

THE BULLETIN OF SYMBOLIC LOGIC

Edited by

James Cummings, *Managing Editor*

Matthias Baaz

Ali Enayat

Guram Bezhanishvili

Leonid Libkin

Katalin Bimbó

Øystein Linnebo

Paola D'Aquino

Arno Pauly

Peter Dybjer

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Nam Trang

Thesis Abstracts Editor

Christian Rosendal

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Editors

James Cummings (Managing Editor), Department of Mathematical Sciences, Carnegie Mellon University, Wean Hall 6113, Pittsburgh, PA 15213, USA

jcumming@andrew.cmu.edu

Matthias Baaz, Institute for Discrete Mathematics and Geometry, Vienna University of Technology, Weidner hauptstrasse 8-10, 1040 Vienna, Austria

baaz@logic.at

Guram Bezhanishvili, New Mexico State University, New Mexico, USA

Katalin Bimbó, University of Alberta, Alberta, Canada

bimbo@ualberta.ca

Paola D'Aquino, Department of Mathematics and Physics, Università della Campania "L. Vanvitelli", viale Lincoln 5, Caserta 81100, Italy

paola.daquino@unia2.it

Peter Dybjer, Department of Computer Science and Engineering, Chalmers University of Technology, SE 412 96 Göteborg, Sweden

peterd@chalmers.se

Ali Enayat, Department of Philosophy, Linguistics, and Theory of Science, University of Gothenburg, Box 200, SE 405 30, Gothenburg, Sweden

ali.enayat@gu.se

Leonid Libkin, Laboratory for Foundations of Computer Science, University of Edinburgh, Informatics Forum, IF 5.33, Crichton Street, Edinburgh, EH8 9AB, UK

libkin@inf.ed.ac.uk

Øystein Linnebo, Department of Philosophy, IFIKK, 0315 Oslo, Norway

oystein.linnebo@ifikk.uio.no

Arno Pauly, Swansea University, Wales

arno.m.pauly@gmail.com

Reviews editors

Graham Leach-Krouse (Managing Editor), Kansas State University, Kansas, USA, gkrouse@ksu.edu

Albert Atserias atserias@cs.upc.edu,

Mark van Atten mark.vanatten@univ-paris1.fr,

Benno van den Berg bennovdberg@gmail.com,

Clinton Conley clintonc@andrew.cmu.edu

Bradd Hart hartb@mcmaster.ca,

Dugald Macpherson pmthdm@maths.leeds.ac.uk,

Antonio Montalbán antonio@math.berkeley.edu,

Christian Retoré christian.retore@limm.fr

Marion Scheepers mscheepe@boisestate.edu, and

Nam Trang namtrang35@gmail.com.

Thesis abstracts editor

Christian Rosendal rosendal@umd.edu

Articles present topics of broad interest in a way that is accessible to a large audience. They can be purely expository, survey, or historical articles or they may contain, in addition, new ideas or results or new approaches to old ones.

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