Studies of the fast ion confinement in the Large Helical Device by using neutron measurement and integrated codes

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(Received 31 January 2020; revised 7 May 2020; accepted 11 May 2020)

The neutral beam (NB) fast ion confinement in the Large Helical Device (LHD) is studied for several full field ($B_t \sim 2.75$ T) magnetic configurations by a combination of neutron measurement and simulations. To investigate the NB fast ion confinement, we have performed a series of short-pulse NB injection experiments. The experiment results are analysed by the integrated code TASK3D-a. From this investigation, the effective particle diffusion coefficients of the tangential and perpendicular NBs are approximately $D^{\text{eff}} \sim 0.1 \text{ m}^2 \text{ s}^{-1}$ and $D^{\text{eff}} \sim 1 \text{ m}^2 \text{ s}^{-1}$ in the standard configuration. It is clarified that the NB fast ion confinement improves when the plasmas are shifted inward. Moreover, it is also found that the simulation, which considers the deuteron dilution effect due to the presence of impurity ions, can describe a neutron emission rate consistent with the measurement.

Key words: fusion plasma, plasma confinement, plasma heating

1. Introduction

Generally, the temperature of fusion plasmas is sustained by the external heating. The heatings are achieved by the kinetic energy transfer from fast particles to the bulk plasma through Coulomb collisions. Additionally, in future fusion power plants, fusion plasmas will mainly be sustained by fusion-born α particles, which have 3.5 MeV kinetic energy. Therefore, fast particles should be confined until their velocities are decelerated to the plasma thermal velocity. For this reason, the fast particle confinement is one of the most important issues (Heidbrink & Sadler 1994; Gorelenkov, Pinches & Toi 2014) for magnetically confined fusion devices.

There are several diagnostics systems to investigate the fast particle physics (Gorelenkov *et al.* 2014), such as the neutral particle analyser (Medley & Roquemore 1998; Osakabe *et al.* 2006; Kamio *et al.* 2019), fast ion D_{α} spectroscopy (FIDA) (Luo, Heidbrink & Burrell 2004; Heidbrink *et al.* 2007), fast ion loss detector (Darrow *et al.* 1995; Ogawa *et al.* 2010) and neutron spectroscopy (Adams *et al.* 1993; Ishikawa *et al.* 2007). Because the deuterium plasma experiment campaign began in

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the Large Helical Device (LHD) (Osakabe *et al.* 2017, 2018; Takeiri 2018*a,b*) from March 2017, the investigation of fast ion behaviour using neutron diagnostics (Isobe *et al.* 2018; Ogawa *et al.* 2019) and FIDA (Fujiwara *et al.* 2019) have been enabled in LHD.

In LHD deuterium plasmas, ~2.45 MeV fast neutrons are yielded owing to the deuterium-deuterium (DD) fusion reaction. Because of the high injection energy of neutral beams of up to $E_b \sim 180$ keV, most of the neutrons are generated by the fusion reaction between fast deuteron and thermal deuteron instead of the reaction between thermal ions (Osakabe *et al.* 2017). This is the so-called 'beam-thermal' fusion reaction. In such cases, we can study the fast ion global confinement from the neutron emission rate S_n . This is because the DD fusion reactivity increases monotonically with their relative kinetic energy up to $E \sim 2$ MeV. If the plasma temperature and density are constant in time, the decrement of the neutron emission rate comes from the decrement of the fusion cross-section due to the fast ion deceleration and the decrement of the fast ion density. Because the fast ion deceleration can be estimated by simulations, we can estimate the fast ion confinement from the neutron measurement without simulating the fast ion transport, which is usually too complex to estimate accurately.

We have studied the effective confinement time of NB fast ions in LHD using neutron measurement in this paper. There are several previous works that investigated fast ion confinement through the neutron diagnostics. Earliest works in tokamaks (Strachan et al. 1981; Heidbrink, Kim & Groebner 1988; Heidbrink et al. 1991) showed that the classical collisional slowing down model can explain the neutron emission with good agreement. The following investigation in the JT-60U tokamak (Tobita et al. 1994) reported a deviation from the classical collisional slowing down model due to the toroidal field ripple for perpendicular NB. Anomalous fast ion losses, which cannot be explained by the toroidal field ripple, were observed on TFTR (Ruskov et al. 1999). Moreover, fast ion confinement was investigated by using neutron measurement also in various types of magnetically confinement device, such as the reversed field pinch devices (Fiksel et al. 2005; Anderson et al. 2014), the spherical tokamak (Heidbrink et al. 2003), the tokamak (Zhang et al. 2012) and the stellarator and heliotron (Isobe et al. 2001; Nuga et al. 2019), In our previous work (Nuga et al. 2019), we have reported the NB fast ion confinement time by using neutron measurement for a single magnetic configuration in LHD. In this paper, we investigate the dependence of the fast ion confinement on the magnetic configuration and discuss the contribution of the charge exchange loss to the fast ion confinement, especially in low electron density plasmas.

The rest of this paper consists of the following. The detail of the experimental scenario and devices are provided in § 2. Simulation tools and models used in this paper are introduced in § 3. The results of the analyses to estimate the fast ion confinement time are shown in §§ 4 and 5. The dilution effect of the deuteron density due to the presence of impurity ions is discussed in § 6. Section 7 concludes this paper.

2. Experimental set-up

2.1. Experimental scenario

A series of experiments which use short-pulse NB injection have been performed in LHD to investigate the fast ion confinement time. The decay time of S_n , yielded by the DD fusion reaction has been observed after short-pulse NBs have been turned off.



FIGURE 1. Typical waveform of this series of experiments (SN148442) is displayed. The NB port through power in each beam, the plasma temperature and density at the position where the normalized minor radius, $\rho = 0.5$, and the neutron emission rate are shown.

In the previous work (Nuga *et al.* 2019), we performed the short-pulse NB experiment in a single magnetic configuration ($R_{ax} = 3.6$ m, $B_t = 2.75$ T), where R_{ax} and B_t indicate the position of the magnetic axis and the strength of the magnetic field on the magnetic axis. The direction of the magnetic field is counter-clockwise in the top view. In this paper, we have performed the short-pulse NB experiment in five magnetic configurations, (R_{ax} , B_t) = (3.53 m, 2.80 T), (3.55 m, 2.79 T), (3.60 m, 2.75 T), (3.75 m, 2.64 T) and (3.90 m, 2.54 T), respectively. A typical waveform of this series of experiments is shown in figure 1. The NB pulse width is ~40 ms in each beam.

In this series of experiments, the fast ion confinement time, τ_c , is assumed to be

$$\tau_c^{-1} = \tau_n^{-1} - (\tau_n^{\rm cl})^{-1}, \tag{2.1}$$

where τ_n is the neutron decay time after NB has been turned off and τ_n^{cl} is the *e*-folding time of the neutron decay rate due to the classical fast ion deceleration. This is because the reduction of the neutron emission rate is caused by the decrease of the fusion cross-section due to the deceleration and the decrease of the fast ion loss. Because the contribution of the fast ion loss is ignored in the estimation of τ_n^{cl} , τ_c can be estimated from τ_n and τ_n^{cl} . In this paper, τ_n can be obtained from the experimental results and τ_n^{cl} can be obtained from the simulation results instead of the analytical solution given by Strachan *et al.* (1981). The method of simulation will be introduced in § 3.

2.2. Experiment apparatus

In this series of experiments, two external heating systems, electron cyclotron heating (ECH) and neutral beam injection (NBI), are used. Plasmas are sustained by 3.5 MW ECH.

The top view of the NBI system in LHD (Takeiri *et al.* 2010) is shown in figure 2. The typical injection energy and power in each beam is also displayed. In LHD, there are three negative ion-based tangential NBs and two positive ion-based perpendicular NBs. The directions of NB#1 and NB#3 are co-directions to the magnetic field and the direction of NB#2 is counter-direction to the magnetic field. It is noted that



FIGURE 2. Top view of NBI system in LHD. There are three tangential beams, NB#1, NB#2 and NB#3, and there are two perpendicular beams, NB#4 and NB#5. Because the direction of the magnetic field line is counter-clockwise, NB#1 and NB#3 are the co-directions to the magnetic field line.

the injection energy of NB#4 is set to the untypically low energy, $E_b \sim 35$ keV, to investigate the dependence of the perpendicular NBs on the injection energy.

Experiments have been performed with five magnetic configurations as noted in § 2.1. The averaged plasma minor radius, which depends on the position of the magnetic axis, is approximately 0.58–0.63 m.

LHD is equipped with several diagnostic systems (Kawahata *et al.* 2010). In this paper, we have mainly used electron temperature and density profiles, the ion ratio among protons, deuterons and helium ions, and the time evolution of the neutron emission rate. The Thomson scattering diagnostic is used for the measurement of the electron density and temperature (Narihara *et al.* 2001; Yamada *et al.* 2010). A fast-response wide dynamic range neutron flux monitor (NFM) (Isobe *et al.* 2018) is equipped in LHD to measure the neutron emission rate.

3. Simulation tools

Estimation of τ_n^{cl} is required to evaluate τ_c as shown in (2.1). Although there is an analytical expression for τ_n^{cl} (Strachan *et al.* 1981), we use the following simulations to include the plasma profiles, plasma volume and NB birth profile for the estimation of τ_n^{cl} .

In this paper, the neutron emission simulations have been performed by the combination among VMEC (Hirshman & Whitson 1983), FIT3D (HFREYA and MCNBI) (Murakami, Nakajima & Okamoto 1995; Sato *et al.* 2008; Vincenzi *et al.* 2016; Seki *et al.* 2019) and CONV_FIT3D (Nuga *et al.* 2019), which are included in the integrated transport analysis suite TASK3D-a (Yokoyama *et al.* 2017). The flow of the simulations are displayed in figure 3. Three-dimensional magnetic equilibrium is calculated by the VMEC code. According to the obtained magnetic configuration, FIT3D calculates the NB fast ion birth profile. At this step, NB fast ion orbits are followed for a few tens of micro-seconds by using the Monte Carlo



FIGURE 3. Flow of the simulations to obtain the time evolution of the neutron emission rate.

method to consider the NB fast ion prompt loss effect. In this process, the effect of the birth profile broadening owing to the deviation of the NB fast ion drift orbit from the magnetic surface is also considered. Moreover, for positive ion-based NBs, the full, half and one-third energy fractions of injected neutral particles are assumed to be 0.78, 0.16 and 0.06, respectively. Although these values are the typical values of perpendicular NBI systems in LHD, they are not reliable for NB#4. This is because NB#4 has an untypically low injection energy in the following analyses. CONV FIT3D solves the NB fast ion slowing down equation to obtain the energy distribution of NB fast ions. Here, the fast ion transport across the magnetic surface during the slowing down process is neglected. In LHD, the beam-thermal fusion reaction is dominant instead of the reaction between thermal ions due to the insufficient plasma temperature. Additionally, in this paper, the fusion reaction between NB fast ions is also negligible. Therefore, it is enough to consider the fusion reaction between NB fast ions and thermal ions in this paper. Because it can be considered that the velocity distribution of thermal ions is isotropic, the velocity direction of NB fast ions is not necessary for the estimation of the fusion reaction rate. For this reason, CONV_FIT3D, which can obtain the energy distribution of NB fast ions, can estimate the neutron emission rate. The details of CONV_FIT3D are introduced in $\S 3.1$.

3.1. CONV_FIT3D

CONV_FIT3D is a code solving the fast ion slowing down equation based on the classical Coulomb collision theory. In the previous work (Nuga *et al.* 2019), we had chosen the model which assumes the NB fast ion velocity $v_{\rm EP}$ is sufficiently faster than the thermal ion velocity $v_{\rm th}$. However, in this paper, we have a perpendicular NB#4, which has an injection energy of $E_b = 35$ keV. NB fast ions, whose kinetic energy is 35 keV, cannot satisfy the assumption $v_{\rm EP} \gg v_{\rm th}$ because the typical temperature of this series of experiments is a few keV. Therefore, we have refined the slowing down

equation based on equation (30c) in Karney (1986). This model assumes a background Maxwellian. The refined equations are expressed as below

$$\frac{\mathrm{d}E}{\mathrm{d}t} = -\frac{2}{\tau_{se}} Z_{\rm EP}^2 E \\ \times \left[1 + \frac{3\pi^{1/2} m_{\rm EP}^{3/2} T_e^{3/2}}{4m_e^{1/2}} \left(\sum_i \frac{n_i Z_i^2}{n_e m_i} g(u_i) \right) \frac{1}{E^{3/2}} \right],$$
(3.1)

$$g(u_i) = \operatorname{erf}(u_i) - u_i \operatorname{erf}'(u_i), \qquad (3.2)$$

$$\tau_{se} = \frac{3(2\pi)^{3/2} \epsilon_0^2 m_{\rm EP} T_e^{3/2}}{n_e e^4 m_e^{1/2} \ln \Lambda},\tag{3.3}$$

$$\operatorname{erf}(u) = \frac{2}{\pi} \int_0^u \exp(-x^2) \,\mathrm{d}x,$$
 (3.4)

$$\operatorname{erf}'(u) = \frac{2}{\pi} \exp(-u^2),$$
 (3.5)

where τ_{se} is the Spitzer slowing down time on electrons, $u_i = v/\sqrt{2}v_{\text{th},i}$ and $v_{\text{th}} = \sqrt{T_i/m_i}$. In the following calculation, we assume that the ion temperature T_i is equal to the electron temperature T_e . In actuality, however, it is expected that T_e is greater than T_i because the plasmas are sustained by ECH.

As noted above, in LHD, the beam-thermal fusion reaction is dominant. In this case, the fusion reaction rate can be expressed as

$$\mathcal{R}_{bt} = n_D \int \langle \sigma v \rangle_{bt} (T_i, E_{EP}) f_{EP}(\boldsymbol{v}_{EP}) \,\mathrm{d}\boldsymbol{v}_{EP}, \qquad (3.6)$$

where n_D is the deuteron density in the bulk plasma. The beam-thermal reactivity $\langle \sigma v \rangle_{bt}$, which is derived by Mikkelsen (Mikkelsen 1989), is implemented in CONV_FIT3D. The fitting coefficients used in the expression of $\langle \sigma v \rangle_{bt}$ are chosen from Bosch & Hale (1992).

4. Analysis results for tangential beams

In figure 4, the example of the simulated neutron emission rate is shown with the measured neutron emission rate. The solid curve is the measured neutron emission rate and the dashed curve is the simulated neutron emission rate. The simulation overestimates the neutron emission rate due to the assumptions that $n_D = n_e$ and $\tau_c = \infty$. From measured and simulated neutron emission rates, we can estimate τ_n and τ_n^{cl} by using the least mean square fitting. The fitting functions are $f(t) = S_n^{p,exp} \exp(-t/\tau_n)$ for the measured decay rate and $f(t) = S_n^{p,sim} \exp(-t/\tau_n^{cl})$ for the simulated neutron emission rates. The durations used for these fittings are defined as the times when the neutron emission rates decay to $S_n^{p,exp}/e$ and $S_n^{p,sim}/e$, respectively.

Similar experiments have been performed with the same magnetic configuration $(R_{ax} = 3.53 \text{ m}, B_t = 2.8045 \text{ T})$ and different plasma parameters to survey the dependence of τ_n on τ_n^{cl} . It is noted that the control parameter is the electron density n_e in these experiments. Additionally, because the plasma heating power is constant in each shot, the electron temperature T_e also changes with the electron density.



FIGURE 4. Example of the neutron emission simulation assuming $n_D = n_e$ and $\tau_c = \infty$.



FIGURE 5. The experimentally measured neutron decay times are plotted against the simulated neutron decay time for tangential NBs in the configuration of $R_{\rm ax} = 3.53$ m. Dashed guide curve is $\tau_n = \tau_c \tau_n^{\rm cl} / (\tau_n^{\rm cl} + \tau_c)$, $\tau_c = 0.53$ s.

Figure 5 is obtained from experiment and simulation results for three tangential NBs. Their injection energies are also displayed in figure 5. In this figure, the x axis denotes the simulated neutron decay time τ_n^{cl} and the y axis denotes the experimental neutron decay time τ_n . The y error-bars shown in figure 5 denote the standard deviation of τ_n . The solid guideline indicates y = x. If the NB fast ions are confined perfectly, plots obey this guide line. Actually, because the NB fast ion loss is not ignorable, plots separate from the guide line as shown in figure 5. Additionally, in figure 5, there is a dashed guide curve which indicates $\tau_n = 0.53\tau_n^{\rm cl}/(\tau_n^{\rm cl} + 0.53)$. The reason for the value $\tau_c = 0.53$ s is explained later. From figure 5, it is found that a different trend, which does not obey the dashed guide curve, appears in the $\tau_n^{cl} > 0.4$ s region. This means that the dominant transport mechanism is different between the $\tau_n^{cl} < 0.4$ s region and the $\tau_n^{cl} > 0.4$ s region. It is noted that the high frequency (>10 kHz) magneto-hydro-dynamics (MHD) instabilities triggered by NBI hardly appeared in the short τ_n^{cl} region. On the contrary, in the long τ_n^{cl} region, NB fast ion driven instabilities were observed in several discharges. Therefore, we can ignore the anomalous transport due to fast ion driven instabilities in the short τ_n^{cl} region. The following analyses in the long τ_n^{cl} region may include the anomalous transport. The low frequency (<10 kHz) MHD instabilities excited by bulk plasma pressure were observed through this series of experiments. The typical amplitude of the low frequency magnetic fluctuation, which is detected by a magnetic probe set



FIGURE 6. The dependence of the inverse of the charge exchange reactivity $1/\langle \sigma v \rangle_{cx}$ on beam energy is shown. Here, it is assumed that the velocity of neutral atoms is negligible.

on the vacuum vessel, was $\delta B/B_t < 2 \times 10^{-5}$. This value is sufficiently low compared to the case where the low frequency magnetic fluctuation plays an important role in the NB fast ion loss (Ogawa *et al.* 2010). Therefore, it can be considered that the NB fast ion loss due to the low frequency fluctuation is negligible.

4.1. Long τ_n^{cl} region ($\tau_n^{cl} > 0.4$ s)

In LHD plasmas, it is known that the neutral atom density in the plasma core region has a negative n_e dependence (Goto *et al.* 2011, 2016; Fujii *et al.* 2015) because the penetration of neutral atoms into the plasma core increases with the decrease of the plasma density. Therefore, it can be considered that the neutral atom density in the plasma core region in $\tau_n^{cl} > 0.4$ s region is higher than that in $\tau_n^{cl} < 0.4$ s region. Here we focus on the $\tau_n^{cl} > 0.4$ s region to investigate the contribution of the charge exchange loss to the fast ion loss.

From figure 5, it is found that the values of τ_n for NB#1, NB#2 and NB#3 are approximately $\tau_n \sim 0.25$ s, 0.2 s and 0.2 s at $\tau_n^{cl} = 1$ s. Here we assume that the separation from the dashed guide curve in the long τ_n^{cl} region can be described only by the charge exchange loss. In this assumption, the neutron decay time τ_n can be expressed as

$$\tau_n^{-1} = (\tau_n^{\rm cl})^{-1} + (\tau_c^{\rm eff})^{-1} + \tau_{\rm cx}^{-1}, \tag{4.1}$$

where τ_c^{eff} is the effective confinement time in the short τ_n^{cl} region and τ_{cx} is the charge exchange time. In this configuration, the value of τ_c^{eff} , which will be obtained in § 4.2, is $\tau_c^{\text{eff}} = 0.53$ s. For these assumptions and estimations, the charge exchange times for NB#1, NB#2 and NB#3 are approximately $\tau_{\text{cx}} = 0.90$ s, 0.47 s and 0.47 s, respectively.

The dependence of the charge exchange reactivity on the beam energy is shown in figure 6. Although fast ions in plasmas have a velocity distribution, we estimate the charge exchange reactivity $\langle \sigma v \rangle_{cx}$ in each beam from the beam injection energy. This is because that we have discussed the fast ion confinement through the measurement of the neutron emission rate, which exponentially depends on the beam energy within the range of the NB injection energy. Accordingly, the charge exchange time can be expressed as $\tau_{cx}^{-1} = n_0 \langle \sigma v \rangle_{cx}(E_b)$, where n_0 is the neutral atom density. From this expression, we can estimate the values of n_0 in each beam. The neutral atom densities, which are felt by fast ions from NB#1, NB#2 and NB#3, are $n_0 = 1.7 \times 10^{14} \text{ m}^{-3}$, $1.9 \times 10^{14} \text{ m}^{-3}$ and $2.1 \times 10^{14} \text{ m}^{-3}$, respectively. In Goto *et al.* (2016), the neutral



FIGURE 7. The short τ_n^{cl} region ($\tau_n^{cl} < 0.4$ s) of figure 5 is focused.

atom density in the LHD plasma, whose electron density is $\sim 2 \times 10^{19} \text{ m}^{-3}$, is measured as approximately 10^{14} m^{-3} . Because the plasmas in the long τ_n^{cl} region have an electron density of approximately $n_e \lesssim 0.5 \times 10^{19} \text{ m}^{-3}$, it can be expected that the neutral density is larger than 10^{14} m^{-3} in these plasmas. Therefore, it can be considered that the estimation of n_0 is a realistic value and the charge exchange loss is not negligible in the long τ_n^{cl} region.

4.2. Short τ_n^{cl} region ($\tau_n^{\text{cl}} < 0.4 \text{ s}$)

Here, we focus on the region $\tau_n^{cl} < 0.4$ s of figure 5 to exclude the cases where the charge exchange loss is significant. The dashed guide curve in figure 7 is obtained by the weighted least mean square fitting in $\tau_n = \tau_n^{cl} \tau_c^{eff} / (\tau_n^{cl} + \tau_c^{eff})$. In this fitting, data in $\tau_n^{cl} > 0.4$ s region are omitted. It is noted that because three tangential NBs have a similar trend, they are fitted in a single curve. For this fitting, the effective fast confinement time in this region is obtained as $\tau_c^{eff} = 0.53$ s.

Similar analyses are performed for the different configurations shown in § 2.1. To compare the confinement among different magnetic configurations, the effective fast ion confinement time τ_c^{eff} is converted into the effective particle diffusion coefficient D^{eff} . The relation between τ_c^{eff} and D^{eff} is expressed as

$$D^{\rm eff} = \frac{a^2}{5.8\tau_c^{\rm eff}},\tag{4.2}$$

where *a* is the plasma minor radius. Here it is assumed that D^{eff} is uniform in the plasma and the plasma poloidal cross-section is not elongated. The R_{ax} dependence of D^{eff} is shown in figure 8. It is found that the fast ion confinement becomes poor when the plasma is shifted outward. Additionally, the absolute value of D^{eff} obtained in this paper is larger than that obtained in tokamaks (Tobita *et al.* 1994; Heidbrink *et al.* 1988).

5. Analysis results for perpendicular beams

Perpendicular beams are analysed by a method similar to the tangential beams. Figure 9 shows the relation between τ_n and $\tau_n^{\rm cl}$ for perpendicular NBs. The dashed guide curve indicates $\tau_n = 0.057 \tau_n^{\rm cl} / (\tau_n^{\rm cl} + 0.057)$. In figure 9, the different trends appear at approximately $\tau_n^{\rm cl} = 0.1$ s.



FIGURE 8. The effective particle diffusion coefficients are plotted against the position of the magnetic axis.



FIGURE 9. The experimentally measured neutron decay times are plotted against the simulated neutron decay time for perpendicular NBs in the configuration of $R_{ax} = 3.53$ m. Dashed guide curve is $\tau_n = \tau_c \tau_n^{cl} / (\tau_n^{cl} + \tau_c)$, $\tau_c = 0.057$ s.

5.1. Long τ_n^{cl} region $(\tau_n^{\text{cl}} > 0.1 \text{ s})$

Similar to § 4.1, we investigate the contribution of the charge exchange loss to the fast ion confinement. From figure 9, the neutron decay times of NB#4 and NB#5 at $\tau_n^{cl} = 0.2$ s are approximately $\tau_n = 0.025$ s and 0.035 s, respectively. From these values and (4.1), the charge exchange times of NB#4 and NB#5 can be estimated as $\tau_{cx} = 0.057$ s and 0.17 s, respectively. The neutral atom densities evaluated from τ_{cx} are $n_0 = 2.1 \times 10^{14}$ m⁻³, and 1.3×10^{14} m⁻³, respectively. These values of density are within the range of realistic values as noted in § 4.2. Therefore, it can be also considered that the charge exchange losses are not negligible for perpendicular beams in the long τ_n^{cl} region.

5.2. Short τ_n^{cl} region ($\tau_n^{cl} < 0.1$ s)

Owing to the above discussion, we focus on the $\tau_n^{cl} < 0.1$ s region to exclude the cases that the charge exchange loss is significant. In figure 10, the short τ_n^{cl} region $\tau_n^{cl} < 0.1$ s of figure 9 is focused on. The guide curve indicates $\tau_c^{eff} \tau_n^{cl} / (\tau_n^{cl} + \tau_c^{eff})$, $\tau_c^{eff} = 0.057$ s. The value of τ_c^{eff} is obtained by the weighted least mean square fitting in $\tau_n = \tau_c^{eff} \tau_n^{cl} / (\tau_n^{cl} + \tau_c^{eff})$.

Similar to the discussion in § 4.2, the effective particle diffusion coefficient D^{eff} for a perpendicular beam is estimated for the five magnetic configurations. In figure 11, the dependence of D^{eff} on R_{ax} for perpendicular beams is shown. It is found that the perpendicular beams have a poorer confinement than the tangential beams. As with



FIGURE 10. The short τ_n^{cl} region ($\tau_n^{cl} < 0.1$ s) of figure 9 is focused on.



FIGURE 11. The effective particle diffusion coefficients for perpendicular beams are plotted against the position of the magnetic axis.

tangential beams, the confinement of the perpendicular beams becomes poor when the plasmas are shifted outward.

It is noted that the perpendicular beam injection energy is not uniform in each configuration due to experimental constraints. In the cases of $R_{ax} = 3.75$ m and 3.9 m, the perpendicular beam injection energy is $E_b = 60$ keV. The data of the $R_{ax} = 3.6$ m configuration consist of the data with $E_b = 35$ keV, 60 keV and 80 keV. In the remaining configurations ($R_{ax} = 3.53$ m and 3.55 m), the data consist of those with $E_b = 35$ keV and 80 keV. These data are fitted in a single curve as shown in figure 10.

6. Discussion regarding the deuteron dilution

In this paper, in order to estimate the fast ion confinement time, we have focused on the neutron decay time instead of the absolute value of the neutron emission rate itself. This is because there are some ambiguities in estimating the absolute value of the neutron emission rate. The fusion reaction rate in beam-thermal reaction dominant plasmas is described by (3.6). Our simulation over-estimates the neutron emission rate due to the assumptions of $n_D = n_e$ and $\tau_c = \infty$ as shown in figure 4. In actual plasmas, however, deuterons are diluted due to the presence of impurity ions. Because the evaluation of the impurity density profile is difficult, the ambiguity cannot be reduced to estimate the neutron emission rate. On the other hand, the estimation of the neutron decay time has fewer ambiguities. This is because the fast ion slowing down process mainly depends on the measurable values, which are electron density n_e and temperature T_e . Since we have estimated the fast ion confinement time τ_c in the previous section, the diluted deuteron density can be evaluated by a comparison between the peak values of the measured and simulated neutron emission rates.



FIGURE 12. The relation between $S_n^{p,exp}$ and $\mathcal{F}S_n^{p,sim}$ is shown for the $R_{ax} = 3.53$ m configuration. The solid line indicates y = x and the dashed line indicates y = 0.42x.

The relation between two neutron emission rate peak values, measured peak value $S_n^{p,exp}$ and simulated peak value $S_n^{p,sim}$, can be expressed as (Nuga *et al.* 2019)

$$\frac{S_{n}^{p, exp}}{S_{n}^{p, sim}} = \frac{n_{D}}{n_{e}} \mathcal{F},
\mathcal{F} \equiv \frac{\tau_{c}}{\tau_{n}^{cl} + \tau_{c}} \frac{1 - \exp(-t_{0}/[\tau_{n}^{cl}\tau_{c}/(\tau_{n}^{cl} + \tau_{c})])}{1 - \exp(-t_{0}/\tau_{n}^{cl})},$$
(6.1)

where t_0 is the beam injection duration $t_0 \sim 40$ ms. Here, we assume that the plasma parameters and the fast ion birth rate are constant during beam injection.

Figure 12 shows the relation between $S_n^{p,exp}$ and $\mathcal{F}S_n^{p,sim}$ for the $R_{ax} = 3.53$ m configuration. It is noted that, in this figure, data in the long τ_n^{cl} region ($\tau_n^{cl} > 0.4$ s for tangential beams and $\tau_n^{cl} > 0.1$ s for perpendicular beams) are omitted. From equation (6.1), the slope of dashed line in figure 12 indicates the ratio of the deuteron density to the electron density n_D/n_e . The value is obtained by the weighted least mean square fitting in $y = \alpha x$, where α is the fitting parameter. For this reason, here we assume the deuteron density ratio to the electron density is approximately $n_D/n_e = 0.42$.

It is noted that this fitting is performed by using only tangential NBs. This is because the full energy fraction of perpendicular NBs is unclear. From figure 12, the plot of NB#5 has a good agreement with the fitting line. This indicates that the assumption of the full energy fraction, 0.78 used in the simulation is valid. On the contrary, results of NB#4 are separated from the fitting line. One of the reasons of this deviation is that the assumption of the full energy fraction, the fraction is invalid. If the deviation can be explained only by the full energy fraction, the fraction becomes 1.2. Therefore, it seems that there are the other factors separating the results from the fitting. In this paper, NB#4 has a low injection energy, whose value is out of the typical range of injection energy. Because of this unusual operation of NB#4, the S_n peak value estimation of NB#4 is not reliable.

The deuterium ion ratio and the helium ion ratio in this series of experiment are approximately $n_{\rm D}/(n_{\rm H} + n_{\rm D}) \sim 1$ and $(n_{\rm D} + n_{\rm H})/(n_{\rm D} + n_{\rm H} + n_{\rm He}) \sim 0.9$. Here, we assume that there are only three ion species, deuterons, helium ions and carbon ions in the plasmas. This assumption indicates $n_e = n_{\rm D} + 2n_{\rm He} + 6n_{\rm C}$. We can estimate the typical ion ratios from the deuteron ratio estimation, two measured ratios and this assumption. These ratios are $n_{\rm D}/n_e = 0.42$, $n_{\rm He}/n_e = 0.047$ and $n_{\rm C}/n_e = 0.081$. The effective charge of the plasma, which consists of these ion ratios, is approximately $Z_{\rm eff} = 3.5$.



FIGURE 13. The carbon density ratio to the electron density $n_{\rm C}/n_e$ is shown for three discharges. The horizontal axis indicates the normalized minor radius ρ . The minus value of ρ means the position inside the magnetic axis.



FIGURE 14. Time evolutions of the measured and simulated neutron emission rates are shown. The bulk deuteron density is assumed to be $n_D/n_e = 0.42$ and the fast ion confinement times are assumed to be $\tau_c = 0.6$ s for tangential beams and $\tau_c = 0.06$ s for perpendicular beams.

From Zhou *et al.* (2010) and Huang *et al.* (2015), the typical value of the effective charge in LHD plasmas measured by an extreme ultraviolet (EUV) spectrometer is approximately $Z_{\text{eff}} = 2-4$. Therefore, this estimation is within the range of the realistic value.

Additionally, the carbon density profile, $n_{\rm C}$, is measured by the charge exchange spectroscopy of CVI using the neutral beam (Chen *et al.* 2019; Ida *et al.* 2019) in LHD. Unlike $n_{\rm D}/(n_{\rm H} + n_{\rm D})$ and $(n_{\rm D} + n_{\rm H})/(n_{\rm D} + n_{\rm H} + n_{\rm He})$, the carbon density ratio to the electron density changes widely shot-by-shot as shown in figure 13. In most of the discharges, the value of n_C/n_e has changed around ≤ 0.1 and it does not exceed 0.2. Therefore, it can be considered that the value $n_D/n_e = 0.42$ is reasonable.

Here we can recalculate the neutron emission rate by using estimated τ_c and ion ratios. Figure 14 shows the time evolutions of the measured and simulated neutron emission rate. In this simulation, the dilution effect of deuteron density and the fast ion loss effect are included. As compared to figure 4, it is found that a consistent result for the measured neutron emission rate can be obtained by this simulation.

7. Conclusion

We have investigated the NB fast ion confinement in LHD deuterium plasmas in five magnetic configurations. The effective confinement time of NB fast ions has been estimated from the decay time of the neutron emission rate after short-pulse NBs are turned off. It can be considered that the decay of the neutron emission rate can be expressed by a combination of a reduction of the fusion cross-section due to the fast ions slowing down and the reduction of the fast ion density due to the fast ion loss. Therefore, the comparison between the simulated neutron decay time τ_n^{cl} , which ignores the fast ion loss, and the measured neutron decay time τ_n clarifies the fast ion confinement time.

As shown in figures 5 and 9, the relation between τ_n and τ_n^{cl} has two trends. In the short τ_n^{cl} region, τ_n obeys the curve, $f(\tau_n^{cl}) = \tau_c \tau_n^{cl} / (\tau_n^{cl} + \tau_c)$, where τ_c is constant. In other words, this region is the high electron density region. On the other hand, τ_n separates from the guide curve as τ_n^{cl} increases. This indicates that the dominant fast ion loss mechanism is different in each region. As shown in §§ 4 and 5, in the long τ_n^{cl} region, the charge exchange loss cannot be negligible because low electron density plasmas include many neutral particles. To reduce the charge exchange loss in the estimation of τ_c , we have focused on the short τ_n^{cl} region. Here the short τ_n^{cl} region indicates $\tau_n^{cl} < 0.4$ s for tangential beams and $\tau_n^{cl} < 0.1$ s for perpendicular beams, respectively. In this region, we can estimate the effective confinement time τ_c^{eff} by the weighted least mean square fitting in $f(\tau_n^{cl})$. In addition, similar analyses have been performed for the other magnetic configurations. In figures 8 and 11, the effective NB fast ion diffusion coefficient D^{eff} is plotted against the position of the magnetic axis. It is clear that the tangential NBs have good confinement rather than the perpendicular NBs. Additionally, inward shifted plasmas have a good confinement of NB fast ions in both injection directions.

The dependence of the neo-classical diffusion coefficient on the position of the magnetic axis in LHD have been discussed numerically in Murakami *et al.* (2002). This reference showed that the neo-classical diffusion coefficient in the $1/\nu$ regime decreases as the plasma shifts inward. Because the neo-classical diffusion is dominated by trapped particles in usual, it can be considered that the dependence of D^{eff} on R_{ax} for perpendicular beam ions has same trend as the reference result. For tangential beam ions, it can be roughly explained that the orbit deviation from the magnetic surface becomes larger as the plasma shifts outward because the toroidal curvature component of the magnetic field, $B_{1,0}$ (poloidal mode number = 1, toroidal mode number = 0), increases as the plasma shifts outward. Obviously, however, the sensitivity of D^{eff} to R_{ax} is different from the reference results. Since the detailed discussion of this issue requires orbit simulations, this is future work.

We have focused on the decay time of the neutron emission rate to estimate τ_c^{eff} instead of the absolute value of the neutron emission rate S_n . The absolute value of S_n linearly depends on the bulk deuteron density, which is difficult to measure in the plasma core region. In actual plasmas, the deuteron density is diluted by the presence of the impurity ions. This dilution effect can be estimated by the obtained τ_c^{eff} and by the difference of the peak values of the measured and simulated neutron emission rates. From figure 12, the ratio of the deuteron density to the electron density is roughly estimated as $n_D/n_e = 0.42$. This estimation suffers no significant contradictions with impurity measurements as shown in § 6. According to the obtained τ_c and n_D/n_e , we can simulate a consistent neutron emission rate to the measured neutron emission rate.

Although we have estimated quantitatively the fast ion confinement time τ_c in LHD plasmas, the transport mechanism itself is still unclear. The clarification of the transport mechanism dominant in the short τ_n^{cl} region is future work.

Acknowledgements

This work is supported partly by LHD project budgets (NIFS07KLPH004 and NIFS14KNTT025). It is performed on 'Plasma Simulator' (FUJITSU FX100) of

NIFS with the support and under the auspices of the NIFS Collaboration Research program (NIFS18KNSR007).

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