Strong terahertz radiation generation by beating of two laser beams in magnetized overdense plasma

A. HEMATIZADEH, F. BAKHTIARI, S. M. JAZAYERI, AND B. GHAFARY

Department of Physics, Iran University of Science & Technology, Narmak, Tehran, Iran (RECEIVED 28 March 2016; ACCEPTED 20 June 2016)

Abstract

Terahertz (THz) radiation generation by nonlinear mixing of two laser beams, obliquely incident on an overdense plasma is investigated. In an overdense plasma, the laser beams penetrate to only thin layer of a plasma surface and reflected. At this thin layer, the laser beams exert a ponderomotive force on the electrons of plasma and impart them oscillatory velocity at the different frequency of lasers. THz waves appear in the reflected component from the plasma surface. The amplitude of THz waves can be augmented by applying the magnetic field perpendicular to the direction of propagation of lasers. It is found that the field strength of the emitted THz radiations is sensitive to the angle of incident of the laser beams, beat frequency, and magnetic field strength. In this scheme, the magnetic field strength plays an important role for strong THz wave generation.

Keywords: Overdense plasma; Magnetic field; Beat frequency; Terahertz generation

1. INTRODUCTION

The problem of efficient generation of terahertz (THz) radiation, frequency range 0.1-10 THz, has attracted considerable interest over the past 10 years due to a lot of important promising applications. Numerous applications can be found in a wide range of fields such as physics, chemistry, biology, information, and security (Cooke & Jespen, 2009; Bartman et al., 2011; Tao et al., 2011; Kim et al., 2012). Various techniques have been employed for THz generation using highpower lasers. Many laser-based THz emitters have been proposed to generate THz wave, using electro-optic crystals (ZnTe, GaAs, LiNbo3, etc.), semiconductors and photoconductive antennas (Jepsen et al., 1996; Hashimshony et al., 1999; Lee et al., 2000; Faure et al., 2004; Vodopyanov, 2008; Chen et al., 2011). When the energy or focusing intensity of the pump laser is high, the materials may be damaged (Li et al., 2012b). In contrast, plasmas can overcome the damage problem of neutral materials. Recent studies have shown that plasmas are promising media to generate strong THz radiation (Sheng et al., 2005). In principle, the laser intensity can be arbitrarily high for plasmas. The typical intensity of a multi-terawatt (TW) laser system is higher than 10^{18} w/cm² (up to 10^{21} w/cm² with a Petawatt laser) (Li

et al., 2012b). Hamster et al. (1993) observed a high-power THz radiation from a plasma short pulse produced by laser, employing 1 TW, 100 fs laser beam focused on gas and solid targets. They also observed THz radiation in a laserinduced plasma channel where ponderomotive force drives radiation. Antonsen et al. (2007) examined the ponderomotive force-driven THz radiation generation in a plasma with space periodic axial density variation. Wu et al. (2007) have studied the effect of transverse magnetic field on the wakefield process and found a significant enhancement in the efficiency of THz generation. Fedele et al. (1986) have reported radial electric field components generated by the propagation of two electromagnetic waves resonantly beating in a plasma. Malik et al. (2010) investigated the THz generation by tunnel ionization of a gas jet with the help of superposed femtosecond laser pulses and by laser beating in periodically modulated plasma. They also reported the generation of tunable THz radiation under the application of 2 fs laser pulses with an external magnetic field (Malik & Malik, 2011). The resonant excitation of THz radiation by beating of two spatial-Gaussian laser beams has been proposed by Malik et al. (2012). Bakhtiari et al. (2015a) have studied the THz generation by beating of two dark hollow laser beams and two circular flat-topped laser beams. Bakhtiari et al. (2015b) have showed strongly THz radiation generation through shape control of emitted THz radiation in collisional plasmas. Chauhan and Parashar (2014) have

Address correspondence and reprint requests to: A. Hematizadeh, Department of Physics, Iran University of Science & Technology, Narmak, Tehran, Iran. E-mail: hematizade@physics.iust.ac.ir

considered two laser beams, which obliquely incident on a plasma slab for two different electron density profiles. Parashar (2014) has reported THz radiation by beating of two laser beams, which obliquely incident on the plasma. Kumar et al. (2015) investigated THz generation in hot plasma with step density profile by two obliquely incident of lasers on the plasma. Compared with low-density gases, overdense plasmas of solids have higher electron density thus holding the promise of producing higher-power THz pulses (Li et al. 2012b). Interaction of laser with an overdense plasma also results in generation of electromagnetic radiation at harmonics of incident wave in the reflected component. Gopal et al. (2012) have reported experimental observation of THz radiation from the rear surface of a solid target with an intense laser pulse and showed THz radiation is mostly emitted at large angles to the target normal. Adak et al. (2015) have observed experimentally THz radiation by a pump pulse at an angle of 45° and a probe pulse at near normal incident, which are focused on a polished BK-7 glass target. Weiss et al. (2000) have showed experimentally by applying an external magnetic field, the power of the generated THz radiation is increased for all examined semiconductor materials. Hangyo et al. (2001) have studied experimentally THz radiation from indium arsenide (InAs) surfaces in the presence of the magnetic field, which excited by femtosecond laser pulses. McLaughlin et al. (2000) have demonstrated experimentally enhancement of THz emission from InAs in the presence of magnetic fields up to 8 T. Migita and Hangyo (2001) have reported experimentally enhancement of THz radiation from InAs surfaces under magnetic fields excited by ultrashort laser pulses for low and high pump power densities. Li et al. (2012a) have reported a plasma-based strong THz source generated in intense laser-solid interactions at relativistic intensities when the laser pulses are incident onto a copper foil at 67.5° Li et al. (2011) have studied interactions of 100 fs laser pulses with solid targets. Shvartsburg and Stenflo (1994) have formulated a new method to study reflection of wideband electromagnetic pulses at a plasma boundary. Aliev et al. (1993) have studied total backward reflection of electromagnetic radiation due to resonant excitation of surface wave over plasma. Parashar et al. (2013) have studied THz radiation in the overdense plasma. Chen et al. (2013) have studied THz radiation by interaction of a relativistic circularly polarized laser pulse with an overdense plasma and have showed remarkably intense THz pulses.

In this work, we study THz radiation generation via nonlinear mixing of two obliquely incident laser beams over an overdense plasma in the presence of magnetic field. Overdense plasmas have been considered since it can be easily realized by employing a metallic sheet or a semiconductor. Also contrary to neutral materials and plasma filaments, almost arbitrarily high laser energies and intensities can be used in laser–solid interactions (Li *et al.*, 2012*b*).

This paper is organized as follows: In Section 2, we study nonlinear oscillatory current density due to the ponderomotive force developed during photo mixing of two laser beams in the presence of static magnetic field. In Sections 3 and 4, we evaluate the THz radiation field and efficiency. In Section 5, we present the results of analytical investigations. Conclusions are presented in Section 6.

2. CALCULATION OF NONLINEAR CURRENT DENSITY

We consider two p-polarized lasers with frequencies ω_1 , ω_2 and wave vector $\vec{k_1}$, $\vec{k_2}$, propagating and polarized in the *xy*plane that obliquely incident on an overdense plasma in the presence of a static magnetic field B_0 along the *z*-direction (Fig. 1).

We consider the electric field of incident lasers as

$$\vec{E}_j = \vec{E}_{j0} \exp\left(-i\left(\omega_j t - \frac{\omega_j}{c}\cos\theta_i x - \frac{\omega_j}{c}\sin\theta_i y\right)\right), \qquad (1)$$

where $\vec{E}_{j0} = A_{j0}(-\tan \theta_i \hat{x} + \hat{y}), j = 1,2.$

In an overdense plasma, where the frequency of incident laser beam smaller than plasma frequency, the electromagnetic radiation cannot penetrate deeply into the plasma. It penetrates into the plasma as far as the evanescence length, which is of the order of $\sim c/\omega_p$ (Bulanov *et al.*, 2001), where, *c* is the speed of light in the vacuum and ω_p is the plasma frequency. Therefore the transmitted fields of laser in the plasma, can be written as (Parashar *et al.*, 2013).

$$\vec{E}_{jT} = \left(\hat{y} - \frac{\omega_j \sin \theta_i}{c} \hat{x}\right) T_j A_{j0} \\ \times \exp\left(-i\left(\omega_j t - \frac{\omega_j}{c} \sin \theta_i y - \frac{\omega_j}{c} \cos \theta_i x\right)\right)$$
(2)

$$\times \exp(-\alpha_j x),$$

where $\alpha_j = (\omega_p^2/c^2 - \omega_j^2 \cos^2 \theta_i/c^2)^{1/2}$, $\omega_p = (4\pi n_0 e^2/m)^{1/2}$, $T_j = 2/(1 + (i\omega_j/\alpha_j c)\cos\theta_i)$, n_0 is equilibrium electron density, *m* and *e* are the electron mass and charge. Since the plasma is overdense, the plasma frequency ω_p must be larger than ω_1 and ω_2 . It is supposed that $\omega_1 > \omega_2$, therefore $n_0 > n_c$. n_c is the critical density and given by $n_c = m\omega_1^2/4\pi e^2$. Lasers impart



Fig. 1. Schematic diagram of THz radiation generation from overdense plasma.

oscillatory velocity to the electrons of plasma $\vec{v_j} = e\vec{E_j}/mi\omega_j$ and exert beat frequency ponderomotive force on them.

$$\vec{F}_{\rm p}^{\rm NL} = -\frac{m}{2} \vec{\nabla} (\vec{v}_1 \bullet \vec{v}_2^*). \tag{3}$$

The nonlinear perturbations in the electron density n_e^{NL} due to nonlinear ponderomotive force \vec{F}_p^{NL} are obtained by solving of continuity equation

$$n_{\rm e}^{\rm NL} = \frac{n_0}{m(\omega^2 - \omega_{\rm c}^2)} \vec{\nabla} \cdot \left(\vec{F}_{\rm p}^{\rm NL} + \vec{F}_{\rm p}^{\rm NL} \times \frac{\omega_{\rm c} \hat{z}}{i\omega}\right),\tag{4}$$

where $\omega_c = eB_0/mc$, $\omega = \omega_1 - \omega_2$ are the electron cyclotron frequency and beating frequency. The density perturbation produces a self-consistent space charge field $\vec{E} = -\vec{\nabla}\phi$ that also produces a density perturbation $n_e^{\rm L} = -(\chi_e/4\pi e)\vec{\nabla}.(\vec{\nabla}\phi)$, where $\chi_e = -\omega_p^2/(\omega^2 - \omega_c^2)$. Linear ponderomotive force is given by $\vec{F}^{\rm L} = e\vec{\nabla}\phi$. Using Poisson's equation $\vec{\nabla}.(\vec{\nabla}\phi) =$ $4\pi e(n_e^{\rm L} + n_e^{\rm NL})$ and equation of motion $m(d\vec{v}_{\omega}^{\rm NL}/dt) = \vec{F}^{\rm L} +$ $\vec{F}^{\rm NL} - \vec{v}_{\omega}^{\rm NL} \times (eB_0/c)\hat{z}$ the nonlinear electron velocity obtained as follows:

$$\vec{v}_{\omega}^{\text{NL}} = \left[f_x \hat{x} + f_y \hat{y} \right] \exp(-(\alpha_1 + \alpha_2)x) \\ \times \exp(-i \left[\omega t - k_x x - k_y y \right]),$$
(5)

where f_x , f_y , f_0 , k_y , and k_x are defined as

$$f_x = \frac{f_0}{mi\omega(1 + (\omega_c/i\omega)^2)} \times \left[\left(\frac{-\chi_e}{(1 + \chi_e)} + 1 \right) + \frac{-\omega_c^2\chi_e}{\omega^2(1 + \chi_e)} \right) (ik_x - (\alpha_1 + \alpha_2)) \\ + \left(\frac{-\chi_e\omega_c}{i\omega(1 + \chi_e)} + \frac{\omega_c}{i\omega} \left(\frac{-\chi_e}{(1 + \chi_e)} + 1 \right) \right) ik_y \right],$$

$$f_{y} = \frac{f_{0}}{mi\omega(1 + (\omega_{c}/i\omega)^{2})} \times \begin{bmatrix} -\left(\frac{-\chi_{e}\omega_{c}}{i\omega(1 + \chi_{e})} + \frac{\omega_{c}}{i\omega}(\frac{-\chi_{e}}{(1 + \chi_{e})} + 1)\right) \\ (ik_{x} - (\alpha_{1} + \alpha_{2})) \\ +\left((\frac{-\chi_{e}}{(1 + \chi_{e})} + 1) + \frac{-\omega_{c}^{2}\chi_{e}}{\omega^{2}(1 + \chi_{e})}\right)ik_{y} \end{bmatrix},$$

$$f_{0} = \frac{e^{2}T_{1}T_{2}^{*}A_{10}A_{20}}{2m\omega_{1}\omega_{2}}\left(1 + \frac{\omega_{1}\omega_{2}\sin^{2}\theta_{i}}{c^{2}\alpha_{1}\alpha_{2}}\right),$$

$$k_y = \frac{\omega \sin \theta_i}{c}, \quad k_x = \frac{\omega \cos \theta_i}{c}.$$

From Eq. (5) we can calculate the nonlinear current density $\vec{J}_{\omega}^{\rm NL}$ as

$$\bar{J}_{\omega}^{\rm NL} = -n_0 e \bar{v}_{\omega}^{\rm NL},$$

$$\vec{J}_{\omega}^{\text{NL}} = -n_0 e \Big[f_x \hat{x} + f_y \hat{y} \Big] \exp(-(\alpha_1 + \alpha_2) x) \\ \times \exp(-i \Big[\omega t - k_x x - k_y y \Big] \Big).$$
(6)

3. THZ RADIATION GENERATION

The wave equation governing the THz wave is derived from the third and fourth Maxwell's equations

$$\nabla^2 \vec{E}_{\omega} - \vec{\nabla} (\vec{\nabla} \cdot \vec{E}_{\omega}) + \frac{\omega^2}{c^2} \bar{\bar{\varepsilon}} \vec{E}_{\omega} = \frac{-4\pi i \omega}{c^2} \vec{J}_{\omega}^{\text{NL}},\tag{7}$$

where $\overline{\epsilon}$ is the electric permittivity tensor with components $\epsilon_{xx} = \epsilon_{yy} = 1 - (\omega_p^2/(\omega^2 - \omega_c^2))$, $\epsilon_{xy} = -\epsilon_{yx} = (i\omega_p^2\omega_c/\omega(\omega^2 - \omega_c^2))$, $\epsilon_{zz} = 1 - (\omega_p^2/\omega^2)$, and $\epsilon_{xz} = \epsilon_{yz} = \epsilon_{zx} = \epsilon_{zy} = 0$ (Bittencourt, 2004). The solution of wave equation in the vacuum x < 0 is given by plane wave as

$$\vec{E}_{\rm I} = \vec{E}_{\rm THz} = A_{\rm R} \left[\frac{k_y}{k_x} \hat{x} + \hat{y} \right] \\ \times \exp\left(-i \left[\omega t + k_x x + k_y y \right] \right).$$
(8)

Equation (7) is nonhomogeneous second-order partial differential equation. The general solution of this equation comprises from its particular solution and solution of homogeneous part. Homogeneous part of Eq. (7) is $\nabla^2 \vec{E}_{\omega} - \vec{\nabla}(\vec{\nabla}.\vec{E}_{\omega}) + (\omega^2/c^2)$ $\overline{\epsilon}\vec{E}_{\omega} = 0$, which its solution is as

$$A_{\rm T}[\delta \hat{x} + \hat{y}] \exp(-i[\omega t - k_x x - k_y y]),$$

where

$$\delta = \frac{(-k_y\beta + (\omega^2/c^2)\varepsilon_{yx})}{(-k_y^2 + (\omega^2/c^2)\varepsilon_{xx})}, \quad \beta = \sqrt{\frac{\omega^2}{c^2}} \left(\varepsilon_{xx} + \frac{\varepsilon_{yx}^2}{\varepsilon_{xx}}\right) - k_y^2.$$

Particular solution of Eq. (7) is given by

$$\begin{bmatrix} E'_{0x}\hat{x} + E'_{0y}\hat{y} \end{bmatrix} \exp(-(\alpha_1 + \alpha_2)x) \\ \times \exp(-i[\omega t - k_x x - k_y y]),$$

where

$$E'_{0x} = \frac{(4\pi i \omega n_0 e/c^2)}{(-k_y^2 + (ik_x - (\alpha_1 + \alpha_2))^2)(\omega^2/c^2)\varepsilon_{xx}} + ((\omega^2/c^2)\varepsilon_{xx})^2 + ((\omega^2/c^2)\varepsilon_{yx})^2} \times \left(\frac{f_y((ik_x - (\alpha_1 + \alpha_2))ik_y + \frac{\omega^2}{c^2}\varepsilon_{yx})}{+f_x((ik_x - (\alpha_1 + \alpha_2))^2 + \frac{\omega^2}{c^2}\varepsilon_{xx})} \right),$$

$$E'_{0y} = \frac{(4\pi i\omega n_0 e/c^2)}{(-k_y^2 + (ik_x - (\alpha_1 + \alpha_2))^2)(\omega^2/c^2)\varepsilon_{xx}} + ((\omega^2/c^2)\varepsilon_{xx})^2 + ((\omega^2/c^2)\varepsilon_{yx})^2 \times \left(f_x((ik_x - (\alpha_1 + \alpha_2))ik_y - \frac{\omega^2}{c^2}\varepsilon_{yx}) + f_y(-k_y^2 + \frac{\omega^2}{c^2}\varepsilon_{xx}) \right).$$

Therefore, general solution of Eq. (7) in the plasma $x \ge 0$ is

$$\vec{E}_{\rm II} = \begin{pmatrix} A_{\rm T}[\delta \hat{x} + \hat{y}] \\ + [E'_{0x} \hat{x} + E'_{0y} \hat{y}] \exp(-(\alpha_1 + \alpha_2)x) \end{pmatrix} \times \exp(-i[\omega t - k_x x - k_y y]).$$
(9)

 $A_{\rm R}$ and $A_{\rm T}$ are the constant coefficients. On applying the boundary conditions at x = 0, $(E_{\rm I})_y = (E_{\rm II})_y$ and $(\epsilon_{\rm IE_I})_x = (\epsilon_{\rm II}E_{\rm II})_x$. We obtain from Eqs (8) and (9)

$$A_{\rm R} = A_{\rm T} + E'_{\rm 0v} \tag{10}$$

and

$$A_{\rm R}\frac{k_{\rm y}}{k_{\rm x}} = \varepsilon_{\rm xx} \big[A_{\rm T} \delta + E'_{0\rm x} \big] - \varepsilon_{\rm yx} \big[A_{\rm T} + E'_{0\rm y} \big]. \tag{11}$$

From Eqs (10) and (11), the amplitude of generated THz wave in the reflected component is obtained as follows:

$$|A_{\rm R}| = \left| \frac{-\varepsilon_{xx} \delta E'_{0y} + \varepsilon_{xx} E'_{0x}}{k_y / k_x - \varepsilon_{xx} \delta + \varepsilon_{yx}} \right|.$$
(12)

4. THZ RADIATION EFFICIENCY

The efficiency of the emitted radiation is the ratio of the energy of THz radiation and the energy of the incident lasers. According to Rothwell and Cloud (2009) in general, the average electromagnetic energy stored per unit volume is given by the formula:

$$w_{\mathrm{E}i} = \frac{\varepsilon}{8\pi} \frac{\partial}{\partial \omega_i} \left[\omega_i \left(1 - \frac{\omega_\mathrm{p}^2}{\omega_i^2} \right) \right] \langle |E_i|^2 \rangle. \tag{13}$$

The energy densities of the incident lasers and THz radiation are evaluated as

$$\begin{split} w_{\text{pump}} &= \frac{\varepsilon}{8\pi} \frac{\partial}{\partial \omega_i} \left[\omega_i \left(1 - \frac{\omega_p^2}{\omega_i^2} \right) \right] \langle \left| E_{\text{pump}} \right|^2 \rangle \quad \text{and} \\ w_{\text{THz}} &= \frac{\varepsilon}{8\pi} \frac{\partial}{\partial \omega} \left[\omega \left(1 - \frac{\omega_p^2}{\omega^2} \right) \right] \langle \left| E_{\text{THz}} \right|^2 \rangle, \end{split}$$

respectively. Based on this and following the method used by

Malik *et al.* (2014), the efficiency of the THz radiation (η) is calculated as

$$\eta = \frac{w_{\text{THz}}}{w_{\text{pump}}} = \frac{\langle |E_{\text{THz}}|^2 \rangle}{\langle |E_{\text{pump}}|^2 \rangle} = \frac{1}{A_{10}^2} \left| \frac{-\varepsilon_{xx} \delta E'_{0y} + \varepsilon_{xx} E'_{0x}}{(k_y/k_x) - \varepsilon_{xx} \delta + \varepsilon_{yx}} \right|^2.$$
(14)

5. RESULTS AND DISCUSSION

We have used the following set of parameters $\lambda_1 = 9.6$, $\lambda_2 = 9.75 \,\mu\text{m}$, and $eA_{20}/\omega_1 mc = 0.003$. The typical parameters can be belonged to a CO2 laser. Plasma frequency supposed as $\omega_p = 2.25 \times 10^{14} \,\text{rad/s}$, which is corresponding to the electron density $n_0 = 1.6 \times 10^{19} \,\text{cm}^{-3}$. Critical density supposed as $n_c = 1.2 \times 10^{19} \,\text{cm}^{-3}$. In Figure 2, the normalized THz wave amplitude $|A_R/A_{10}|$ versus angle of incident lasers θ_i is plotted. As the figure shows, in the absence of magnetic field the normalized THz amplitude has a minimum about $\theta_i = 20^\circ$ and a maximum about $\theta_i = 70^\circ$. In the presence of a magnetic field, the form of curve roughly does not change, but the magnetic field increases generated THz amplitude for all angles of incident.

Figure 3 shows the variation of efficiency of THz radiation with normalized beating frequency for different values of magnetic field strength. From this figure it is clear that the effect of magnetic field gradually disappears in large beating frequency. Also by increasing of beating frequency the efficiency is decreasing, the similar behavior occurs in the underdense plasma (Malik *et al.*, 2014). This figure and Figure 4 illustrate that the present scheme of frequency-mixing of two laser beams in an overdense magnetized plasma is very effective. High efficiency can be obtained if



Fig. 2. Normalized THz amplitude $|A_R/A_{10}|$ versus angle of incident θ_i for different values of magnetic field strength.



Fig. 3. Variation of efficiency of THz radiation versus normalized beating frequency for different values of strength of magnetic field.

large angle of incident lasers and strong magnetic field are used. Figure 3 also shows that the efficiency of THz radiation from an overdense magnetized plasma is greater than the underdense plasma (Malik *et al.* 2010, 2012, 2014; Malik & Malik, 2011; Bakhtiari *et al.* 2015*a*, *b*). Malik and Singh (2015) have proposed THz radiation generation by beating of two super-Gaussian lasers in rippled density plasma and realized the efficiency about 0.25 for an applied magnetic field about 60 kG, where the present scheme can be realized efficiency about 0.27 for the applied magnetic field about 50 kG.



Fig. 4. Efficiency of THz radiation versus angle of incident θ_i for different values of strength of magnetic field, when $\omega/\omega_p = 0.01338$.

6. CONCLUSION

We have presented a scheme for THz generation based on nonlinear mixing of two obliquely incident laser beams on an overdense magnetized plasma. It is investigated that the amplitude and efficiency of the THz wave increases with increasing of magnetic field also THz wave amplitude can be optimized at a particular angle which occurred in large incident angle of lasers. Our analytical investigations show that this scheme is quite effective for getting the strong THz radiation and the efficiency of THz radiation from an overdense magnetized plasma is greater than the underdense plasma. A natural extension for future works is to include collision into this scheme.

ACKNOWLEDGMENT

Authors thank members of Department of Physics, Iran University of Science & Technology for their helpful discussion.

REFERENCES

- ADAK, A., ROBINSON, A.P.L., SINGH, P.K., CHATTERJEE, G., LAD, A.D., PASLEY, J. & KUMAR, G.R. (2015). Terahertz acoustics in hot dense laser plasmas. *Phys. Rev. Lett.* (*PRL*) **114**, 115001.
- ALIEV, Y.M., FROLOV, A.A., BRODIN, G. & STENFLO, L. (1993). Total backward reflection of electromagnetic radiation due to resonant excitation of surface waves. *Phys. Rev. E* 47, 4623.
- ANTONSEN, T.M., PALASTRO, J. & MICHBERG, H.M. (2007). Excitation of terahertz radiation by laser pulses in nonuniform plasma channels. *Phys. Plasma* 14, 033107.
- BAKHTIARI, F., GOLMOHAMADY, S., YOSEFI, M., KASHANI, F. & GHAF-ARY, B. (2015*a*). Generation of terahertz radiation in collisional plasma by beating of two dark hollow laser beams. *Laser Part. Beams* 33, 463–472.
- BAKHTIARI, F., YOSEFI, M., GOLMOHAMADY, S., JAZAAYERI, S.M. & GHAFARY, B. (2015b). Generation of terahertz radiation by beating of two circular flat-topped laser beams in collisional plasma. *Laser Part. Beams* 33, 713–722.
- BARTMAN, V.L., LITVAK, A.G. & SUVOROV, E.V. (2011). Mastering the terahertz domain: Sources and applications. *Phys. – Usp.* 54, 837.
- BITTENCOURT, J.A. (2004). Fundamentals of Plasma Physics. 3rd edn. New York: Springer-Ver1ag.
- BULANOV, S.V., CALIFANO, F., DUDNIKOVA, G.I., ZH. ESIRKEPOV, T., INOVENKOV, I.N., KAMENETS, F.F., LISEIKINA, T.V., LONTANO, M., MIMA, K., NAUMOVA, N.M., NISHIHARA, K., PEGORARO, F., RUHL, H., SAKHAROV, A.S., SENTOKU, Y., VSHIVKOV, V.A. & ZHAKHOVSKII, V.V. (2001). Relativistic interaction of laser pulses with plasmas. In *Reviews of Plasma Physics* (Shafranov, V.D., Ed.), Vol. 22, pp. 227–335. New York: Kluwer Academic/Consultants Bureau.
- CHAUHAN, S. & PARASHAR, J. (2014). Laser beat wave excitation of terahertz radiation in a plasma slab. *Phys. Plasmas* 21, 103113.
- CHEN, Z., ZHOU, X., WERLEY, C.A. & NELSON, K.A. (2011). Generation of high power tunable multicycle teraherz pulses. *Appl. Phys. Lett.* **99**, 071102.
- CHEN, Z.Y., LI, X.Y. & YU, W. (2013). Intense terahertz emission from relativistic circularly polarized laser pulses interaction with overdense plasmas. *Phys. Plasmas* 20, 103115.

- COOKE, D.G. & JESPEN, P.U. (2009). Dynamic optically induced planar terahertz quasioptics. *Appl. Phys. Lett.* **94**, 241118.
- FAURE, J., TILBORG, J.V., KANIDAL, R.A. & LEEMANS, W.P. (2004). Modelling laser-based table-top THz sources: Optical rectification, propagation and electro-optic sampling. *Opt. Quantum Electron.* 36, 681.
- FEDELE, R., ANGELIS, U.D. & KATSOULEAS, T. (1986). Generation of radial fields in the beat-wave accelerator for Gaussian pump profiles. *Phys. Rev. A* 33, 4412–4414.
- GOPAL, A., MAY, T., HERZER, S., REINHARD, A., MINARDI, S., SCHU-BERT, M., DILLNER, U., PRADARUTTI, B., POLZ, J., GAUMNITZ, T., KALUZA, M.C., JÄCKEL, O., RIEHEMANN, S., ZIEGLER, W., GE-MUEND, H.-P., MEYER, H.-G. & PAULUS, G.G. (2012). Observation of energetic terahertz pulses from relativistic solid density plasmas. *New J. Phys.* 14, 083012 (11 pp).
- HAMSTER, H., SULLIVAN, A., GORDON, S., WHITE, W. & FALCONE, R.W. (1993). Subpicosecond, electromagnetic pulses from intense laser-plasma interaction. *Phys. Rev. Lett.* **71**, 2725.
- HANGYO, M., MIGITA, M. & NAKAYAMA, K. (2001). Magnetic field and temperature dependence of terahertz radiation from InAs surfaces excited by femtosecond laser pulses. *J. Appl. Phys.* **90**, 3409.
- HASHIMSHONY, D., ZIGLER, A. & PAPADOPOULOS, K. (1999). Generation of tunable far-infrared radiation by the interaction of a superluminous ionizing front with an electrically biased photoconductor. *Appl. Phys. Lett.* **74**, 1669–1671.
- JEPSEN, P.U., JACOBSEN, R.H. & KEIDING, S.R. (1996). Generation and detection of terahertz pulses from biased semiconductor antennas. J. Opt. Soc. Amer. B 13, 2424–2436.
- KIM, K.W., KIM, H., PARK, J., HAN, J.K. & SON, J.H. (2012). Terahertz tomographic imaging of transdermal drug delivery. *IEEE Trans. Terahertz Sci. Technol.* 2, 99.
- KUMAR, M., TRIPATHI, K.V. & JEONG, Y. (2015). Laser driven terahertz generation in hot plasma with step density profile. *Phys. Plasmas* 22, 063106.
- LEE, Y.S., MEADE, T., PERLIN, V., WINFUL, H., NORRIS, T.B. & GAL-VANAUSKAS, A. (2000). Generation of narrow-band terahertz radiation via optical rectification of femtosecond pulses in periodically poled lithium niobate. *Appl. Phys. Lett.* **76**, 2505–2507.
- LI, C., ZHOU, M.-L., DING, W.-J., DU, F., LIU, F., LI, Y.-T., WANG, W.-M., SHENG, Z.-M., MA, J.-L., CHEN, L.-M., LU, X., DONG, Q.-L., WANG, Z.-H., LOU, Z., SHI, S.-C., WEI, Z.-Y. & ZHANG, J. (2011). Effects of laser-plasma interactions on terahertz radiation from solid targets irradiated by ultrashort intense laser pulses. *Phys. Rev. E* 84, 036405.
- LI, Y.T., LI, C., ZHOU, M.L., WANG, W.M., DU, F., DING, W.J., LIN, X.X., LIU, F., SHENG, Z.M., PENG, X.Y., CHEN, L.M., MA, J.L., LU, X., WANG, Z.H., WEI, Z.Y. & ZHANG, J. (2012a). Strong terahertz radiation from relativistic laser interaction with solid density plasmas. *Appl. Phys. Lett.* **100**, 254101.

- LI, Y.-T., WANG, W.-M., CHUN, L. & SHENG, Z-M. (2012b). High power terahertz pulses generated in intense laser-plasma interactions. *Chin. Phys. B* 21, 095203.
- MALIK, A.K., MALIK, H.K. & KAWATA, S. (2010). Investigations on terahertz radiation generated by two superposed femtosecond laser pulses. J. Appl. Phys. 107, 113105-1–113105-9.
- MALIK, A.K., MALIK, H.K. & STROTH, U. (2012). Terahertz radiation generation by beating of two spatial-Gaussian lasers in the presence of a static magnetic field. *Phys. Rev. E* **85**, 016401-1–016401-9.
- MALIK, A.K. & SINGH, K.P. (2015). High-intensity terahertz generation by nonlinear frequency-mixing of lasers in plasma with DC magnetic field. *Laser Part. Beams* 33, 519–524.
- MALIK, A.K., SINGH, K.P. & SAJAL, V. (2014). Highly focused and efficient terahertz radiation generation by photo-mixing of lasers in plasma in the presence of magnetic field. *Phys. Plasmas* 21, 073104.
- MALIK, H.K. & MALIK, A.K. (2011). Tunable and collimated terahertz radiation generation by femtosecond laser pulses. *Appl. Phys. Lett.* **99**, 251101-1–251101-3.
- MCLAUGHLIN, R., CORCHIA, A., JOHNSTON, M.B., CHEN, Q., CIESLA, C.M., ARNONE, D.D., JONES, G.A.C., LINFIELD, E.H., DAVIES, A.G. & PEPPER, M. (2000). Enhanced coherent terahertz emission from indium arsenide in the presence of a magnetic field. *Appl. Phys. Lett.* **76**, 2038.
- MIGITA, M. & HANGYO, M. (2001). Pump-power dependence of THz radiation from InAs surfaces under magnetic fields excited by ultrashort laser pulses. *Appl. Phys. Lett.* **79**, 3437.
- PARASHAR, J. (2014). Terahertz Radiation Generation by beating two obliquely incident lasers on a Plasma with Density Gradient. 39th Int. Conf. on Infrared, Millimeter, and Terahertz waves (IRMMW-THz) 14771076, Tucson, AZ.
- PARASHAR, J., MISHRA, E. & MAHAJAN, S.K. (2013). Generation of terahertz radiation by nonlinear mixing of two laser beams in overdense plasma. *Indian J. Phys.* 87, 699–703.
- ROTHWELL, E.J. & CLOUD, M.J. (2009). *Electromagnetic*. Boca Raton: CRC Press, Taylor and Francis Group.
- SHENG, Z.M., MIMA, K., ZHANG, J. & SANUKI, H. (2005). Emission of electromagnetic pulses from laser wakefields through linear mode conversion. *Phys. Rev. Lett.* 94, 095003.
- SHVARTSBURG, A.B. & STENFLO, L. (1994). Reflection of wideband electromagnetic pulses at a plasma boundary. *Phys. Scr.* 49, 712.
- TAO, H., PADILLA, W.J., ZHANG, X. & AVERITT, R.D. (2011). Recent progress in electromagnetic metamaterial devices for terahertz applications. *IEEE J. Sel. Top. Quantum Electron.* 17, 92.
- VODOPYANOV, K.L. (2008). Optical THz-wave generation with periodically inverted GaAs. *Laser Photon. Rev.* 2, 11–25.
- WEISS, C., WALLENSTEIN, R. & BEIGANG, R. (2000). Magnetic-field-enhanced generation of terahertz radiation in semiconductor surfaces. *Appl. Phys. Lett.* 77, 4160.
- WU, H.C., SHENG, Z.M., DONG, Q.L., XU, H. & ZHANG, J. (2007). Powerful terahertz emission from laser wakefields in inhomogeneous magnetized plasmas. *Phys. Rev. E*, **75**, 016407-1–016407-7.