

DATA REPORT

X-ray powder diffraction data and characterization of Mirabegron

Jose H. Quintana Mendoza,^{1,2,3,a)} J. A. Henao,¹ Andrea P. Aparicio,¹ and Arnold R. Romero Bohorquez^{1,2}

¹Grupo de Investigación en Química Estructural (GIQUE), Escuela de Química, Facultad de Ciencias, Universidad Industrial de Santander, A.A. 678, Carrera 27, Calle 9 Ciudadela Universitaria. Bucaramanga, Colombia

²Grupo de Investigación en Compuestos Orgánicos de Interés Medicinal (CODEIM), Parque Tecnológico Guatiguará, Universidad Industrial de Santander, A.A. 678, Piedecuesta, Colombia

³Grupo de Investigación en Biocalorimetría, Departamento de Química, Universidad de Pamplona, Km 1 vía Bucaramanga, Pamplona, Colombia

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Mirabegron, (C₂₁H₂₄N₄O₂S), is a β₃-adrenoceptor agonist approved in Japan, the USA, Canada and Europe, for the treatment of overactive bladder symptoms. There are no entries for this important active pharmaceutical ingredient in the Cambridge Structural Database or the Powder Diffraction File-4/Organics database. In this contribution, the powder diffraction pattern of Mirabegron, an unreported phase, are presented with a study by spectroscopy methods (Fourier-transform infrared spectroscopy [FT-IR] and RAMAN) and thermal analysis (thermogravimetric analysis [TGA]-differential scanning calorimetry [DSC]). © 2017 International Centre for Diffraction Data. [doi:10.1017/S0885715617001129]

Key words: Mirabegron, characterization, X-ray powder diffraction

I. INTRODUCTION

Mirabegron (Figure 1), an active pharmaceutical ingredient (API) approved in Japan, the USA, Canada and Europe, used for the symptomatic treatment of urgency, increased micturition frequency and/or urgency incontinence as may occur in adult patients with overactive bladder (OAB) syndrome. Mirabegron is a potent and selective β₃-adrenoceptor agonist (Nitti *et al.*, 2013).

There are no entries for this important API in the Cambridge Structural Database (CSD) (Groom *et al.*, 2016) or the Powder Diffraction File (PDF)-4/Organics database. A study by spectroscopy methods (Fourier-transform-infrared spectroscopy (FT-IR), RAMAN), thermal analysis [thermogravimetric analysis (TGA)-differential scanning calorimetry (DSC)] and X-ray powder diffraction of this material, crystallized from a commercial product, was carried out as part of our interest in the structural characterization of pharmaceuticals compounds.

II. EXPERIMENTAL

A. Extraction and crystallization

Commercial Mirabegron was dissolved in a mixture of isopropanol: water. After filtering, the extract was crystallized

by the solvothermal method in an autoclave under heating at 60 °C for 4 h. The density of the crystals was determined by the floatation method using potassium iodide solution.

B. IR and RAMAN spectroscopy

The FT-IR spectrum was measured in a IS50 FT-IR Nicolet Thermo Scientific spectrophotometer over the range 4000–400 cm⁻¹ with 32 scans per sample in KBr pellets. RAMAN spectrum was recorded in a LabRam HR Evolution using a laser at 532 nm with 100% attenuation to 3 s. in a range of 1700–800 cm⁻¹ owing to fluorescence sample.

C. Thermal analysis, TGA-DSC

Thermal analysis TGA-DSC were performed in a Thermal Analyzer differential thermal analysis/DSC Instrument Serie Discovery, both experiments under a nitrogen atmosphere with mass flow 50.0 ml min⁻¹, equilibrate at 25 °C, ramp at 10 °C min⁻¹ to 500 °C for TGA and 550 °C for DSC analysis.

C. X-ray powder diffraction data collection

Powder diffraction patterns were recorded at room temperature on a BRUKER D8 ADVANCE diffractometer

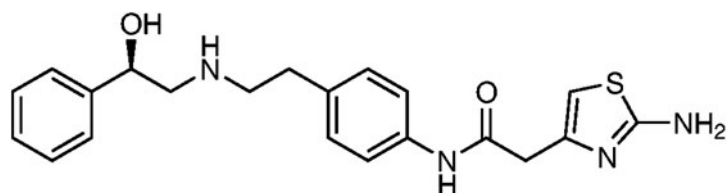


Figure 1. Chemical structure of mirabegron.

^{a)} Author to whom correspondence should be addressed. Electronic mail: jhquintanam@gmail.com

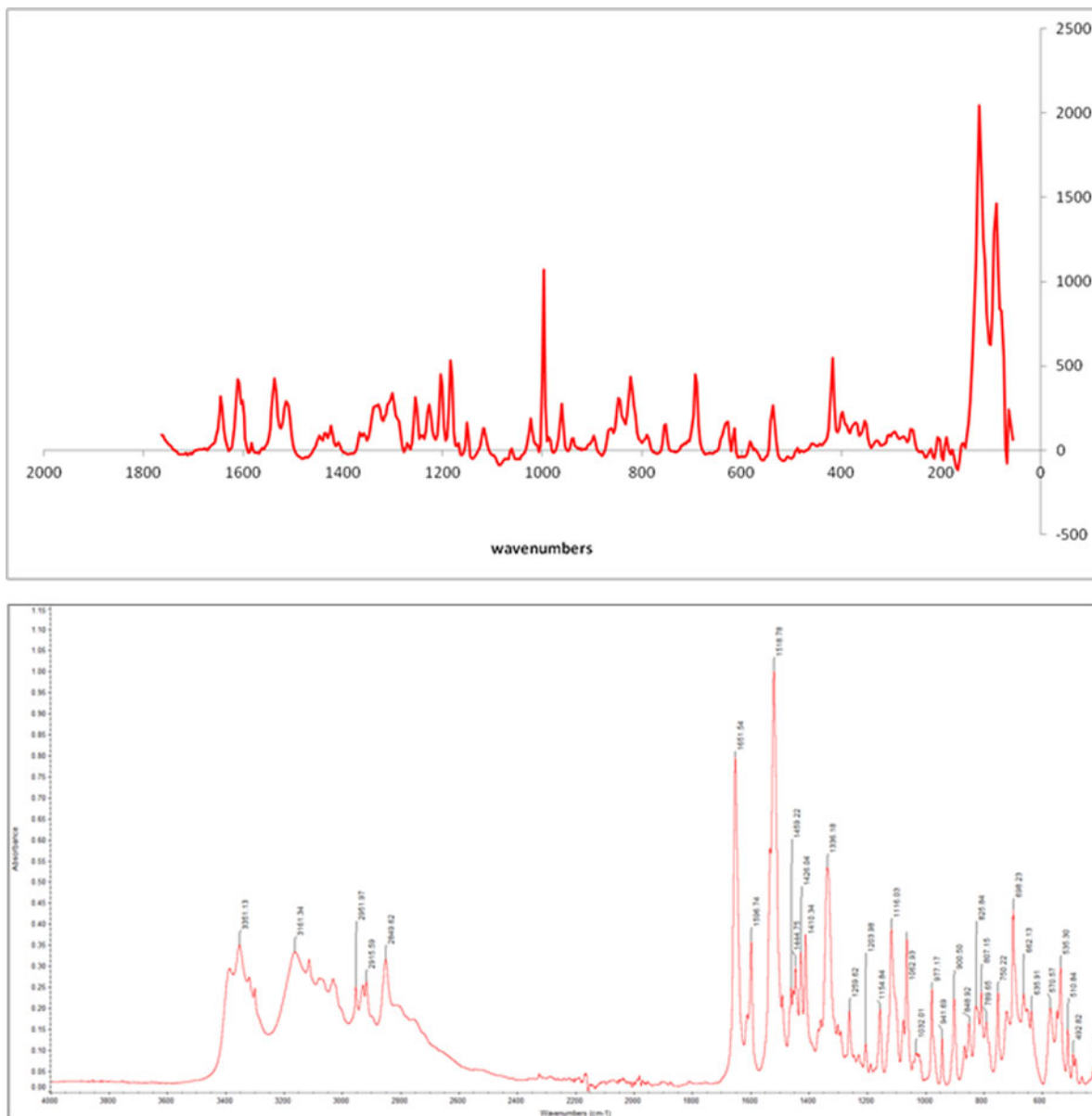


Figure 2. (Colour online) RAMAN spectrum (top) and IR spectrum (bottom) of mirabegron.

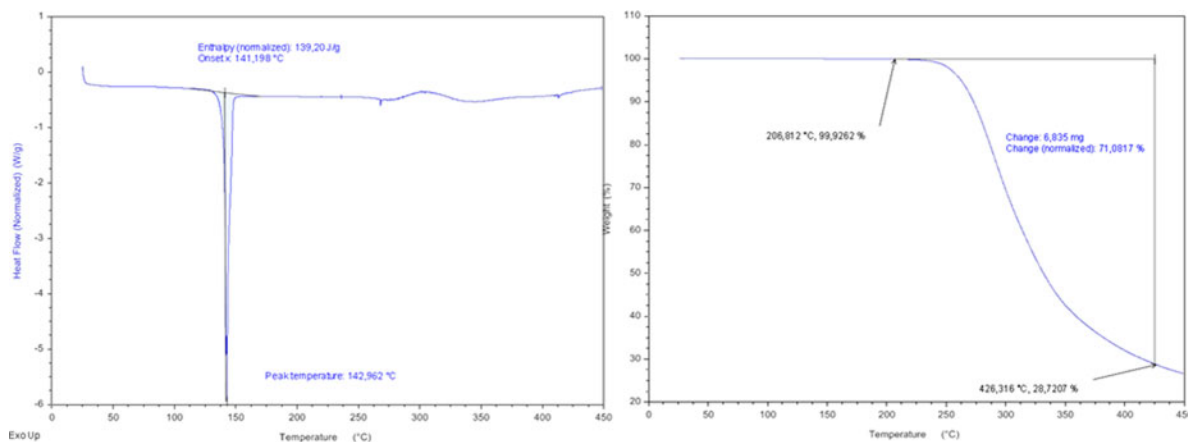


Figure 3. (Colour online) DSC (right) curve and TGA curve (left) of mirabegron.

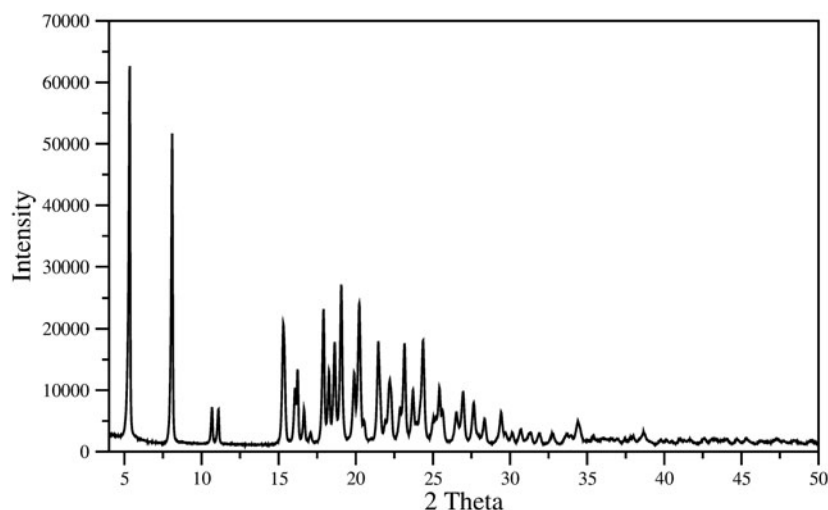


Figure 4. Powder diffraction pattern of mirabegron.

using $\text{CuK}\alpha$ radiation, operating at 40 kV and 40 mA, in steps of 0.0156° (2θ), from 4° to 50° at 1 s per step. The diffractometer was equipped with the primary and secondary Soller slits of 2.5° , divergence slit of 0.6 mm, Nickel filter of 0.02 mm, and a LynxEye detector. The fitting and subtraction of background, using the Sonneveld and Visser (1975) method, smoothing by sliding polynomials (Savitzky and Golay, 1964) and $K\alpha_2$ -stripping (Rachinger, 1948) were performed

using PowderX program (Dong, 1999); the second derivative method was used to determine the peak observed positions.

III. RESULTS AND DISCUSSION

Raman spectrum (Figure 2) shows a strong band at 997 cm^{-1} , corresponding to the vibration C–S. The vibration

TABLE I. X-ray powder diffraction data of mirabegron.

| $2\theta_{\text{obs}} (^\circ)$ | $d_{\text{obs}} (\text{\AA})$ | $(hkl)_{\text{obs}}$ | h | K | L | $2\theta_{\text{calc}} (^\circ)$ | $d_{\text{calc}} (\text{\AA})$ | $\Delta 2\theta (^\circ)$ |
|---------------------------------|-------------------------------|----------------------|-----|-----|-----|----------------------------------|--------------------------------|---------------------------|
| 5.341 | 16.5328 | 1000 | 0 | 0 | 1 | 5.333 | 16.5573 | -0.008 |
| 8.090 | 10.9201 | 825 | 0 | 1 | 1 | 8.093 | 10.9160 | 0.003 |
| 10.668 | 8.2862 | 90 | 0 | 0 | 2 | 10.678 | 8.2787 | 0.010 |
| 11.082 | 7.9776 | 87 | 0 | 1 | 2 | 11.096 | 7.9674 | 0.014 |
| 15.299 | 5.7868 | 327 | 0 | 2 | 1 | 15.280 | 5.7938 | -0.019 |
| 16.049 | 5.5180 | 144 | 0 | 0 | 3 | 16.046 | 5.5191 | -0.003 |
| 16.214 | 5.4623 | 192 | 0 | 2 | 2 | 16.227 | 5.4580 | 0.013 |
| 16.634 | 5.3253 | 87 | 1 | 0 | 0 | 16.644 | 5.3221 | 0.010 |
| 17.056 | 5.1945 | 26 | 1 | 0 | 1 | 17.071 | 5.1900 | 0.015 |
| 17.893 | 4.9533 | 353 | -1 | 0 | 1 | 17.898 | 4.9519 | 0.005 |
| 18.251 | 4.8569 | 189 | 1 | 1 | 0 | 18.261 | 4.8543 | 0.010 |
| 18.619 | 4.7618 | 267 | 0 | -2 | 1 | 18.623 | 4.7609 | 0.004 |
| 19.046 | 4.6560 | 423 | 1 | 1 | 2 | 19.062 | 4.6520 | 0.016 |
| 19.883 | 4.4618 | 185 | 1 | -1 | 1 | 19.882 | 4.4620 | -0.001 |
| 20.214 | 4.3895 | 378 | 0 | -1 | 3 | 20.214 | 4.3894 | 0.000 |
| 20.524 | 4.3239 | 53 | -1 | 0 | 2 | 20.536 | 4.3213 | 0.012 |
| 20.983 | 4.2303 | 4 | -1 | 1 | 2 | 20.988 | 4.2293 | 0.005 |
| 21.452 | 4.1389 | 271 | 0 | 0 | 4 | 21.450 | 4.1393 | -0.002 |
| 21.572 | 4.1161 | 156 | 1 | 1 | 3 | 21.575 | 4.1157 | 0.003 |
| 21.915 | 4.0525 | 55 | 1 | 2 | 1 | 21.913 | 4.0529 | -0.002 |
| 22.181 | 4.0045 | 166 | 0 | -2 | 2 | 22.157 | 4.0088 | -0.024 |
| 22.278 | 3.9873 | 143 | 1 | -1 | 2 | 22.283 | 3.9864 | 0.005 |
| 22.867 | 3.8859 | 91 | 1 | 2 | 0 | 22.867 | 3.8859 | 0.000 |
| 23.144 | 3.8400 | 269 | 0 | 3 | 1 | 23.148 | 3.8393 | 0.004 |
| 23.694 | 3.7521 | 140 | -1 | 2 | 0 | 23.689 | 3.7529 | -0.005 |
| 23.926 | 3.7162 | 49 | -1 | 1 | 3 | 23.923 | 3.7167 | -0.003 |
| 24.149 | 3.6824 | 113 | -1 | 0 | 3 | 24.128 | 3.6856 | -0.021 |
| 24.345 | 3.6532 | 280 | -1 | 2 | 2 | 24.343 | 3.6535 | -0.002 |
| 25.033 | 3.5543 | 65 | 1 | 1 | 4 | 25.034 | 3.5542 | 0.001 |
| 25.201 | 3.5310 | 68 | 1 | -2 | 1 | 25.166 | 3.5359 | -0.035 |
| 25.413 | 3.5020 | 149 | 0 | 1 | 5 | 25.424 | 3.5005 | 0.011 |
| 25.618 | 3.4745 | 85 | 1 | -1 | 3 | 25.631 | 3.4727 | 0.013 |
| 26.314 | 3.3841 | 23 | 0 | -2 | 3 | 26.362 | 3.3781 | 0.048 |

Continued

TABLE I. Continued

| $2\theta_{\text{obs}}$ (°) | d_{obs} (Å) | $(H_0)_{\text{obs}}$ | h | K | L | $2\theta_{\text{calc}}$ (°) | d_{calc} (Å) | $\Delta 2\theta$ (°) |
|----------------------------|----------------------|----------------------|-----|-----|-----|-----------------------------|-----------------------|----------------------|
| 26.508 | 3.3598 | 84 | 1 | 2 | 4 | 26.513 | 3.3592 | 0.005 |
| 26.600 | 3.3484 | 53 | 0 | -3 | 1 | 26.622 | 3.3457 | 0.022 |
| 26.940 | 3.3069 | 142 | -1 | -1 | 3 | 26.948 | 3.3060 | 0.008 |
| 27.631 | 3.2258 | 112 | 1 | 3 | 2 | 27.631 | 3.2257 | 0.000 |
| 27.856 | 3.2002 | 29 | 1 | 3 | 1 | 27.869 | 3.1987 | 0.013 |
| 28.336 | 3.1471 | 69 | -1 | 0 | 4 | 28.338 | 3.1469 | 0.002 |
| 29.129 | 3.0632 | 17 | 1 | 1 | 5 | 29.130 | 3.0631 | 0.001 |
| 29.409 | 3.0347 | 88 | -1 | 3 | 1 | 29.405 | 3.0351 | -0.004 |
| 29.671 | 3.0085 | 29 | -1 | 3 | 2 | 29.684 | 3.0072 | 0.013 |
| 29.981 | 2.9781 | 19 | 1 | 2 | 5 | 29.940 | 2.9820 | -0.041 |
| 30.132 | 2.9635 | 31 | -1 | 3 | 0 | 30.127 | 2.9640 | -0.005 |
| 30.563 | 2.9227 | 26 | 1 | 0 | 5 | 30.602 | 2.9190 | 0.039 |
| 30.686 | 2.9112 | 39 | 0 | 1 | 6 | 30.707 | 2.9093 | 0.021 |
| 31.013 | 2.8813 | 11 | 0 | -2 | 4 | 30.996 | 2.8828 | -0.017 |
| 31.186 | 2.8657 | 26 | 0 | 2 | 6 | 31.168 | 2.8673 | -0.018 |
| 31.308 | 2.8548 | 32 | 0 | 4 | 1 | 31.288 | 2.8566 | -0.020 |
| 31.887 | 2.8043 | 30 | -1 | 1 | 5 | 31.898 | 2.8034 | 0.011 |
| 32.629 | 2.7422 | 21 | 0 | 4 | 0 | 32.659 | 2.7397 | 0.030 |
| 32.755 | 2.7319 | 28 | 0 | 4 | 4 | 32.791 | 2.7290 | 0.036 |
| 32.923 | 2.7183 | 9 | -1 | 2 | 5 | 32.946 | 2.7165 | 0.023 |
| 33.676 | 2.6593 | 27 | 1 | 1 | 6 | 33.662 | 2.6603 | -0.014 |
| 33.920 | 2.6407 | 24 | 2 | 1 | 1 | 33.940 | 2.6392 | 0.020 |
| 34.389 | 2.6057 | 64 | 2 | 1 | 2 | 34.388 | 2.6058 | -0.001 |
| 34.533 | 2.5952 | 45 | 2 | 0 | 2 | 34.536 | 2.5950 | 0.003 |
| 34.899 | 2.5688 | 8 | 1 | 4 | 1 | 34.864 | 2.5713 | -0.035 |
| 35.050 | 2.5581 | 9 | 0 | 4 | 5 | 35.045 | 2.5584 | -0.005 |
| 35.371 | 2.5356 | 23 | 2 | -1 | 1 | 35.368 | 2.5358 | -0.003 |
| 35.692 | 2.5135 | 10 | 2 | 1 | 3 | 35.691 | 2.5136 | -0.001 |
| 35.977 | 2.4943 | 15 | -1 | -1 | 5 | 35.971 | 2.4947 | -0.006 |
| 36.057 | 2.4889 | 15 | 0 | -1 | 6 | 36.024 | 2.4912 | -0.033 |
| 36.232 | 2.4773 | 13 | -1 | 4 | 2 | 36.227 | 2.4777 | -0.005 |
| 36.400 | 2.4663 | 11 | -1 | 4 | 1 | 36.406 | 2.4659 | 0.006 |
| 36.547 | 2.4567 | 15 | -1 | 1 | 6 | 36.538 | 2.4573 | -0.009 |
| 36.907 | 2.4335 | 14 | -1 | 4 | 3 | 36.882 | 2.4351 | -0.025 |
| 37.032 | 2.4256 | 9 | 2 | 2 | 3 | 37.049 | 2.4245 | 0.017 |
| 37.425 | 2.4010 | 13 | 1 | -3 | 3 | 37.420 | 2.4014 | -0.005 |
| 37.727 | 2.3825 | 12 | -2 | -1 | 2 | 37.733 | 2.3822 | 0.006 |
| 37.796 | 2.3783 | 17 | 2 | 1 | 4 | 37.771 | 2.3798 | -0.025 |
| 37.970 | 2.3678 | 22 | 0 | 3 | 7 | 37.980 | 2.3672 | 0.010 |
| 38.383 | 2.3433 | 14 | 1 | 2 | 7 | 38.372 | 2.3439 | -0.011 |
| 38.653 | 2.3275 | 32 | 2 | -1 | 3 | 38.648 | 2.3278 | -0.005 |
| 38.916 | 2.3124 | 10 | 0 | 5 | 2 | 38.908 | 2.3129 | -0.008 |
| 39.094 | 2.3023 | 5 | 1 | -2 | 5 | 39.117 | 2.3010 | 0.023 |
| 39.747 | 2.2660 | 11 | 2 | 3 | 2 | 39.749 | 2.2658 | 0.002 |
| 40.041 | 2.2500 | 9 | 1 | 3 | 7 | 40.025 | 2.2509 | -0.016 |
| 40.136 | 2.2449 | 11 | 2 | 3 | 3 | 40.155 | 2.2438 | 0.019 |
| 40.419 | 2.2298 | 5 | 1 | 0 | 7 | 40.432 | 2.2291 | 0.013 |
| 40.529 | 2.2240 | 6 | 2 | 1 | 5 | 40.528 | 2.2241 | -0.001 |
| 40.999 | 2.1996 | 15 | 2 | 2 | 5 | 41.015 | 2.1988 | 0.016 |
| 41.276 | 2.1855 | 9 | 0 | 2 | 8 | 41.284 | 2.1851 | 0.008 |
| 41.497 | 2.1744 | 11 | 0 | 4 | 7 | 41.512 | 2.1736 | 0.015 |
| 41.645 | 2.1670 | 12 | 1 | -4 | 2 | 41.639 | 2.1672 | -0.006 |
| 41.873 | 2.1557 | 4 | -1 | -3 | 4 | 41.886 | 2.1550 | 0.013 |
| 42.354 | 2.1323 | 7 | -2 | 3 | 1 | 42.349 | 2.1326 | -0.005 |
| 42.567 | 2.1221 | 16 | 0 | 3 | 8 | 42.604 | 2.1204 | 0.037 |
| 43.092 | 2.0975 | 15 | -2 | -3 | 1 | 43.066 | 2.0987 | -0.026 |
| 43.328 | 2.0866 | 12 | 0 | -5 | 1 | 43.333 | 2.0864 | 0.005 |
| 43.571 | 2.0755 | 7 | 0 | 5 | 6 | 43.560 | 2.0761 | -0.011 |
| 43.733 | 2.0682 | 9 | -1 | 5 | 3 | 43.757 | 2.0671 | 0.024 |
| 43.899 | 2.0608 | 11 | 1 | -1 | 7 | 43.936 | 2.0591 | 0.037 |
| 44.067 | 2.0533 | 13 | -1 | 5 | 1 | 44.050 | 2.0541 | -0.017 |
| 44.29 | 2.0435 | 1 | 1 | 3 | 8 | 44.295 | 2.0433 | 0.005 |
| 44.711 | 2.0252 | 13 | 2 | 4 | 3 | 44.707 | 2.0254 | -0.004 |
| 44.863 | 2.0187 | 9 | -1 | -4 | 3 | 44.831 | 2.0201 | -0.032 |
| 45.299 | 2.0003 | 16 | 1 | -3 | 5 | 45.269 | 2.0015 | -0.030 |
| 45.495 | 1.9921 | 7 | 0 | 4 | 8 | 45.502 | 1.9919 | 0.007 |

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TABLE I. Continued

| $2\theta_{\text{obs}}$ (°) | d_{obs} (Å) | $(III)_{\text{obs}}$ | h | K | L | $2\theta_{\text{calc}}$ (°) | d_{calc} (Å) | $\Delta 2\theta$ (°) |
|----------------------------|----------------------|----------------------|-----|-----|-----|-----------------------------|-----------------------|----------------------|
| 46.189 | 1.9638 | 9 | -1 | -1 | 7 | 46.165 | 1.9648 | -0.024 |
| 46.314 | 1.9588 | 8 | -1 | -3 | 5 | 46.323 | 1.9584 | 0.009 |
| 46.659 | 1.9451 | 9 | 0 | 2 | 9 | 46.657 | 1.9452 | -0.002 |
| 47.053 | 1.9297 | 10 | 0 | 6 | 3 | 47.014 | 1.9313 | -0.039 |
| 47.260 | 1.9218 | 14 | 0 | -3 | 6 | 47.257 | 1.9219 | -0.003 |
| 47.724 | 1.9042 | 9 | -1 | 3 | 8 | 47.736 | 1.9037 | 0.012 |
| 47.951 | 1.8957 | 4 | 1 | 5 | 7 | 47.932 | 1.8964 | -0.019 |
| 48.186 | 1.8870 | 6 | 1 | 2 | 9 | 48.178 | 1.8873 | -0.008 |
| 48.277 | 1.8836 | 8 | 0 | 6 | 1 | 48.284 | 1.8834 | 0.007 |
| 48.454 | 1.8772 | 11 | -2 | 1 | 6 | 48.445 | 1.8775 | -0.009 |
| 48.750 | 1.8665 | 5 | 1 | -2 | 7 | 48.754 | 1.8663 | 0.004 |
| 48.941 | 1.8596 | 3 | 1 | 1 | 9 | 48.945 | 1.8595 | 0.004 |
| 49.283 | 1.8475 | 6 | 1 | 6 | 4 | 49.284 | 1.8475 | 0.001 |
| 49.490 | 1.8403 | 12 | 0 | 0 | 9 | 49.506 | 1.8397 | 0.016 |
| 49.737 | 1.8317 | 7 | 2 | -4 | 1 | 49.762 | 1.8309 | 0.025 |

C=N appears at 1610 cm^{-1} and one at 1644 cm^{-1} corresponds to C=O. The FT-IR spectrum (Figure 2) shows the bands characteristic of the functional groups in the material showing the chemical nature of the compound. Stretching O-H is overlapped by the bands of stretching N-H observed at 3351 cm^{-1} and the amide at 3161 cm^{-1} absorption bands widened by possibly Csp²-H and Csp³-H are observed at 3050 cm^{-1} and 2951 cm^{-1} , respectively. The characteristic band of the amide carbonyl (band I) is observed at 1557 cm^{-1} while the band II amide is observed at 1508 cm^{-1} . Other important bands are 1596 cm^{-1} to stretching C=C and 1333 cm^{-1} corresponding to the C-N vibration. In general, the spectrum shows absorption bands widened by possibly numerous hydrogen bonds in the structure.

Mirabegron melts at 142.96 °C , according to the first endotherm in DSC analysis (Figure 3). The TGA curve (Figure 3) shows that the material is stable up to 200 °C , experiencing weight loss 70.08% at $\sim 206\text{--}426\text{ °C}$. This corresponds to the total decomposition of mirabegron.

The indexing of pattern recorded (Figure 4) for the material was carried out with DICVOL14 (Boultif and Louër, 2014). The analysis with NSB*AIDS83 (Mighell *et al.*, 1981), resulted in a triclinic unit cell P1 with parameters: $a = 5.351(2)\text{ Å}$, $b = 11.612(2)\text{ Å}$, $c = 17.591(2)\text{ Å}$, $\alpha = 70.79(1)$, $\beta = 84.42(2)$, $\gamma = 86.29(2)$, $V = 1026.6(3)\text{ Å}^3$, and figures of merit associated are $M20 = 30.6$ and $F30 = 67.7$ (0.0085, 52) (de Wolf, 1968; Smith and Snyder, 1979). Table I contains the corresponding powder diffraction data. This pattern, in PD3 format, will be submitted for inclusion in the Powder Diffraction File. The space group is P1 with $Z = 2$, of the commercial material is chiral. The fitting of the whole pattern with the Le Bail algorithm in FULLPROF program (Rodríguez-Carvajal, 1990), using the above-mentioned unit cell parameters, accounts for all the diffraction maxima recorded. $Z = 2$ was estimated by density obtained by the flotation method ($d = 1.22(1)\text{ g cm}^{-3}$), and the calculated density, using this Z -value and the volume obtained from the indexing process, was 1.21 g cm^{-3} , similar to measured density.

SUPPLEMENTARY MATERIAL

The supplementary material for this article can be found at <https://doi.org/10.1017/S0885715617001129>.

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