# Generation of proton beams from two-species targets irradiated by a femtosecond laser pulse of ultra-relativistic intensity

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#### Abstract

The paper presents results of two-dimensional particle-in-cell simulations of ion beam acceleration at the interactions of a 130-fs laser pulse of intensity in the range  $10^{21}-10^{23}$  W/cm<sup>2</sup>, predicted for the Extreme Light Infrastructure lasers, with thin hydrocarbon (CH) or erbium hydride (ErH<sub>3</sub>) targets. A special attention is paid to the effect of the laser pulse intensity and polarization (linear, circular) on the proton energy spectrum, the proton beam spatial distribution and the proton pulse shape and intensity. It is shown that for the low laser intensities (~ $10^{21}$  W/cm<sup>2</sup>) considerably higher proton beam parameters (proton energies, beam intensities) are achieved for the ErH<sub>3</sub> target for both polarizations and the effect of polarization on the beam parameters is significant (higher parameters are achieved for the linear polarization). However, for the highest, ultra-relativistic intensities (~ $10^{23}$  W/cm<sup>2</sup>) higher proton beam parameters are attained for the CH target and the effect of polarization on these parameters is relatively low. In this case, for both polarizations quasi-monoenergetic proton beams are generated from the CH target of the mean proton energy ~2 GeV and  $dE_p/\bar{E}_p \approx 0.3$  for the linear polarization and  $dE_p/\bar{E}_p \approx 0.2$  for the circular one. At the highest laser intensities also the proton pulse peak intensities are higher for the CH target and for both polarizations they reach values well above  $10^{21}$  W/cm<sup>2</sup>. In the paper, the properties of proton beam generation indicated above are discussed in detail and a physical explanation of the observed effects is done.

Keywords: Laser acceleration; Laser plasma; Ions; Particle-in-cell simulations

#### 1. INTRODUCTION

Extreme Light Infrastructure (ELI) (Danson *et al.*, 2015; https://www.eli-laser.eu) is a currently implemented largescale European project that uses cutting-edge laser technologies to build multi-petawatt (PW) lasers generating femtosecond pulses of ultra-relativistic intensities  $\sim 10^{22}$ – $10^{23}$  W/ cm<sup>2</sup>. The launch of ELI will open a doorway into new areas of fundamental research as well as establishing new technical developments and applications. Laser-driven ion/ proton acceleration is a topical and rapidly developing research area stimulated by a variety of potential applications. The use of the ELI lasers to accelerate ions makes it possible to apply the produced intense ion beams of sub-GeV and GeV ion energies into various branches of nuclear physics (Ledingham & Galster, 2010) and high-energy-density physics (Patel *et al.*, 2003; Macchi *et al.*, 2013; Fernandez *et al.*, 2014) as well as for medical applications such as the hadron cancer therapy (Bulanov *et al.*, 2002; Ledingham & Galster, 2010; Macchi *et al.*, 2013).

The mechanisms of ion acceleration and parameters of generated ion beams depend significantly on both the laser beam and irradiated target parameters, in particular on the laser beam intensity and the thicknesses and composition of the target. The ions can be accelerated by several laserinduced mechanisms such as: the TNSA (target normal sheath acceleration) (Wilks et al., 2001; Borghesi et al., 2006; Badziak, 2007; Macchi et al., 2013), the RPA (radiation pressure acceleration) (Esirkepov et al., 2004; Macchi et al., 2005, 2013; Liseykina et al., 2008; Robinson et al., 2008) [also known as the skin-layer ponderomotive acceleration (SLPA) (Badziak, 2007; Badziak et al., 2008b)], the laser BOA (break-out afterburner) (Yin et al., 2006, 2007; Macchi et al., 2013; Fernandez et al., 2014), the CESA (collisionless electrostatic shock acceleration) (Denavit, 1992; Silva et al., 2004; Macchi et al., 2013), or the LICPA (laserinduced cavity pressure acceleration) (Badziak et al., 2010,

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2012). Since the dominant acceleration mechanism is determined by the laser-target interaction conditions, the laser beam parameters as well as the structure of the targets must be carefully selected to produce the ion beams of characteristics required for a particular application. Furthermore, the ion acceleration mechanisms should be well identified and controlled.

Previous studies presented in papers (Foord *et al.*, 2008; Domański et al., 2016a, b) have shown a strong influence of the target composition on the ion beam parameters. It was proven that in the case of laser pulses produced by the PW titanium-sapphire laser facilities (laser intensity  $I_{\rm L} \leq$  $10^{21}$  W/cm<sup>2</sup>, laser power  $P_L < 1$  PW), using hydride targets with heavy atoms, instead of commonly used hydrocarbon (CH) targets, allows for a considerable increase in all particular important parameters of the proton beams. In this paper, we deliver a comprehensive analysis of the effect of the target composition as well as the laser beam polarization and intensity for the laser beam parameters predicted for the ELI facilities. This research was performed using two-dimensional (2D) particle-in-cell (PIC) simulations, which are a convenient and effective tool for studies of laser-driven ion acceleration and for the prediction of parameters of laseraccelerated ion beams. The correctness of the PIC code used in the simulations was verified by a comparison of the results obtained using this code with the ones from the measurements presented in (Badziak et al., 2008a) as well as with the results of 3D simulations of carbon ion acceleration carried out in (Sgattoni et al., 2014).

The numerical simulations were performed for thin CH and heavy atoms erbium hydride (ErH<sub>3</sub>) targets irradiated by a 130 fs duration laser pulse of the intensity ranging from  $10^{21}$  to  $10^{23}$  W/cm<sup>2</sup> and 800 nm wavelength. The laser pulse shape in time and space (along the y-axis) was described by a super-Gaussian function of the power index equal to 6 and the laser beam width (FWHM-Full Width Half Maximum) was assumed to be 8 µm. The transverse dimensions of the targets were equal to 12 µm and their areal mass density ranging from 0.06 to 0.8 mg/cm<sup>3</sup>. Molecular densities of the targets corresponded to solid-state densities and they were equal to  $4.86 \times 10^{22}$  molecules/cm<sup>3</sup> for CH and  $2.69 \times$  $10^{22}$  molecules/cm<sup>3</sup> for ErH<sub>3</sub>. The ionization degrees of target components were assumed to be 1 for hydrogen, 6 for carbon and 10 (Foord et al., 2008) for erbium. A pre-plasma layer of 0.25 µm thickness and the density shape described by an exponential function was placed in front of the target. The simulations were performed in the s, y space equal to  $160 \times 32 \,\mu\text{m}^2$  and the number of macroparticles (optimized) was assumed to be  $5 \times 10^6$  for thinner targets ( $\sigma_t \le 0.2 \text{ mg}/$ cm<sup>2</sup>) and  $9 \times 10^6$  for thicker targets ( $\sigma_t > 0.2 \text{ mg/cm}^2$ ).

### 2. RESULTS AND DISCUSSION

Figure 1 presents a 2D spatial distribution of charge density of erbium ions (a), carbon ions (c), and protons (b, d) generated from both types of investigated target. The targets were irradiated by the circularly polarized (CP) laser pulses of intensity equal to  $10^{23}$  W/cm<sup>2</sup> and the presented situation



Fig. 1. The 2D spatial distributions of charge density of erbium ions (a), carbon ions (c), and protons (b, d) generated from the ErH<sub>3</sub> (a, b) and CH (c, d) targets.  $I_L = 10^{23} \text{ W/cm}^2$ , circular polarization.



Fig. 2. The 2D spatial distributions of charge density of erbium ions (a), carbon ions (c) and protons (b, d) generated from the ErH<sub>3</sub> (a, b) and CH (c, d) targets.  $I_L = 2 \times 10^{23} \text{ W/cm}^2$ , linear polarization.

corresponds to the final stage of ion acceleration (the simulation time is equal to 0.4 ps). It can be observed that protons are clearly separated from the erbium ions which attain much lower velocities than protons. The difference between velocities of protons and carbon ions is much smaller, and some carbon ions move with the velocities close to the proton velocities. It is worth mentioning that the mean energy achieved by the protons generated from the CH target is higher than for those generated from the ErH<sub>3</sub> target, and that the energy dispersion of protons emitted from the CH target is quite small. The analogical plot for the linearly polarized (LP) laser pulse is presented in Figure 2. It is clearly visible that the parameters of ion beams generated from both types of the target do not depend significantly on the state of polarization of the laser beam.

The weak influence of laser polarization on the acceleration process could be explained by the dominance of the RPA mechanism. In this mechanism the mean ion energy depends on the laser energy fluence and the target areal density. These parameters were identical for the considered cases with different polarizations.

Figure 3 presents a 2D spatial distribution of electric field component parallel to laser beam propagation direction for CP and for the initial and later stages of simulations. This component of the electric field is directly responsible for ion acceleration. It is visible that protons are accelerated by the RPA field. The difference between energies of proton beams generated using CH and ErH<sub>3</sub> can be explained by the difference in the strength of interaction between heavier

ions stored in the target and the electric field which accelerates these ions. The interaction between erbium ions and the field is much weaker than the interaction between the field and carbon ions due to the lower q/m value for the erbium ions (q is the ion charge and m is the ion mass). For this reason, the amount of energy transferred by the field to protons during the initial stage of acceleration is higher for the erbium-hydrogen plasma than for the CH plasma (Fig. 4). However, in the RPA mechanism the acceleration process is limited by the transparency of the plasma. The plasma becomes transparent for light when the density of electrons in plasma decreases below the critical density. In the case of ErH<sub>3</sub> target, the electrons are concentrated both in the region of erbium ions and protons in later phases of acceleration, while in the case of polystyrene target the electrons achieve more or less the same velocity as protons and carbon ions and are concentrated in the same region. For this reason, in the case of CH target the dispersion of electron energy is smaller and the density of electrons is higher. Consequently, for the CH target the plasma becomes transparent later and the process of ion acceleration lasts longer than for the ErH<sub>3</sub>. As a result, after a sufficiently long time (>100 fs) the higher energies of protons are achieved for the polystyrene target (Fig. 4).

Figure 5 presents the energy spectra of protons accelerated forward from both types of investigated target by a CP or LP laser pulse for the early and late stages of simulation. As opposite to the previous studies for lower laser intensities (Domański *et al.*, 2016*a*, *b*), the shapes of most of these spectra



Fig. 3. The 2D spatial distributions of electric field component parallel to laser beam propagation direction for circular polarization in the initial (a) and later (b) stages of acceleration.  $I_{\rm L} = 10^{23} \, \text{W/cm}^2$ .

are rather similar to the Gaussian distribution. For this reason, the parameters appropriate to describe the spectra are the mean ion energy and the standard ion energy deviation. The mean energy of protons generated from the polystyrene target for both types of polarization is equal to 1.8 GeV. The proton energy dispersion is smaller for the CP than for the linear one and the standard deviation expressed in the mean energy units is equal to  $dE_p/\bar{E}_p = 0.19$  for CP and  $dE_p/\bar{E}_p = 0.3$  for LP. The mean energy of protons generated from the ErH<sub>3</sub> target is equal to 0.7 GeV for CP and 0.6 GeV for LP, while the standard deviations of proton energies equal to 0.68 for CP and 0.71 for LP. The difference between energy dispersion of the proton beam generated from different targets



Fig. 4. The time dependence of the mean energy of protons generated from CH and ErH<sub>3</sub> targets.  $I_{\rm L} = 10^{23}$  W/cm<sup>2</sup>.



**Fig. 5.** The energy spectra of protons generated forward from the ErH<sub>3</sub> target and the CH target for two different stages of the proton acceleration.  $I_{\rm L} = 10^{23}$  W/cm<sup>2</sup> for CP and  $I_{\rm L} = 2 \times 10^{23}$  W/cm<sup>2</sup> for LP, (a) linear polarization, (b) circular polarization.

could be explained by the higher penetration of the laser pulse into the proton sheet in case of the  $ErH_3$  target.

The following figures present the mean energy and the standard energy deviation of protons (Fig. 6) and heavy ions (Fig. 7) generated from both types of target and for both types of polarization as a function of laser beam intensity (the laser energy fluence is the same for both types of polarization, the laser intensities on the horizontal axis correspond to CP). It can be observed that the influence of the target's composition on the efficiency of ion acceleration significantly depends on the laser beam intensity. For high laser intensities  $\geq 10^{22} \text{ W/cm}^2$ , the mean proton energies are higher for CH than for ErH<sub>3</sub>, while for the lower ones the higher proton energies are achieved for the ErH<sub>3</sub> target. This effect could be explained by the fact that at lower laser intensities the influence of relativistic transparency on the acceleration process is low and the efficiency of proton acceleration is determined by the q/m value of the heavy ion component of the target [see the explanation related to Figure 4 and (Domański et al., 2016b)].

Both for CH and  $\text{ErH}_3$  the widths of the proton energy spectrum are smaller for CP than for LP. Additionally, for the CH target they decrease with an increase in laser intensity. The dispersion of proton energy for the  $\text{ErH}_3$  target is higher than that for the CH target and weakly depends on the laser intensity. The average energies per nucleon of





Fig. 6. The mean energy (a) and the standard energy deviation (b) of protons generated from the  $ErH_3$  target and the CH target as a function of laser intensity for linear (LP) and circular (CP) polarization.



**Fig. 7.** The mean energy (a) and the standard energy deviation (b) of heavy ions generated from the  $\text{ErH}_3$  target and the CH target as a function of laser intensity for linear (LP) and circular (CP) polarization.

heavy ions are much higher for the carbon ions than for the erbium ions. The energy spectra of both kinds of ions are broad  $(dE_i/\bar{E}_i \sim 1)$  and the widths of the spectra weakly depend on the intensity.

The quantitative values of the mean energy and the standard energy deviation for protons and heavy ions for the ErH<sub>3</sub> and the CH targets as a function of the areal target density  $\sigma_t$  are shown in Figures 8 and 9. For thin targets of  $\sigma_t < 0.1 \text{ mg/cm}^2$ , the mean proton energies are higher for CH than for ErH<sub>3</sub>, while for thicker targets the higher efficiencies of the proton acceleration are achieved for the ErH<sub>3</sub> target. Since the electron energy dispersion in the ErH<sub>3</sub> target is higher than in the CH one, this type of target becomes transparent for the laser light earlier which results in lower proton energies when the target is thin. For thick targets the laser pulse cannot penetrate through the target and better results are achieved for ErH<sub>3</sub>.

Such characteristics of ion beams as the beam intensity, the beam ion current density and the shape and duration of the ion pulse are important from the point of view of potential applications of laser-generated ion beams and in the applications such as the fast ignition of nuclear fusion, the production of high-energy-density matter or some nuclear physics experiments, they play a key role (Patel *et al.*, 2003; Ledingham & Galster, 2010; Macchi *et al.*, 2013; Fernandez *et al.*, 2014). Figure 10 presents the temporal distributions of intensity of proton beams generated from the ErH<sub>3</sub> target and the



**Fig. 8.** The mean energy (a) and the standard energy deviation (b) of protons generated from the ErH<sub>3</sub> target and the CH target as a function of the target areal density for linear (LP) and circular (CP) polarization.  $I_{\rm L} = 10^{23}$  W/cm<sup>2</sup> for CP and  $I_{\rm L} = 2 \times 10^{23}$  W/cm<sup>2</sup> for LP.



**Fig. 9.** The mean energy (a) and the standard energy deviation (b) of heavy ions generated from the ErH<sub>3</sub> target and the CH target as a function of the target areal density for linear (LP) and circular (CP) polarization.  $I_{\rm L} = 10^{23}$  W/cm<sup>2</sup> for CP and  $I_{\rm L} = 2 \times 10^{23}$  W/cm<sup>2</sup> for LP.



Fig. 10. The temporal distribution of intensity of proton beams generated from the ErH<sub>3</sub> target and the CH target for linear (a) and circular (b) polarization.  $I_L = 10^{23}$  W/cm<sup>2</sup> for CP and  $I_L = 2 \times 10^{23}$  W/cm<sup>2</sup> for LP.



Fig. 11. The spatial distribution of intensity of proton beams generated from the ErH<sub>3</sub> target and the CH target for linear (a) and circular (b) polarization.  $I_{\rm L} = 10^{23}$  W/cm<sup>2</sup> for CP and  $I_{\rm L} = 2 \times 10^{23}$  W/cm<sup>2</sup> for LP.

CH target for the linear (a) and circular (b) polarization. These distributions were detected 40 µm behind the rear surface of the target. The spatial (transverse) distributions of the proton beam intensity are shown in Figure 11. The weak influence of laser polarization on the temporal distribution of the proton beam can be observed. In turn, the target's composition strongly influences this characteristic. In the case of CH target, the proton pulse of duration equal to ~11 fs and intensity by an order of magnitude higher than in the case of CH target is produced. It is worth mentioning that the generated proton beams are much shorter and their intensities are much higher than those produced in classical accelerators. For ErH<sub>3</sub>, the waists of the ion beams are comparable to the waist of the laser pulse, while for CH, they are broader.

Figure 12 presents the peak proton beam intensity (a) and the peak proton current density (b) as a function of laser beam intensity for the ErH<sub>3</sub> and CH targets and for both types of laser beam polarization. In the case of higher laser intensities, the presented values are higher for the CH target, while in the case of lower laser intensities they are higher for the ErH<sub>3</sub> target or are similar for both types of the targets. In particular, at the laser pulse intensity of  $10^{23}$  W/cm<sup>2</sup> and the polystyrene target the peak proton beam intensity and the peak proton current density reaches extremely high values, respectively, of  $0.8 \times 10^{22}$  W/cm<sup>2</sup> (two orders of magnitude higher than for the ErH<sub>3</sub> target)



**Fig. 12.** The peak proton beam intensity (a) and the peak proton current density (b) as a function of laser intensity for the  $ErH_3$  and CH targets and for both types of laser beam polarization.

and of  $4.5 \times 10^{12}$  A/cm<sup>2</sup> (one order of magnitude higher than for the ErH<sub>3</sub> target).

## 3. CONCLUSIONS

It has been shown that the influence of the target's compositions on the parameters of the generated ion/proton beams significantly depends on other laser-target system parameters such as the laser pulse intensity and the target's thickness. In the case of laser intensities  $\geq 10^{22}$  W/cm<sup>2</sup> and CH and ErH<sub>3</sub> targets with areal densities smaller than 0.1 mg/ cm<sup>2</sup> higher efficiency of proton acceleration is obtained for the CH targets, while in other cases the higher accelerations efficiency is achieved with the ErH<sub>3</sub> targets. At the laser intensities predicted for the ELI lasers ( $\sim 10^{23} \text{ W/cm}^2$ ), both for the circular and the linear laser light polarization, the mean energies of protons generated for the CH target can reach values approaching 2 GeV; however, the proton energy spectrum is relatively broad (~0.2  $\bar{E}_p$  for CP and ~0.3  $\bar{E}_{p}$  for LP). At short distances from the irradiated target (<50 µm), the proton pulse is very short (<20 fs), and the proton beam intensities and the proton current densities reach extremely high values,  $>10^{21}$  W/cm<sup>2</sup> and  $>10^{12}$  A/cm<sup>2</sup>, respectively, which are much higher than those attainable in conventional accelerators. Such proton beams can open the door for new areas of research in

high-energy-density physics as well as nuclear physics and can also prove useful for some medical applications.

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