ranking group $R_{1:7}$, a similar trend is shown. The nonlinear increase of y_{κ} from R_7 to R_1 indicates that the UMZs at lower ranks are more closely distributed nearer the wall while the higher ranked UMZs $(R_{1:3})$ are thicker so that they are further apart from each other towards the pipe centre. The results of y_{κ} using both grouping methods indicate that the UMZs are not uniformly distributed from the centreline to the wall but in a hierarchical distribution where zones near the wall are more densely populated, similar to TBL (de Silva *et al.* 2016, 2017).

The average thickness of the UMZs in each group can be calculated from the radial location r_{κ} of the zones. The calculation is illustrated in figure 7(a) for the grouping method based on the ranking of u_m . The illustration is idealised to have three UMZs ranked from R_1 to R_3 . Note that the thickness of the innermost zone equals its radial location r_{κ} . Figure 7(b) shows the group average thickness $\langle t \rangle$ of the UMZs calculated from $1 - \langle y_{\kappa} \rangle$. The value of $\langle t \rangle$ from group R_7 to R_1 increases monotonically: UMZs are the thinnest nearer the wall and the zone thickness increases when departing from the wall. The slope of $\langle t \rangle$ decreases group by group from the wall (R_7) toward the pipe centre until the second innermost group (R_2) , then there is a sudden increase in the slope of $\langle t \rangle$ for the innermost zones $(R_1$ and $M_1)$. This supports the previous finding in § 3.2 where the innermost UMZs in the pipe flow were found to be much thicker than the other UMZs in a pipe and the UMZ below the TNTI in a TBL. This is understood as in a pipe and channel, the opposing walls each have a flow similar to a TBL so that the innermost zone in a pipe contains the zones furthest away from the opposing walls interacting at the centre.

3.3.2. Zonal means inside and outside the UMZs

In order to investigate how UMZs at different wall-normal locations differ from each other, the zonal mean statistics of the UMZs in different u_m groups $M_{1:5}$ are computed.

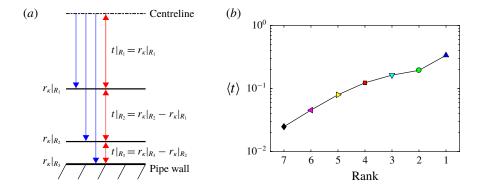


FIGURE 7. (a) An illustration of computing the average UMZ thickness of each u_m and ranking group, $\langle t \rangle$ from the average UMZ radial location r_{κ} of each group. (b) The average UMZ thickness $\langle t \rangle$ of each ranking group R_i .

The zonal mean inside a UMZ is averaged in the region between the UMZ lower-bounding interface closer to the wall up to the centreline, in other words, over its radial extent from the pipe centre (see the definition of r_{κ} in figure 2c); the zonal mean outside a UMZ is averaged over the region outside its lower bounding interface at r_{κ} towards the wall. Means inside the UMZ are denoted with a hat as \widehat{U} and $\widehat{u^2}$; means outside the UMZ are denoted with a tilde as \widetilde{U} and $\widetilde{u^2}$, similar to Kwon *et al.* (2014). Figure 8 shows the zonal mean inside $(\widehat{U}, \widehat{u^2})$ with dot-dashed lines and zonal means outside $(\widetilde{U}, \widetilde{u^2})$ with dashed lines. The global average profiles of \overline{U} and $\overline{u^2}$ with solid lines are shown as references.

In figure 8(a), the zonal mean profiles U are plotted for u_m groups $M_{1:5}$. The mean streamwise velocity inside the UMZ (\widehat{U}) is always larger than the time mean (\overline{U}) whereas the mean outside the UMZ (\widehat{U}) is always smaller than \overline{U} . The velocity difference between \widehat{U} and \widetilde{U} for each u_m group M_i indicates the velocity jump across the UMZ interface (see figure 9). The value of \widetilde{U} for each u_m group follows the time mean \overline{U} profile very near the wall and starts to deviate from \overline{U} away from the wall. The \widehat{U} data are available in a large range of wall-normal locations, and can extend very close to the wall at $y/R \approx 0.01$ for group M_5 . This shows the large meandering behaviour of the UMZ. To measure the level of meandering of the UMZs in terms of how far they can extend towards the wall in extreme cases, figure 8(b) shows the minimum wall-normal location \widehat{y} that the UMZ can extend to (where \widehat{U} is last available near the wall). The value of \widehat{y} for group $M_{5:2}$ increases steadily from the wall to the centre from $\widehat{y}/R \approx 0.01$ to 0.05 whereas the innermost UMZs with $u_m > U_{CL}$ in group M_1 can extend significantly less close to the wall with $\widehat{y}/R \approx 0.22$.

Figure 8(c,d) shows the zonal mean profiles of U and u^2 for UMZs in group M_2 only. This provides a relatively direct comparison between a pipe and channel: UMZs in group M_2 have $u_m/Ucl \in [0.9, 1)$ and the channel results are from a single UMZ defined at a fixed $u_\kappa/U_{CL} = 0.95$. In figure 8(c), the pipe profiles of group M_2 can extend further towards the wall due to the grouping: some of the UMZs in group M_2 are defined at a lower threshold velocity u_κ than the channel core so that they are naturally thicker and closer to the wall. The differences between the pipe profiles (in red) and the channel profiles (in black) are mainly caused by the difference in \overline{U} due to the Reynolds number difference. Higher Reynolds number of the channel

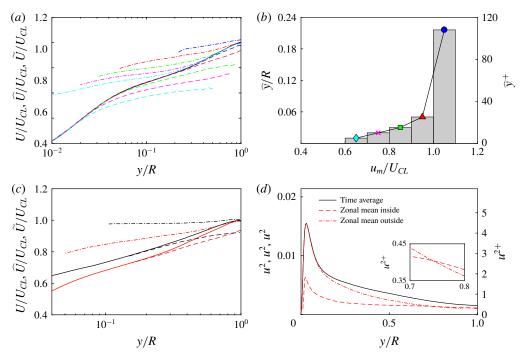


FIGURE 8. Zonal mean profiles of the streamwise velocity U for UMZs in u_m groups (a) $M_{1:5}$ with colours as in table 1 and (c) M_2 (in red) overlaid with channel flow results by Kwon *et al.* (2014) (in black). (b) The wall-normal location of the most near-wall data of the zonal mean inside the UMZs of each group in (a), \hat{y} (symbols as in table 1). (d) The streamwise velocity fluctuation u^2 for group M_2 only. The solid lines (——) are the time averages of U and u^2 in (a,c,d). The dot-dashed lines (— · —) are the zonal means inside the UMZ, \hat{U} and $\hat{u^2}$; the dashed lines (----) are the zonal means outside the UMZ, \hat{U} and $\hat{u^2}$.

 $(Re_{\tau}=1000)$ has \overline{U} developing faster nearer the wall. Otherwise, the trend between \widehat{U} , \widetilde{U} and \overline{U} is very similar in a pipe and channel. In figure 8(d), the zonal mean streamwise fluctuation u^2 is computed relative to zonal means of U following Kwon $et\ al.\ (2014)$

$$\hat{u^2} = (U - \hat{U})^2, \quad \tilde{u^2} = (U - \tilde{U})^2.$$
 (3.1*a*,*b*)

The turbulent intensity inside the UMZ, $\widehat{u^2}$, is much lower than the turbulent intensity outside the zone, $\widetilde{u^2}$. The difference between $\widehat{u^2}$ and $\widetilde{u^2}$ becomes smaller towards the centreline; $\widehat{u^2}$ and $\widetilde{u^2}$ cross over at $y/R \approx 0.74$ where $\widehat{u^2}$ starts to be larger than $\widetilde{u^2}$ until the centreline (see zoomed view inside figure 8d). A similar behaviour of $\widehat{u^2}$ and $\widetilde{u^2}$ was observed in the channel (Kwon *et al.* 2014) and the cross-over point of $\widehat{u^2} > \widehat{u^2}$ was also at $y/h \approx 0.74$ (h is the channel half-height). Therefore, despite the Reynolds number effect, the quiescent core of channel and the UMZs (M_2) of a pipe are very similar.

3.3.3. Conditional average across the UMZ interface

Conditional averages are computed for flow properties across the UMZ interface as functions of the distance from the interface, ξ . Figure 9(a) shows the group average

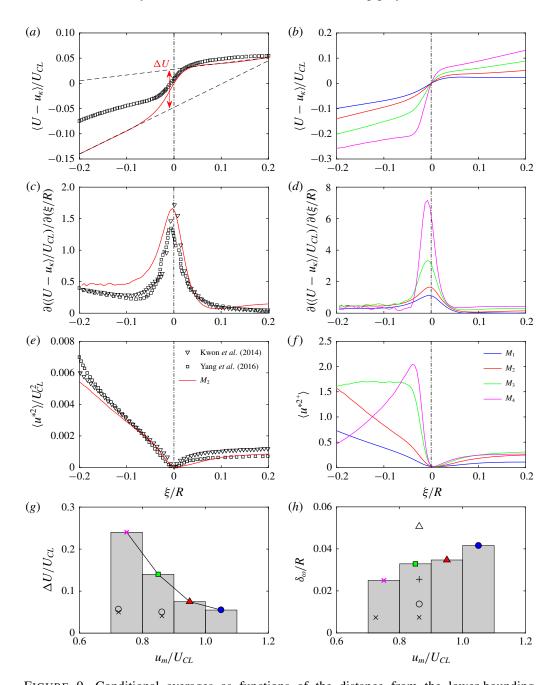


FIGURE 9. Conditional averages as functions of the distance from the lower-bounding UMZ interface (ξ) for (a) the streamwise velocity U for u_m group M_2 , (b) U for groups $M_{1:4}$, (c) velocity gradient $\partial U/\partial \xi$ for group M_2 , (d) $\partial U/\partial \xi$ for groups $M_{1:4}$, (e) streamwise velocity fluctuation u^{*2} for group M_2 and (f) u^{*2} for groups $M_{1:4}$. The legends in (e) and (f) apply to (a,c) and (b,d) respectively. (g) The magnitude of velocity jump in U across the UMZ interface, ΔU for groups $M_{1:4}$. (h) The UMZ interface thickness δ_ω calculated from (3.1) for groups $M_{1:4}$. (g,h) Are overlaid with TBL results by de Silva $et\ al.\ (2017)$ at $Re_\tau=14\,500\ (\times),\ Re_\tau=8000\ (\bigcirc),\ Re_\tau=2800\ (+)$ and $Re_\tau=1200\ (\triangle)$.

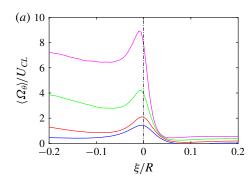
streamwise velocity $\langle U \rangle$ against ξ for a single u_m group M_2 , overlaid with results from the channel (Yang et al. 2016). The angle brackets () in this section indicate conditional averaging across the interface for UMZs in each u_m group; $\xi = 0$ indicates the UMZ interface and $\xi > 0$ represents the inside of the UMZ. In figure $\theta(a)$, the abrupt jumps in U across the interface are similar between UMZs in M_2 and the quiescent core of the channel: before entering the zone ($\xi < 0$), U develops fairly slowly until the near vicinity of the interface where it experiences a sharp change of the rate. The velocity gradient $\partial U/\partial \xi$ of group M_2 is shown in figure 9(c), overlaid with the results of the quiescent cores in the channel (Kwon et al. 2014; Yang et al. 2016). A local maximum of velocity gradient corresponding to the abrupt jump in U at the interface is similar here in a pipe. The streamwise fluctuation u^2 across the UMZ interface is shown in figure 9(e,f). In figure 9(e), for UMZs in group M_2 of pipe and the quiescent core of channel, u^2 behaves very similarly in a pipe and channel in which the streamwise fluctuation decreases dramatically across the interface with a local minimum at $\xi \approx 0$, and then remains very low inside the UMZ. In figure 9(f), the u^2 profiles for groups $M_{3,4}$ are different from groups $M_{1,2}$ because the UMZs in groups $M_{3,4}$ travelling at lower u_m are very close to the wall, close enough to capture the rapid increase in $\overline{u^2}$ in the near-wall region (see figure 8d for y/R < 0.05).

Figure 9(b) shows $\langle U \rangle$ against ξ for u_m groups $M_{1:4}$. The increase in U across the UMZ interface is larger (higher magnitude) and more abrupt (higher velocity gradient) for interfaces closer to the wall, as found in TBL (de Silva et al. 2017). Figure 9(d) corresponds to figure 9(b), showing the increase in maximum velocity gradient at $\xi = 0$ for UMZs nearer the wall travelling at lower u_m . The magnitude of the velocity jump, ΔU is defined similar to Yang et al. (2016), as illustrated in figure 9(a). The value of ΔU for UMZs in group $M_{1:4}$ is shown in figure 9(g) with the TBL results (de Silva et al. 2017) at $Re_{\tau} = 8000$ and 14 500. The values of ΔU in both pipe and TBL are found to be larger for UMZs travelling at lower u_m nearer the wall. The overall magnitude of ΔU in the pipe is significantly larger than the TBL. This is partly caused by the lower Reynolds number in the pipe: the number of UMZs is generally lower at lower Reynolds number so that U jumps across fewer interfaces with larger ΔU to achieve the centreline velocity. This increase in ΔU with decreasing Reynolds number is shown by the TBL results where the $Re_{\tau} = 8000$ case ('O') has higher ΔU than $Re_{\tau} = 14\,500$ ('×'). However, the increase in ΔU with lowering Reynolds number is not as significant as the difference in ΔU between the pipe and TBL. This suggest that the velocity jump of U across the UMZ interface is, on average, stronger in a pipe than TBL.

In figure 9(a-d), the velocity jumps and the peaked velocity gradients at the UMZ interface take place in a narrow distance over ξ as the UMZ interfaces themselves have a thickness (de Silva *et al.* 2017). The thickness of the interfaces is estimated by

$$\delta_{\omega} = \frac{\Delta \langle U \rangle}{\partial \langle U \rangle / \partial y|_{max}},\tag{3.2}$$

following Kwon et al. (2014) and de Silva et al. (2017). Figure 9(h) shows the UMZ interface thickness δ_{ω} for groups $M_{1:4}$. The value of δ_{ω} is lower for UMZs closer to the wall as found in the TBL, so that the thinner UMZs nearer the wall also have thinner interfaces accompanied by a sharper and larger jump in U. The hierarchical distribution of the UMZ and UMZ interface and the magnitude of ΔU together suggest a discrete step-like model of the velocity profile in wall turbulence which has been used as the initial velocity profile in the turbulence modelling by Bautista



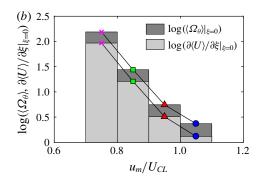


FIGURE 10. (a) Conditional-average azimuthal vorticity Ω_{θ} for u_m groups $M_{1:4}$ as a function of the distance from the lower-bounding UMZ interface. (b) The local maximum Ω_{θ} (in a) and $\partial U/\partial \xi$ (in figure 8d) at the UMZ interface ($\xi \approx 0$).

et al. (2019). The overlaid TBL results of δ_{ω} at $Re_{\tau} = 1200-14\,500$ are roughly in the range of u_m in group M_3 of the pipe. The interface thickness in the TBL increases when Re_{τ} decreases, as expected, since there are less UMZs at larger scales at lower Reynolds number. The UMZ interface in a pipe at a much lower $Re_{\tau} = 500$ has δ_{ω} in between the $Re_{\tau} = 2800$ and 1200 cases of the TBL, indicating that the UMZ interfaces are, on average, thinner in a pipe than TBL. This supports the previous finding where the velocity jump in U was found to be stronger in a pipe so that the velocity jumps in a pipe are more abrupt over thinner interfaces in a pipe than TBL. That the UMZ interfaces are found to be thinner in the DNS data of a pipe than the experimental data of a TBL may also be due to the limited spatial resolution in the experiments.

Figure 10(a) shows the conditional average of azimuthal vorticity $\langle \Omega_{\theta} \rangle$ against ξ where $\Omega_{\theta} = \partial V_r/\partial x - \partial U/\partial r$; Ω_{θ} peaks in the proximity of the interface similar to $\partial U/\partial \xi$ in figure 9(d). The initial Ω_{θ} away from the interface at $\xi/R = -0.2$ is significantly higher for UMZ groups closer to the wall since vorticities are stronger nearer the wall. The local maximum of Ω_{θ} at $\xi = 0$ in figure 10(a) and $\partial U/\partial \xi$ in figure 9(d) are plotted in figure 10(b). The peak azimuthal vorticity and streamwise velocity gradient have very similar trends: Ω_{θ} and $\partial U/\partial \xi$ both decrease almost log-linearly from the wall (M_4) towards the centre (M_2) , apart from the innermost UMZs in group M_1 , which shows a lowered rate of decrease. The differences in conditional averages of the innermost UMZs from the other zones are consistent with the findings in the previous §§ 3.3.1 and 3.2.

3.4. The vortex-interface attachment

3.4.1. Dynamics of the attachment

The local maximum azimuthal vorticity Ω_{θ} at the UMZ interface in figure 10(a) suggests a strong correlation between the UMZ interfaces and the vortical structures. Figure 11 shows an instantaneous UMZ interface defined at $u_{\kappa}/U_{CL}=0.8$ in (a) and 0.9 in (b) for the same snapshot in the streamwise plane, superpositioned on the contour of Ω_{θ} (with the prograde vortices in red and the retrograde vortices in blue). Different colour scales are used in figure 11(a,b) to improve the clarity of the contours of the surrounding vortical structures at different strengths. On these streamwise planes, the interface continuously follows the azimuthal vortices with

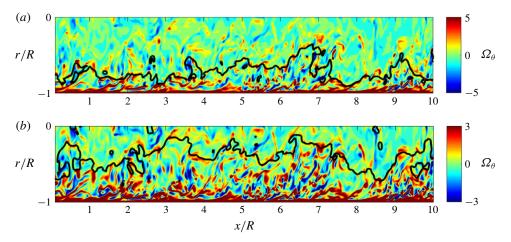


FIGURE 11. Contours of azimuthal vorticity Ω_{θ} in the streamwise plane, super-positioned with instantaneous UMZ interfaces defined at (a) $u_{\kappa}/U_{CL} = 0.8$ and (b) $u_{\kappa}/U_{CL} = 0.9$ for the same snapshot. The background contours of Ω_{θ} in (a,b) only differ in the colour axis.

similar strength, so that the $u_{\kappa}/U_{CL}=0.8$ interface in figure 11(a) is generally much closer to the wall, being attached to stronger vortices nearer the wall. This is consistent with the observations by Adrian *et al.* (2000) where patches of spanwise vortices were found aligned along the strong shear layers inside a TBL. In figure 11, the UMZ interface threads through the azimuthal vortices and folds into bulges and valleys to form a persistent vortex-interface attachment.

The dynamics of this vortex-interface attachment is further investigated. Supplementary movies of the attachment between vortices and UMZ interfaces over time are available in both fixed and moving frames at https://doi.org/10.1017/jfm.2019.947 (movies 1–4). Figure 12 shows three snapshots from the moving-frame video with a constant time gap. In these snapshots, the interface contorts to follow the inclined trains of eddies (marked with dashed lines) from the wall towards the pipe centre. The interface initially attached to vortex A in figure 12(a) meanders as vortex A deforms and moves with the flow in figure 12(b). In figure 12(c), when vortex A is weakened and merged with weaker eddies, the local interface changes significantly to reattach to a nearby vortex at A' to maintain the desirable vortical strength. The weakened vortex A then attaches to an iso-surface defined at a lower velocity threshold.

3.4.2. The three-dimensional attachment

Figure 13(a) shows the vortex-interface attachment in the azimuthal direction of the pipe on a cross-stream plane for a UMZ interface defined at $u_{\kappa}/U_{CL}=0.8$ corresponding to figure 11(b). The azimuthal vortices have elongated tube shapes in the azimuthal direction and vortices at similar strengths vary in their wall distance. Similar to the attachment shown in the streamwise direction in figure 11 and also Adrian et al. (2000), the UMZ interface contorts to attach to individual vortices and switches at the gaps between the azimuthal vortices to attach to the next vortex at desired strength. The 3-D attachment for the UMZ interface is shown in figure 13(b) for a UMZ interface defined at $u_{\kappa}/U_{CL}=0.8$. The attachment of the UMZ interface to vortical structures is significantly biased to the prograde vortices (in red) whereas the retrograde vortices (blue) are rarely found on the interface surface. To quantify

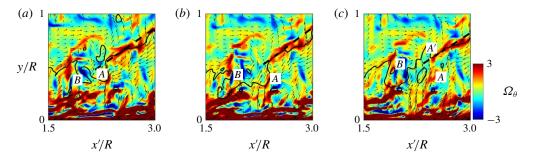


FIGURE 12. Contours of Ω_{θ} and the UMZ interface defined at $u_{\kappa}/U_{CL}=0.9$ plotted on a streamwise moving frame approximately at the flow speed downstream with time from (a) to (c) with a uniform time gap between each two of the three snapshots. Label A in (a,b) marks a prograde vortex weakened and joined the nearby vortices at A' in (c). Label B marks a strong retrograde vortex the interface is attached to. (The arrows show the vector of streamwise and wall-normal velocity fluctuations, u and v.)

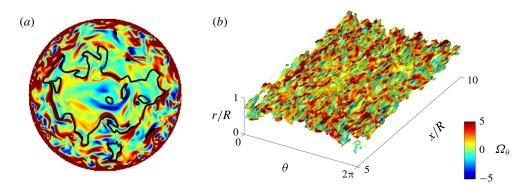
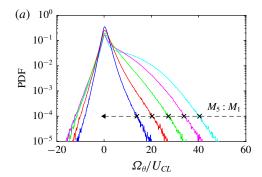


FIGURE 13. (a) Contour of azimuthal vorticity Ω_{θ} in a cross-stream plane, superpositioned with an instantaneous UMZ interface defined at $u_{\kappa}/U_{CL}=0.9$. (b) A 3-D instantaneous UMZ interface defined at $u_{\kappa}/U_{CL}=0.8$ with colour based on the azimuthal vorticity Ω_{θ} on the interface surface. The UMZ interface is shown for 1/6 of the streamwise extent, unwrapped in the azimuthal direction.

the attachment, figure 14(a) shows the time-average PDFs of Ω_{θ} on the 3-D interface surface of the UMZs in u_m groups $M_{1:4}$. Through group M_1 to M_5 from the centre to the wall, there is a continuous increase in the skewness of prograde vortices (defined as positive Ω_{θ}) denoted as Ω_{θ}^p , which is the strongest closest to the wall. The negative ends of the PDFs representing attachment on retrograde vortices (Ω_{θ}^r) show small changes for different UMZ groups. The magnitude of prograde vorticity Ω_{θ}^p at a fixed PDF of 10^{-4} for each u_m group (marked by '×' along the dashed line at PDF= 10^{-4}) is shown in figure 14(b). The increase in Ω_{θ}^p against UMZ modal velocity u_m shows a marked linearity, even for the fastest travelling UMZs in group M_1 which have been found to be different from the other groups in the previous results. The linear increase of Ω_{θ}^p towards the wall against u_m has a slope of $d\Omega_{\theta}^p/du_m \approx 66.4$ with negligible variation (maximum 4.8%) between different u_m groups.

Figure 15 shows the conditional-average vorticity of the prograde (Ω_{θ}^{p}) and retrograde (Ω_{θ}^{r}) vortices for UMZs in group M_{2} against ξ . At the interface $(\xi = 0)$



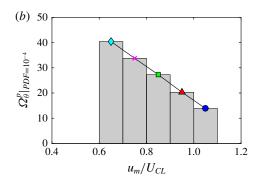


FIGURE 14. (a) PDF of the azimuthal vorticity Ω_{θ} on the 3-D UMZ interfaces for u_m groups $M_{i=1:5}$. Here, Ω_{θ} is defined as positive for prograde vortices and negative for retrograde vortices. (b) The magnitude of positive prograde azimuthal vorticity, Ω_{θ}^{p} at a probability density of 10^{-4} for groups $M_{1:5}$ (marked by '×' in (a)).

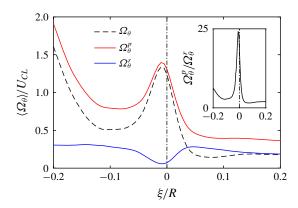


FIGURE 15. Conditional-average profiles of total azimuthal vorticity Ω_{θ} , prograde vorticity Ω_{θ}^{p} and retrograde vorticity Ω_{θ}^{r} as functions of distance from the UMZ interface (ξ) for u_{m} group M_{2} . The total azimuthal vorticity $\Omega_{\theta} = \Omega_{\theta}^{p} - \Omega_{\theta}^{r}$. The inset shows the ratio between the prograde and retrograde vorticity $\Omega_{\theta}^{p}/\Omega_{\theta}^{r}$ against ξ .

where the total Ω_{θ} peaks in figure 10, here, it shows that nearly all Ω_{θ} is contributed from Ω_{θ}^{p} while Ω_{θ}^{r} decreases to a local minimum at the UMZ interface. The distribution of $\Omega_{\theta}^{p,r}$ for group M_{2} is, again, very similar to the quiescent core in the channel (Yang *et al.* 2016). Inside figure 15, the ratio of prograde and retrograde vorticity peaks at the interface, achieving $\Omega_{\theta}^{p}/\Omega_{\theta}^{r} \approx 25$ for UMZs in group M_{2} . Results in this section suggest that the contorted shape of the UMZ interface is a consequence of its attachment to the azimuthal/spanwise vortices which move three-dimensionally with varying wall-normal location. Additionally, the attachment is predominantly to prograde vortices.

3.5. The contortion of the UMZ interface

The contortion of the UMZ interfaces forms bulges and valleys similar to the engulfment of TNTI. The UMZ interface contortion is a different way of viewing the streaky feature of the streamwise velocity fluctuation: the valleys extending closer to

the wall corresponds to the high-speed streaks while the bulges where the interface shrink towards the pipe centre are the low-speed streaks U. The UMZ interface contortion away from the wall largely represents the LSM and VLSM whereas the UMZ interface in the very-near-wall region captures the streamwise fluctuation of the near-wall cycle. Figure 16 shows an instantaneous UMZ interface belonging to u_m group M_2 with $u_{\kappa}/U_{CL} = 0.9$, coloured based on the interface radial location r_{κ} . The UMZ interface can meander very close to the pipe wall, sweeping high-speed flow closer to the wall (red) or shrinking towards the pipe centre with low-speed flow ejected toward the pipe centre (blue). Figure 16(b) unwraps the UMZ interface in figure 16(a) along the azimuthal direction θ using the same colour axis based on r_{κ} , viewing the outer surface of the interface facing towards the pipe wall. The streaks of high- and low-momentum flow are similar to the channel (Kwon et al. 2014). Figure 16(c) shows the inner surface of the interface facing the pipe centre which is not visible in figure 16(a). An inverse colour axis based on the wall-normal location of the interface y_k is used so that ejections (bulges) towards the pipe centre are now in red. The inner face of the UMZ interface shows some significantly amplified bulges, for example, at $\theta \approx \pi/2$ and $x/R \approx 8$, which was not evident for the channel (Kwon et al. 2014). (The difference between bulges and valleys on the UMZ interface is discussed in detail in § 3.6.) This particular UMZ interface with $u_{\kappa}/U_{CL} = 0.9$ in figure 16 is located relatively in the centre of the pipe where the large-scale highand low-momentum streaks (red and blue) of the LSMs are evident, and bear a clear similarity to those in the channel flow (Monty et al. 2007; Illingworth, Monty & Marusic 2018).

3.5.1. The 2-D contortion

The contortion of the UMZ interface surface in the streamwise and azimuthal directions are computed from the 3-D instantaneous velocity field. The 2-D contortion is measured by the UMZ interface length in the streamwise (r-x) plane) and azimuthal $(r-\theta)$ plane) directions, denoted as l_x and l_θ respectively. Here, l_x and l_θ are computed by an algorithm that calculates the exact length of the interface using the high resolution 3-D data. The lengths of the islands outside the enclosed region of the main part of the UMZ are preserved because it is found that, in three dimensions, the frequently observed islands on the 2-D planes are relatively rare. A majority of the islands are connected in three dimensions as part of the three-dimensional interface contortion. In figure 16, the projections on the streamwise and cross-stream planes show examples for l_x and l_θ , respectively.

The lengths of the interface per unit length in both directions are shown in figure 17(a). Here, l_x is normalised by the streamwise extent of the pipe $L_x = 30R$ while l_{θ} is normalised by the perimeter of a circle with a radius equal to the UMZ interface average radius r_{κ} : $L_{\theta} = 2\pi \langle r_{\kappa} \rangle$. Because $\langle r_{\kappa} \rangle$ varies for UMZs in different u_m groups, the unit length in the azimuthal direction L_{θ} is not constant but is larger nearer the wall. In figure 17, both l_x/L_x and l_{θ}/L_{θ} increase as UMZs move away from the wall towards the centre of the pipe through $M_{1:5}$, so that the 2-D contortion intensifies for interfaces away from the wall in both directions. The UMZ interface in the azimuthal direction is always more contorted than the streamwise direction as l_{θ}/L_{θ} is always higher than l_x/L_x in all u_m groups. The same trend was found for the quiescent core of a channel (Yang et al. 2016) which has l_x/L_x overlaid in figure 17(a) as ' \square ' and l_{θ}/L_{θ} by ' \bigstar ' between groups $M_{1,2}$. The increase of both l_x/L_x and l_{θ}/L_{θ} is rather slow initially near the wall. Away from the wall, l_{θ}/L_{θ} shows significantly more rapid increase towards to the pipe centre whereas l_x/L_x

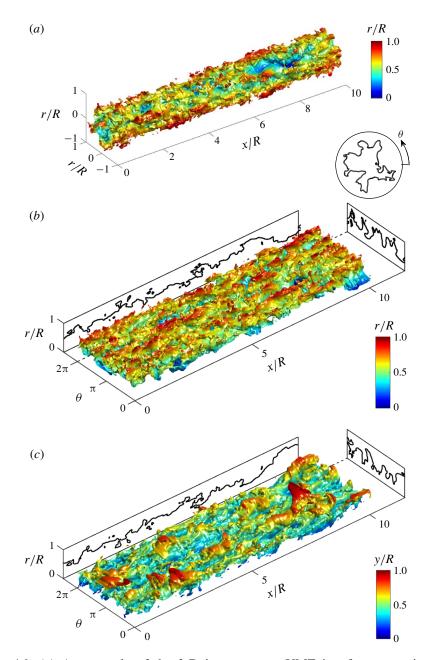
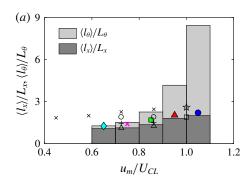


FIGURE 16. (a) An example of the 3-D instantaneous UMZ interface as an iso-surface defined at $u_{\kappa}/U_{CL}=0.9$. Colour indicates the radial elevation of the interface: bulges ejecting away from the wall are in blue and sweeping extensions towards the wall are in red. (b) The interface in (a) unwrapped in the azimuthal direction, showing the outside of the interface that is facing the wall. The 2-D projections of the interface are plotted on the streamwise plane at $\theta=2\pi$ and the cross-stream planes (original and unwrapped) at x/R=10. (c) Interface unwrapped from (a), showing the inside of the interface facing the pipe centre. The colour in (c) is different from (a,b) where red indicates ejections and blue indicates sweeps towards the wall.



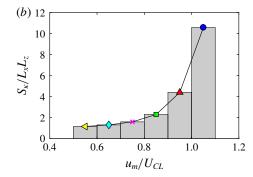


FIGURE 17. (a) UMZ folding intensity in two dimensions: the average length of UMZ interface per unit length in the streamwise direction, l_x/L_x and the azimuthal direction, l_θ/L_θ for u_m groups $M_{1:5}$. The streamwise extent $L_x=30R$ is constant and the azimuthal extent $L_\theta=2\pi\langle r_\kappa\rangle$ varies for UMZs in different groups with $\langle r_\kappa\rangle$ as the average radial location of the UMZ interface of a group. The markers are l_θ/L'_θ with constant azimuthal extent $L'_\theta=\pi R$ for all groups. The overlaid results from TBL by de Silva *et al.* (2017) at $Re_\tau=14\,500$ (×), $Re_\tau=8000$ (○), $Re_\tau=2800$ (+) and $Re_\tau=1200$ (△) are for l_x/L_x only. The overlaid channel flow results by Yang *et al.* (2016) at $Re_\tau=1000$ have l_x/L_x (□) and l_θ/L_θ (★). (b) UMZ interface folding intensity in three dimensions: the average surface area of the 3-D UMZ interface S_κ per unit area L_xL_z for groups $M_{1:6}$.)

increases much more slowly than l_{θ}/L_{θ} . The 2-D azimuthal contortion l_{θ}/L_{θ} shows a very strong wall-distance dependence compared to l_x/L_x since L_{θ} increases in the radial direction as r_{κ} . When a constant unit azimuthal length $L'_{\theta}=2\pi R$ is used for normalisation, which is more comparable to the channel with a fixed spanwise extent, l_{θ}/L'_{θ} (represented by symbols) still increases as UMZs move away from the wall but very slowly with a very similar trend to l_x/L_x . The value of l_{θ}/L'_{θ} is still always higher than l_x/L_x as found in the channel, suggesting that the contortion of the 3-D interface is stronger in the azimuthal direction than in the streamwise direction in both a channel and pipe.

The 2-D contortion in the streamwise direction l_x/L_x from TBL by de Silva *et al.* (2016) of $Re_{\tau} = 1200-14\,500$ is also overlaid on the pipe results in figure 17(a). There is a clear increase in l_x/L_x when the Reynolds number increases in the TBL. For u_m groups $M_{3,4}$, the streamwise contortion of UMZs in the pipe is very close to the TBL at a roughly doubled Reynolds number $Re_{\tau} = 1200$. This supports the previous findings in conditional averages where UMZs in a pipe at a lower Reynolds number are quantitatively more similar to a TBL at higher Reynolds numbers.

3.5.2. The 3-D contortion

The 3-D contortion of the UMZ interface is measured by the surface area of the interface S_{κ} per unit area $L_x L_{\theta}$ where $L_x L_{\theta}$ is the area of a smooth surface at the interface average radial location $\langle r_{\kappa} \rangle$ with zero contortion. Figure 17(*b*) shows $S_{\kappa}/L_x L_{\theta}$ for u_m groups $M_{1:6}$; $S_{\kappa}/L_x L_{\theta}$ shows a very similar trend to l_{θ}/L_{θ} in which the increase is rather slow initially in groups $M_{6:4}$ with a UMZ interface area roughly twice the unit area. The 3-D contortion is the lowest for UMZs closest to the wall (M_6) and achieves the highest $S_{\kappa}/L_x L_{\theta} \approx 11$ in group M_1 . It is interesting to note that S_{κ} of the inner most UMZ interfaces (M_1) is over 10 times the non-contorted reference area. The contortion of the UMZ interfaces behaves similarly as a function of the wall distance, both the

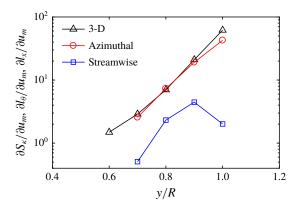


FIGURE 18. The gradient of the 2-D and 3-D interface folding intensities l_x , l_θ and S_κ in figure 17 against UMZ modal velocity u_m .

2-D and 3-D contortions of UMZ interfaces intensify when departing from the wall. This may be partly due to the suppression from the wall where interfaces are less free to meander and also because that the streamwise fluctuation is on smaller scales nearer the wall. The increase in UMZ interface contortion with distance from the wall shows the increase in meandering of the LSMs with wall distance (Kevin & Hutchins 2019). The rate of increase of the 3-D contortion is shown in figure 18 as the gradient of $\partial S_{\kappa}/\partial u_m$. The slope of the semi-log straight line $\partial^2 S_{\kappa}/\partial u_m^2 = 10^c$ has the exponent c = 9.7 with a maximum 15 % variation between different u_m groups.

3.6. Asymmetric large-scale modulation and bursting

The symmetry/asymmetry of Q2 ejections (bulges) and Q4 sweeps (valleys) on the UMZ interface is investigated for all u_m groups covering a wider range of scales in the flow along the wall-normal direction. Figure 19 shows the unwrapped 3-D surface of an instantaneous UMZs in u_m group M_2 away from the wall, and another one in group M_6 very close to the wall. The fluctuation of the wall-normal location of the UMZ interface is defined as $y'_{\kappa} = y_{\kappa} - \langle y_{\kappa} \rangle$. The value of y'_{κ} is plotted on the cross-stream plane at x/R = 5 for both interfaces in figure 19. Positive y'_{κ} corresponds to the bulges on UMZ interfaces for ejections while negative y'_{κ} represents the valleys for sweep events. In figure 19(a), the magnitudes of sweep and ejection of the UMZ in group M_2 away from the wall show no clear bias whereas the near-wall UMZ interface from group M_6 is positively skewed, showing amplified ejections compared to sweeps. This matches the findings in a channel and TBL where the amplified near-wall activities as footprint of the large-scale structures (Marusic 2001; Jiménez *et al.* 2004; Hutchins & Marusic 2007a,b; Mathis, Hutchins & Marusic 2009a; Mathis *et al.* 2009b) are asymmetric towards ejections into bursting (Agostini & Leschziner 2014).

The asymmetry between bulges and valleys, ejections and sweeps are measured by the skewness of the wall-normal location fluctuation y'_{κ} as a function of the wall distance using 3-D volumetric data. The skewness of y'_{κ} is computed as $\zeta = y'^3_{\kappa}/\sigma^3$ where σ is the standard deviation of the fluctuation. Positive ζ indicates asymmetry with biased ejection over sweep; negative ζ indicates sweep over ejection; and $\zeta = 0$ indicates balanced ejection and sweep. Figure 20 shows the average skewness $\langle \zeta \rangle$ for UMZs in u_m groups $M_{1:6}$. UMZs closest to the wall (M_6) show the highest asymmetry towards Q2 ejections with $\zeta > 1$. The level of asymmetry biased to ejection events

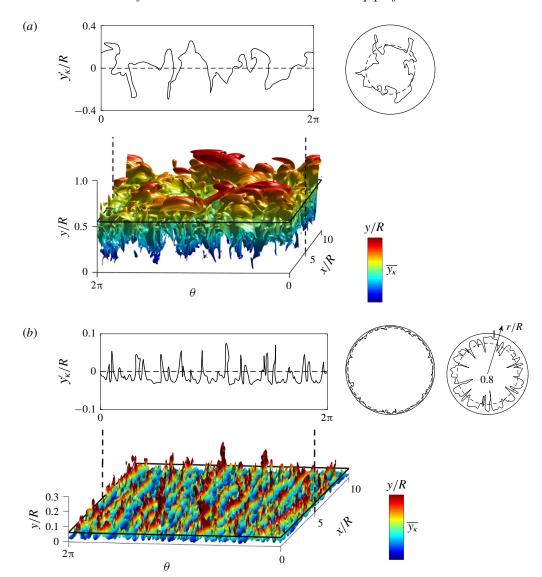


FIGURE 19. Examples of instantaneous 3-D UMZ interfaces in u_m groups (a) M_2 with $u_\kappa/U_{CL}\approx 0.9$ and (b) M_6 with $u_\kappa/U_{CL}\approx 0.5$. The colour axes for both interfaces are centred on the average wall-normal location of the interface $\langle y_\kappa \rangle$. The 2-D projections of the interfaces in the cross-stream plane are at x/R=5. The interface wall-normal location fluctuation y_κ' has $y_\kappa'=y_\kappa-\langle y_\kappa\rangle$.

decrease for UMZs departing from the wall towards the centreline. In group M_2 , with UMZs being the most comparable to the quiescent core in a channel (Kwon *et al.* 2014; Yang *et al.* 2016), $\zeta \approx 0$ indicates that the UMZs in this group have fairly symmetric sweep and ejection. The innermost UMZ group M_1 is the only group with negative ζ so these innermost UMZs travelling at $u_m > U_{CL}$ have opposite asymmetric behaviour of sweep over ejection. The gradient of the decrease in asymmetry level, $\partial \zeta / \partial u_m$ is plotted on the right-hand side y-axis. Here, $\partial \zeta / \partial u_m$ decreases uniformly

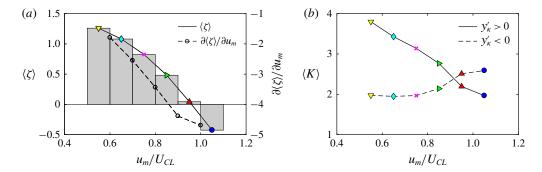


FIGURE 20. Conditional average of (a) skewness ζ of the UMZ interface wall-normal location fluctuation around the average interface wall-normal location, $y_{\kappa}' = y_{\kappa} - \langle y_{\kappa} \rangle$ (positive ζ indicates that the interface is skewed towards the pipe centre with bulge regions of ejection events more amplified than the valley regions of sweep events, and *vice versa*; $\zeta \to 0$ indicates balanced bulge and valley on the UMZ interface) and (b) kurtosis K of the positive (Q2 ejection) part and negative (Q4 sweep) part of the UMZ interface fluctuation y_{κ}' in u_m groups $M_{1:6}$.

except for the innermost UMZs in group M_1 . It is, again, evident that the innermost UMZ in a pipe is different from the other UMZs.

Another feature of the UMZ interfaces shown in figure 19 is that the UMZ interface closer to the wall in figure 19(b) is spikier for Q2 ejections ($y'_{\kappa} > 0$) where the Q4 sweep regions are relatively smooth and flat. Away from the wall, the UMZ interface from group M_2 shows the opposite trend, in which the sweeps towards the wall are spikier than ejections. Figure 20 shows the statistical measurement of the spikiness of the UMZ interfaces in each u_m group by computing the kurtosis $K = y_{\kappa}^{4}/\sigma^{4}$ of the ejection part $(y'_{\kappa} > 0)$ and sweep $(y'_{\kappa} > 0)$ part of the UMZ interfaces. The value of K of the ejection part of the UMZ interface decreases monotonically with wall distance whereas the sweep region has K increasing towards the pipe centre. The cross-over point of $K \mid y'_{\kappa} > 0$ and $K \mid y'_{\kappa} < 0$ indicates that the innermost UMZ interfaces in groups $M_{1,2}$ occupying the centred half of the pipe $(\langle y_{\kappa} \rangle / R \ge 0.5)$ have the opposite spikiness between ejections and sweeps from groups $M_{3:6}$. The UMZs closest to the wall in group M_6 has ejection regions nearly twice sharper than the sweeps $(K \mid y'_{\kappa} > 0/K \mid y'_{\kappa} < 0 \approx 1.93)$ whereas the inner most UMZs have ejections 25 % less sharp than the sweeps. The spiky upper part of the near-wall UMZ interfaces and the lower part of the centre interfaces show an interlocking structural arrangement between the near-wall ejections and the large-scale sweeps from the centre. The flatness of the near-wall sweeps and centre ejections on the UMZ interface is due to the suppression from the wall and the congested pipe centre with flow coming in from the opposing walls respectively.

3.7. Summary: comparing turbulent pipe, channel and boundary layer flows

Similarities and differences between the present results of turbulent pipe, channel and TBL have been shown. First, the pipe and channel are widely accepted to be more similar as both are pressure-driven wall turbulence (Monty *et al.* 2009). The zonal mean flow properties in § 3.3.2 are found to be very similar between a pipe and channel (Kwon *et al.* 2014) in terms of both trend and measurement. The only difference is in the mean velocity profile \overline{U} due to different Reynolds numbers so

that the channel with Re_{τ} doubled compared to the pipe has \overline{U} developing faster near the wall (see figure 8c). The conditional-average quantities show a large number of similarities between the quiescent cores of the channel (Kwon $et\ al.\ 2014$; Yang $et\ al.\ 2016$) and the UMZs in a pipe travelling at similar u_m . This includes the jumps in the streamwise velocity U with local peaks of velocity gradient across the UMZ interface, and the rapid decay of turbulent intensity at the interface which remains low inside the UMZ. The conditional-average profiles are similar in both the trend and measurement between the pipe and the channel with slight differences caused by the grouping of UMZs in the pipe.

By comparing to the TBL results by Laskari et al. (2018), the innermost UMZ in a pipe is found to be very different to the outermost UMZ below the TNTI in a TBL, which are the UMZs travelling at the highest u_m furthest away from the wall in both geometries. The innermost UMZ in a pipe (often referred to as the quiescent core) also exhibits different behaviours to all the other UMZs in a pipe. This includes its average wall distance, zone thickness, maximum extent to the wall by meandering. The other UMZs in a pipe apart from the 'core' are otherwise qualitatively very similar to a TBL, such as the hierarchical distribution of the UMZs in the wall-normal direction. The conditional average of the streamwise velocity jump at the UMZ interface and interface thickness show similar trends as functions of the wall distance in a pipe and TBL but with significantly different measurements. The velocity jump over UMZ interfaces is noticeably larger in a pipe than TBL with the Reynolds number effect taken into account. The differences in statistical results suggest that, for turbulent pipe and boundary layer flows at a similar Re_{τ} , there are on average, more UMZs in a pipe with thinner interfaces accompanied by a larger jump in U and higher azimuthal/spanwise vorticity. These interfaces are more contorted in the streamwise direction (and very possibly in the azimuthal/spanwisedirection in three dimensions) of a pipe than a TBL at similar Reynolds numbers. All these results suggest that the two pressure-driven wall-bounded flows, the pipe and channel, are similar both qualitatively and quantitatively whereas a pipe and TBL with many qualitative similarities differ quantitatively. Although only the quiescent core region as the single innermost UMZ in the channel is compared in the study, the general trends suggest that the similarities between these three types of wall turbulence decrease when comparing pipe to channel, channel to TBL and TBL to pipe (Monty et al. 2009).

3.8. A note on the Reynolds number effect

The present results of pipe flow are at a moderate $Re_{\tau} = 500$. Quantitative similarities between the pipe and TBL (see §§ 3.3.3 and 3.5.1) at different Reynolds numbers suggest that the characteristics of UMZs in a pipe are comparable to TBL at a much higher Reynolds number ($Re_{\tau} \approx 1200-2800$). The present pipe data show a low Reynolds number effect in the mean axial velocity \overline{U} compared to a channel at $Re_{\tau} = 1000$ (Kwon et al. 2014). The UMZs in lower u_m or ranking groups are very close to the wall, where turbulence has been found not to scale with wall variables at low Reynolds numbers (Wagner, Huttl & Friedrich 2001). In turbulent channel flow at very low Reynolds number, direct interaction of opposing walls and a lower wavenumber in velocity fluctuation in the near-wall region were observed by Antonia et al. (1992). Lower wavenumbers in the near-wall velocity fluctuations at low Re_{τ} reduce the number of high- and low-momentum streaks with increased streaks spacing. This has been observed when comparing the present pipe flow to pipe data at a lower and a higher $Re_{\tau} = 180$ and 1000 (not shown for brevity). For UMZs in the near-wall region, this low Reynolds number effect would result in lower contortion in both two and three dimensions with less turbulent production near the wall.

4. Conclusion

This study investigates the characteristics and dynamics of the multiple uniformmomentum zones (UMZ) and UMZ interfaces in a fully developed turbulent pipe flow. The high resolution 3-D data from DNS is used to compare the UMZs in pipe, channel and TBL. Extensive qualitative similarities were found between these three types of wall turbulence: the hierarchical scale of UMZs being thinner and demarcated by thinner UMZs nearer the wall; the sharp velocity jump and concentrated azimuthal/spanwise vortices at the UMZ interfaces; when the number of UMZ increases, all existing zones becomes thinner, move away from the wall and travel at higher velocities to accommodate the more refined zones near the wall. The innermost UMZs in the pipe are found noticeably different to all the other UMZs which behave similar to the multiple UMZs in TBL, such as an increase in zone thickness and a higher local maximum of azimuthal vorticity at the interface. Conditional-average analyses show a large number of quantitative similarities between a pipe and channel where the pipe and TBL have different measurements. At a comparable Reynolds number, there are, on average, more UMZs in a pipe than TBL and channel, and these are bounded by thinner interfaces. Some quantitative similarities between the present pipe flow at a moderate Reynolds number $Re_{\tau} = 500$ and results of TBLs at higher Reynolds numbers (doubled) suggest that a pipe may be more comparable to a TBL at a higher Reynolds number.

The contortion of the UMZ interface, which is a manifestation of the high- and low-momentum streaks of streamwise velocity fluctuation, is investigated in both two and three dimensions. The interface contortion in both two and three dimensions increases with increasing wall distance. The 2-D meandering of the UMZ interface in the azimuthal direction is always more intense than the streamwise direction. The faster-travelling UMZs away from the wall are representative of LSMs while the UMZs in the near-wall region capture the small-scale velocity fluctuation of the near-wall cycle. The third-order skewness between bulges and valleys on the 3-D UMZ interface shows that the large-scale modulation on the near-wall activities is asymmetric to ejections over sweeps. When departing from the wall, the level of asymmetry decreases to symmetric/balanced ejections and sweeps. The innermost UMZs travelling faster than the centreline velocity show the opposite asymmetry of more amplified sweeps over ejections. The fourth-order kurtosis of the ejections and the sweep part of the UMZ interface show that the small-scale near-wall ejections are twice spikier than the sweeps and the opposite occurs in the centre half of the pipe. The biased skewness and kurtosis between ejections and sweeps shows the difference between the large-scale and the small-scale structures.

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Declaration of interests

The authors report no conflict of interest.

Supplementary movies

Supplementary movies are available at https://doi.org/10.1017/jfm.2019.947.

Appendix. Statistics of UMZs detected from kernel density estimation

To investigate the effect of using different detection schemes on the results of UMZ characteristics, some of the results shown in the main sections are reproduced using kernel density estimation (KDE) for UMZ detection. A consistent algorithm to Fan *et al.* (2019) is used: a Gaussian KDE with bandwidth $h = \sigma (4/3)^{1/5} n^{-1/5}$ where σ is the standard deviation of U from the snapshot and n is the sample size of U.

Figure 21(a) shows the histogram of U from an instantaneous snapshot where the kernel function and the peak detection agree with each other on the well-distinctive peaks. The KDE algorithm suggests fewer UMZs $N_{UMZ} \approx 3$ on average than the PDF method (figure 3), but N_{UMZ} is still higher in the pipe than the channel (Fan *et al.* 2019) when both using KDE for UMZ detection. Figure 21(b) shows the PDF of the number of KDE detected UMZs in each of the modal velocity groups used in this study. The KDE bandwidth filters out many of the slower-travelling UMZs in the lower u_m groups but the distribution is very similar to the result

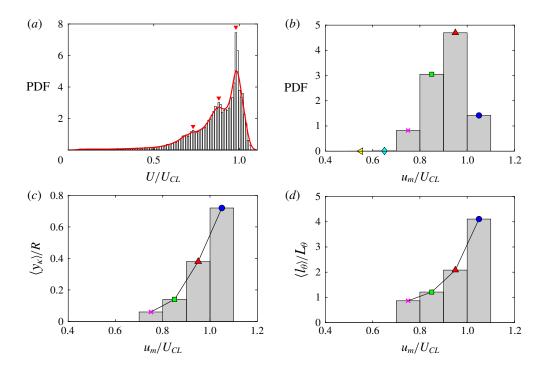


FIGURE 21. (a) The PDF of instantaneous U from a snapshot; the peaks representing the UMZs detected from the peak detection scheme are labelled by ' ∇ '; the red line is the kernel estimation function of the PDF with bandwidth $h = \sigma(4/3)^{1/5} n^{-1/5}$. (b) PDF of N_{UMZ} in each u_m group of $M_{1:6}$ for UMZs detected from KDE. (c) Conditional-average interface wall-normal location y_k for UMZs detected from KDE in u_m group $M_{1:4}$. (d) Two-dimensional UMZ interface folding intensity in the azimuthal direction, l_θ/L_θ for u_m groups $M_{1:4}$ for UMZs detected from KDE. The KDE results in (b-d) correspond to figures 4(a), 6(a) and 17(a) respectively.

from using the peak detection scheme (figure 4a). Figure 21(a,b) shows the average wall-normal location and the 2-D contortion of UMZ interfaces in the higher u_m groups $M_{1:4}$ and correspond to figures 6(a) and 17(a) respectively. The change of detection scheme alters the group average but the trend of y_k and l_θ/L_θ is consistent: the UMZs are thicker away from the wall, forming a hierarchical distribution and the UMZ interfaces are wavier when departing from the wall. The replicated results using KDE instead of PDF peak detection show that the statistical behaviours of the UMZ are reasonably insensitive to the detection scheme.

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