

A TIME-VARYING APPROACH OF THE US WELFARE COST OF INFLATION

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Money-demand specifications exhibit instability, especially for long spans of data. This paper reconsiders the welfare cost of inflation for the US economy using a flexible time-varying (TV) cointegration methodology to estimate the money-demand function. We find evidence that the TV cointegration estimation provides a better fit of the actual data than a time-invariant estimation and that the throughout unitary income elasticity only exists for the log–log form over the entire sample period. Our estimate of the welfare cost of inflation for a 10% inflation rate lies in the range of 0.025–0.75% of gross domestic product (GDP) and averages 0.27%. In sum, our findings fall well within the ranges of existing studies of the welfare cost of inflation. We find that the welfare cost averages 7.4% higher during expansions than recessions for 10% inflation rate. Finally, the interest elasticity of money demand shows substantial variability over our sample period.

Keywords: Money-Demand Function, Welfare Cost of Inflation, Time-Varying Cointegration

1. INTRODUCTION

Macroeconomists borrow ideas from microeconomics to consider the welfare cost of inflation, which refers to the changes in social welfare caused by inflation. Bailey (1956) and Friedman (1969) develop the now traditional approach that treats real money balances as a consumption good and inflation as a tax on real balances. This approach measures the welfare cost as the appropriate area under the money–demand curve.

Ireland (2009) re-examines the welfare cost estimates reported in Lucas (2000), noting that the extension of Lucas’s sample of annual data from 1900 to 1994 to 1900 to 2004 adds another period of extremely low interest rates with which

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to estimate the money-demand function. Ireland (2009, p. 1043, Fig. 2) plots the data, showing that the semilog specification may fit the more recent data (i.e., post-1979) better than the log–log specification that Lucas (2000) uses. Ireland (2009) considers only the post-1979 period, using quarterly rather than annual observations. He concludes that the semilog specification dominates the log–log specification, reporting a welfare cost for a 10% inflation rate of less than 0.25% of income (2009, p. 1048). Lucas (2000) finds a welfare cost for 10% inflation of just over 1.8% of income for the log–log specification and just less than 1.2% for the semilog specification.

The idea of instability in the money-demand function also received considerable attention just prior to, and shortly after, 1979. Goldfeld (1976) referred to this issue as the “Case of the Missing Money” that began in 1973. The post-1973 economic events raised doubts about the conventional wisdom concerning the stability of money demand. Much effort tried to re-establish the stability of the money demand. One approach considered the appropriate definition of money—M1, M2, or other constructed measures [Garcia and Pak (1979)].¹ Another approach explored the specification of short-run dynamic monetary adjustments, in terms of supply-versus demand-adjusting models [Miller (1990)]. And a virtually inexhaustible supply of other competing hypotheses exists.² Judd and Scadding (1982) reviewed the different rationalizations of the post-1973 money market events. Building on an older idea of Chow (1966) about the short-and long-run money demand, Miller (1991) applied the new econometric technique of cointegration and error-correction modeling to examine the short-and long-run money demand.

Rather than redefining how to measure money or considering the short-run dynamics of the money market, we consider changes in the structure (i.e., elasticities) of money demand, using a time-varying (TV) parameter cointegration approach for quarterly data from 1959 to 2010. In addition, the more recent data add another period of very low interest rates with which to estimate the money-demand function. We find strong evidence of TV parameters in the cointegration relationship, and the log–log specification, once again, dominates the semilog specification. Finally, our TV estimates of the welfare cost of inflation generally fall closer to the findings of Ireland, implying smaller effects than in Lucas (2000).

The welfare cost of inflation considers the long-run effects of inflation and abstracts from the effects of inflation on redistribution because of any difference between expected and actual inflation. That is, the calculation of the welfare cost assumes that the private sector expects the current inflation rate, which could describe an economy with a well-functioning inflation-targeting regime. Moreover, all contracts reflect the actual and expected inflation rate so that no distortions exist in real decisions.

Since the welfare cost of inflation captures long-run effects, the first step in calculating this welfare cost searches for the long-run money–demand relationship. Typically, that means determining whether a cointegrating relationship exists among the variables in the money-demand function. The rejection of traditional cointegration, however, does not necessarily mean that cointegration does not exist.

Rather, the cointegrating relationship may reflect either instability or nonlinearity, or both. Papers that address the instability issue include, for example, Khan (1974), Duprey (1980), Tesfatsion and Veitch (1990), Hafer and Jansen (1991), Miller (1991), Lütkepohl (1993), Ireland (2009), Rao and Kumar (2011), Wang (2011), Nakashima and Saito (2012), Lucas and Nicolini (2013), and Mogliani and Urga (2015) and papers that address the nonlinearity issue include Vinod (1998), Escribano (2004), Serletis and Shahmoradi (2005, 2007a, 2007b), Bae and DeJong (2007), Calza and Zaghini (2009), Nakashima (2009), Jawadi and Sousa (2013), and Gupta and Majumdar (2014). A linear TV function can summarize nonlinearity of any form [Granger (2008)] and also capture structural change by considering in the limit each point in time as a different regime, as it seems empirically true for the case of the money-demand function.

This paper reconsiders the welfare cost of inflation for the US economy using the system-based TV cointegration method of Bierens and Martins (2010) to estimate the long-run relationship between money, income, and the interest rate according to the Meltzer (1963) log–log and the Cagan (1956) semilog specifications. We find significant evidence of TV cointegration against the standard cointegration approach of time-invariant (TI) coefficients.

The unitary income elasticity only exists for the log–log form over the entire sample period. This specification produces estimates of the welfare cost of inflation for a 10% inflation rate that lie in the range of 0.025–0.75% of GDP over time and averaging 0.27% in sample. This compares favorably to the values of about 0.2–0.3% of income that Fischer (1981), Serletis and Yavari (2004), and Ireland (2009) report but differ from those that Lucas (2000) reports of closer to 1.

Our model with TV coefficients fits the data better and is more general than the standard TI specification adopted by the authors cited above. Therefore, our results probably indicate that the single-valued welfare cost of inflation obtained from standard cointegration methods captures the sample average of the estimated welfare costs at each point of time. We can relate the periods when the welfare cost falls below or above average to the position of the US business cycle. That is, we find that the welfare cost averages from 12.0%, 10.3%, and 7.4% higher during expansions than recessions for 0%, 2%, and 10% inflation rates. To the best of our knowledge, this is the first paper to estimate TV, long-run money-demand functions for the US economy, and more importantly, also the first to provide a TV measure of the associated welfare costs of inflation, using quarterly data on the measure of real money balances, real income, and nominal interest rate over the period of 1959:Q1–2010:Q4.

Mogliani and Urga (2015) consider the instability of the long-run US money demand and the welfare cost of inflation using a sample of annual data from 1900 to 2013. They first test for cointegration over the entire sample, finding evidence of no cointegration. Then, they re-examine the data sample for cointegration with breaks in the structure, finding such breaks in 1945 and 1976. Zuo and Park (2011) and Barigozzi and Conti (2014) provide estimates of TV long-run money-demand functions for China and Europe, based on the single-equation Park and Hahn

(1999) and Bierens and Martins (2010) approaches, respectively. Still, neither of them do (TV) welfare analysis. On the other hand, Kumar (2014) estimates the (TV) welfare cost of inflation in India over the period of 1996:Q2–2013:Q1 using a different methodology: the Kalman filter. The measurement money-demand equation is an AR(1) model for money over income with a nominal interest rate as a regressor. The state equation for the TV (semi) elasticity of the money demand is a standard random walk process. He concludes that the welfare cost increased in recent years (about 0.04% in 2012).

The paper conforms to the following outline. Section 2 briefly discusses the existing literature in this area. Section 3 lays out the theoretical issues involved in calculating the welfare cost of inflation. Section 4 describes the econometric methodology, discusses the data, implements the method, and analyzes the findings. Section 5 concludes.

2. EXISTING EMPIRICAL ESTIMATES

We can primarily categorize the voluminous literature on the welfare costs of inflation in the US, and internationally,³ under three alternative approaches. First, the simplest analysis computes the deadweight loss by evaluating the area under the money–demand curve in a partial-equilibrium framework [Fischer (1981), Lucas (1981), Gillman (1995), Serletis and Yavari (2004), Ireland (2009), Lim et al. (2011), Gupta and Majumdar (2014)]. Second, another method computes the welfare cost from general-equilibrium models [Cooley and Hansen (1989), Gillman (1993), Gomme (1993), Lucas (1994), Dotsey and Ireland (1996), Aiyagari et al. (1998), Pakko (1998), Wu and Zhang (1998), Lucas (2000), Evans and Kenc (2003), Lagos and Wright (2005), Burstein and Hellwig (2008), Craig and Rocheteau (2008), Henriksen and Kydland (2010), Boel and Camera (2011), Silva, (2012), Adão and Silva (2013)].⁴ Third, other authors use partial-equilibrium models that capture the interaction between capital income taxation and inflation [Feldstein (1997, 1999)]. Understandably, these three approaches reach different conclusions regarding the sizes of the welfare cost of inflation. In general, welfare costs obtained from calculating the deadweight loss under the long-run money-demand function produce estimates substantially lower than those obtained from general-equilibrium models and partial-equilibrium models that account for the interaction between capital income taxation and inflation.⁵ This is expected, since the former approach accounts only for the money-demand distortion brought about by positive nominal interest rates, while, in general equilibrium, increases in inflation can distort other marginal decisions, affecting both the level and the growth rate of aggregate output. Furthermore, the interactions between inflation and a not-completely-indexed tax code can add substantially to the welfare cost of inflation as well.

Fischer (1981) and Lucas (1981) calculate relatively low welfare costs of inflation. Fischer (1981) computes the deadweight loss generated by increasing the inflation rate from 0% to 10% at just 0.3% of GDP, using the monetary base

(government money) as the definition of money. Lucas (1981) calculates the welfare cost of the same change in the inflation rate from 0% to 10% inflation at 0.45% of GDP, using M1 as the measure of money. Lucas (2000) revises his estimate of the welfare cost upward, to slightly less than 1% of GDP.

Ireland (2009) more recently investigates the welfare cost of money, using quarterly US data covering the period of 1980:Q1–2006:Q4.⁶ He cannot reject the null of unitary long-run income elasticity of money demand. As a consequence, he expresses the money-demand function as the relationships between the nominal money–income ratio and the nominal interest rate. He chooses the (cointegrated) semilog formulation of money demand over the competing (spurious) log–log specification over his sample period of 1980:Q1–2006:Q4. Finally, he finds that the welfare cost of inflation lies between 0.014% and 0.232% of GDP for inflation rates between 0% and 10%, which compares closely to the welfare estimates of Fischer (1981) and Lucas (1981) but not so much to Lucas (2000) for the United States. Essentially, the larger value obtained by Lucas is explained by a different sample period (1900–1994) and model specification (log–log).

Structural models provide a recent alternative to econometric estimates of the triangle under an estimated money–demand curve. Cooley and Hansen (1989) calibrate a cash-in-advance version of a business cycle model. They find that the welfare cost of 10% inflation is about 0.4% of gross national product. In a follow-up paper, Cooley and Hansen (1991) consider the effects of distortionary taxes on the welfare cost measure, finding that the welfare cost rises to nearly 1% when the cash good proves more important in the utility function than the credit good in their cash-in-advance model. Silva (2012) extends the cash-in-advance model to give agents the flexibility to choose when they convert bonds into cash and shows that the welfare cost rises by 10-fold from 0.1% in the benchmark model to 1% in the model with agent flexibility. Other recent general-equilibrium models that estimate the welfare cost of inflation include Dotsey and Ireland (1996), Aiyagari et al. (1998), Burstein and Hellwig (2008), Dibooglu and Kenc (2009), and Henriksen and Kydland (2010).

Pakko (1998) develops a shopping-time model of money demand. He estimates that the welfare cost of raising the inflation rate from 0% to 10% equals 1.3%. Craig and Rocheteau (2008) argue that a search-theoretic framework is necessary for appropriately measuring the welfare cost of inflation. Lagos and Wright (2005) model monetary exchange and provide estimates for the annual cost of 10% inflation of between 3% and 5% of consumption, which translates into 2% to 3.5% of GDP in the United States.

In sum, various methods and specifications to estimate the welfare cost of inflation exist in the literature. Their conclusions do not differ too much with welfare costs as a fraction of GDP below 5%. To summarize, welfare cost estimates are found to range between 0.3% of GDP (Fischer, 1981) and 5.98% of GDP [Wu and Zhang (1998)] for a 10% inflation rate. In this paper, we consider the size of the TV welfare costs of inflation based on the distortion of inflation to the money demand only.

3. WELFARE COSTS OVER TIME

Ireland (2009) suggests that structural change may affect the welfare cost calculations and confines his sample to quarterly data from 1980 to 2006. We address the possibility of structural change by implementing the TV cointegration approach of Bierens and Martins (2010). As such, we calculate a TV welfare cost.

Calculating the welfare cost of inflation depends critically on the specification of the money-demand function. Lucas (2000) employs two money-demand specifications, which come from Meltzer (1963) and Cagan (1956). The first specification due to Meltzer (1963) relates the natural logarithms of real money balances (M/P), real income (Y/P), and nominal interest rate (r), where M denotes the nominal money supply and Y denotes the nominal income. That is,

$$\ln (M/P)_t = \ln A_t + \alpha_t \cdot \ln (Y/P)_t - \eta_t \cdot \ln r_t, \quad (1)$$

where $A_t > 0$ is a TV intercept, α_t is the TV income elasticity of money demand, and $\eta_t > 0$ measures the absolute value of the TV interest elasticity of money demand.

The second specification due to Cagan (1956) links the natural logarithms of real money balances and real income, and the level of the nominal interest rate as follows:

$$\ln (M/P)_t = \ln B_t + \beta_t \cdot \ln (Y/P)_t - \xi_t \cdot r_t, \quad (2)$$

where $B_t > 0$ is a TV intercept, β_t is the TV income elasticity of money demand, and $\xi_t > 0$ measures the absolute value of the semielasticity of money demand with respect to the interest rate.

Then, following the literature, we analyze the specifications for which we cannot reject the null hypothesis that the income elasticity equals unity for all t . Thus, we can write the corresponding TV relationships in equations (1) and (2), respectively, in terms of money-income ratio (m), as follows:

$$\ln m_t = \ln A_t - \eta_t \ln r_t \quad (3)$$

and

$$\ln m_t = \ln B_t - \xi_t r_t. \quad (4)$$

Bailey (1956) identified the welfare cost of inflation as the area under the inverse money-demand function (the consumer surplus) gained by reducing the interest rate to zero from its existing value.⁷ Thus, for an estimated money-demand function given by $m(r, t)$ and the implied inverse demand function represented by $\psi(m, t)$, we can calculate the welfare cost as follows:

$$w(r, t) = \int_{m(r)}^{m(0)} \psi(x, t) dx = \int_0^r m(x, t) dx - r \cdot m(r, t). \quad (5)$$

The second integral in equation (5) shows an alternative way to calculate the consumer surplus. Here, we integrate under the money-demand curve as the

interest rate rises from zero to a positive value, giving the lost consumer surplus. Then, we deduct the associated seigniorage revenue [i.e., $r \cdot m(r;t)$] to deduce the deadweight loss.

Remember that the function m measures money as a fraction of income. Thus, the function w also measures values as a fraction of income. In this case, the value of $w(r;t)$ measures the fraction of income that people need, as compensation, to become indifferent between living in a steady state with an interest rate constant at r or in a steady state with an interest equal to zero. Lucas (2000) shows that when the money-demand function conforms to the log–log specification, $m(r) = A \cdot r^{-\eta}$ so that in equation (3) the level $m(r;t) = A_t \cdot r^{-\eta_t}$. Thus, the welfare cost of inflation as a fraction of GDP equals the following expression:

$$w(r, t) = A_t \left(\frac{\eta_t}{1 - \eta_t} \right) r^{1-\eta_t}. \tag{6}$$

When the money-demand function corresponds to the semilog specification in equation (4), the level of $m(r;t) = B_t \cdot e^{-\xi_t r}$. Now, the welfare cost of inflation conforms to the following expression:

$$w(r, t) = \frac{B_t}{\xi_t} [1 - (1 + \xi_t r) e^{-\xi_t r}]. \tag{7}$$

Equations (6) and (7) imply that the TV interest elasticity and semielasticity of money demand play crucial roles in evaluating the welfare cost of inflation. Thus, in our empirical reassessment of the welfare cost analysis, we first test for the unit income elasticity throughout the sample period and then determine the long-run (cointegrating) relationship between the ratio of money to income and the nominal interest rate in the two specifications—log–log and semilog models.

4. METHODOLOGY, DATA, AND RESULTS

4.1. Econometric Method

In his analysis using models with TI coefficients, Ireland (2009) tested the log–log and semilog specifications for cointegration, finding that the semilog form exhibited cointegration, whereas the log–log form did not. We revisit the issue of the welfare cost of inflation, using the TV-parameter method of cointegration developed by Park and Hahn (1999) and Bierens and Martins (2010).⁸

Park and Hahn (1999) consider a single equation cointegrating regression in the Engle–Granger (1987) tradition with TV parameters. They model the parameters of the cointegrating vector to follow smooth functions of time, using Fourier series expansions. They employ semi-nonparametric sieve estimators, deriving their asymptotic properties, and develop residual-based specification tests. Bierens and Martins (2010) permit the cointegrating vectors in a vector error-correction (VEC) model in the Johansen (1988, 1991) tradition to follow smooth functions of time, similar to Park and Hahn (1999). They model the TV cointegrating

vectors, however, using Chebyshev time polynomials. They estimate the extended VEC model following Johansen’s maximum likelihood approach and develop a likelihood ratio (LR) test for TV cointegration, wherein TI cointegration is the null hypothesis.

Using the TV parameter cointegration methods admits the possibility of a non-linear long-run money-demand function and thus, not knowing the true specification, we consider both models: the semilog and the log–log forms [Bae and deJong (2007)]. See also Granger (2008): “Any non-linear model can be approximated by a TV parameter linear model”.⁹ By specifying a model with TV coefficients, we are able to stick to the literature and obtain results for the semilog and log–log forms. On the other hand, we adopt a money-demand system-based specification, as it is more general and robust to endogeneity than the single equation strategy. It allows us to accommodate for the possibility that more than one cointegrating relationship may exist between the real measure of money, real income, and the nominal interest rate [Wolters and Lutkepohl (1998)].

Following the model specification in Section 5 of Bierens and Martins (2010), consider the TV VEC(*p*)model with a TI drift and Gaussian errors:

$$\Delta Z_t = \mu + \Pi'_t Z_{t-1} + \sum_{j=1}^{p-1} \Gamma_j \Delta Z_{t-j} + \varepsilon_t, \tag{8}$$

where $Z_t \in \mathbb{R}^k$, μ is a $k \times 1$ vector of intercepts, $\varepsilon_t \sim N_k[0, \Omega]$, and T is the number of observations. Our first objective is to test the null-hypothesis of TI cointegration, $\Pi'_t = \Pi' = \alpha\beta'$, where α and β are the fixed $k \times r$ matrices with rank r , against TV cointegration of the type: $\Pi'_t = \alpha\beta'_t$, where α is the same as before, but now β_t ’s are TV $k \times r$ matrices with rank r . In both cases, Ω and Γ_j ’s are fixed $k \times k$ matrices, and $1 \leq r \leq k$. In the case of our model, $k = 3$ or $k = 2$ and $r = 1$ and the first equation gives the money-demand function. If we find evidence for TV cointegration, we compute the TV welfare costs out of the estimated TV cointegrating vector.

Assuming that the function of discrete time β_t is smooth [see Bierens and Martins (2010), for details], and defining $\xi_{i,T} = \frac{1}{T} \sum_{t=1}^T \beta_t P_{i,T}(t)$, $i = 0, \dots, T-1$, as unknown $k \times r$ matrices, we can write β_t as follows:

$$\beta_t = \beta_m(t/T) = \sum_{i=0}^m \xi_{i,T} P_{i,T}(t), \tag{9}$$

for some fixed $m < T-1$, where the orthonormal Chebyshev time polynomials $P_{i,T}(t)$ are defined by: $P_{0,T}(t)=1$, $P_{i,T}(t)=\sqrt{2} \cos[i\pi(t - 0.5)/T]$, $t = 1, 2, \dots, T, i = 1, 2, 3, \dots, m$. Here, we choose m (and also p) according to the standard model selection procedures. We can then specify the error-correction model more conveniently with TI coefficients as follows:

$$\Delta Z_t = \mu + \alpha\xi' Z_{t-1}^{(m)} + \Gamma X_t + \varepsilon_t, \tag{10}$$

where $\xi' = (\xi'_0, \xi'_1 \dots \xi'_m)$ is an $r \times (m+1)k$ matrix of rank r , $Z_{t-1}^{(m)}$ is defined by

$$Z_{t-1}^{(m)} = [Z'_{t-1}, P_{1,T}(t)Z'_{t-1}, P_{2,T}(t)Z'_{t-1}, \dots P_{m,T}(t)Z'_{t-1}]' \tag{11}$$

and $X_t = (\Delta Z'_{t-1}, \dots \Delta Z'_{t-p+1})'$. To test for the null hypothesis of standard TI cointegration as in Johansen (1988, 1991) against the alternative of TV cointegration as defined by model (10), Bierens and Martins (2010) propose an LR test statistic wherein the restricted model takes $\xi' = (\beta', O_{r,k,m})$ and is asymptotically distributed as χ^2_{mkr} under the null hypothesis. The test statistic equals two times the difference of the log-likelihood of the VEC model under $m = 0$ and the log-likelihood of the unrestricted VEC model (10) [see Bierens and Martins (2010) for further details]. Despite the simplicity of the LR test, the asymptotic distribution appears to be a poor approximation to the relevant finite-sample distribution (the test falsely indicates the existence of TV cointegration too often). For that reason, in a recent paper, Martins (in press) proposes wild and independent and identically distributed parametric bootstrap implementations of the original LR test, as they all share the same first-order asymptotic null distribution. Martins (in press) shows that the bootstrap approximation to the finite-sample distribution is very accurate, in particular for the wild bootstrap case.

4.2. Data

In this study, we use quarterly time-series data from the first quarter of 1959 (1959:Q1) to the fourth quarter of 2010 (2010:Q4). Data come from the Federal Reserve Bank of St. Louis FRED database, except that we adjust the series for the measure of money supply (M1) by adding back the funds removed by retail deposit sweep programs using estimates stock based on the MIRS aggregate defined by Cynamon et al. (2006).¹⁰ We measure nominal income and the nominal interest rates by nominal GDP (Y) and the three-month US Treasury bill rate (r), respectively. We seasonally adjust all series, except for the Treasury bill rate, using the Census X12 method. When we use real money balances (M/P) and real GDP (Y/P) independently in the regressions, we divide the corresponding nominal series for MIRS and GDP by the GDP deflator (P), but when we use the money income ratio (m), we just divide MIRS by GDP (i.e., $m = \text{MIRS}/Y$).

Before conducting the cointegration analysis, we consider the time-series properties of the variables—the natural logarithms of money to GDP, real money, real GDP, the interest rate, as well as the level of the interest rate—using the augmented Dickey–Fuller (ADF, 1981), the Phillips–Perron (PP, 1988), the Dickey–Fuller generalized least-squares [DF-GLS, Elliott et al. (1996)], and the Ng–Perron (2001) unit-root tests with an intercept and with an intercept and trend. Table 1 reports the findings. We conclude that all series conform to I(1) processes.

TABLE 1. Unit root test results

Variable	Test type	Intercept	Conclusion	Intercept and trend	Conclusion
ln(<i>m</i>)	ADF	-2.503	I(1)	-0.581	I(1)
	PP	-2.712*	I(0)	-0.621	I(1)
	DF-GLS	-0.324	I(1)	-0.204	I(1)
	Ng-Perron	-0.279	I(1)	-0.676	I(1)
ln(<i>M/P</i>)	ADF	1.557	I(1)	-1.301	I(1)
	PP	1.861	I(1)	-1.072	I(1)
	DF-GLS	2.891	I(1)	-0.694	I(1)
	Ng-Perron	2.508	I(1)	-2.097	I(1)
ln(<i>Y/P</i>)	ADF	-1.933	I(1)	-2.131	I(1)
	PP	-2.168	I(1)	-1.671	I(1)
	DF-GLS	2.699	I(1)	-1.263	I(1)
	Ng-Perron	1.317	I(1)	-4.914	I(1)
ln(<i>r</i>)	ADF	0.629	I(1)	-0.080	I(1)
	PP	-1.156	I(1)	-1.008	I(1)
	DF-GLS	-0.227	I(1)	-0.815	I(1)
	Ng-Perron	2.035	I(1)	-0.187	I(1)
<i>R</i>	ADF	-1.715	I(1)	-2.194	I(1)
	PP	-2.034	I(1)	-2.363	I(1)
	DF-GLS	-1.456	I(1)	-1.540	I(1)
	Ng-Perron	-5.192	I(1)	-6.190	I(1)

Note: The critical values are as follows:

- ADF and PP with intercept (intercept and trend): -3.461, -2.875, and -2.574 (-4.002, -3.431, and -3.139) at the 1%, 5%, and 10% level of significance, respectively.
- DF-GLS with intercept (intercept and trend): -2.576, -1.942, and -1.615 (-3.461, -2.928, and -2.636) at the 1%, 5%, and 10% level of significance, respectively.
- Ng-Perron with intercept (intercept and trend): -13.800, -8.100, and -5.700 (-23.800, -17.300, and -14.200) at the 1%, 5%, and 10% levels of significance, respectively.

* significant at the 10% level.

4.3. Empirical Results

We begin by testing for a long-run relationship between money, income, and the interest rate according to the Meltzer (1963) log-log and the Cagan (1956) semilog specifications. Since the money-demand function provides an important component of many macroeconomic models, economic theory suggests that a long-run relationship should exist between money, income, and the interest rate.

Since we evaluate welfare costs as a percentage of the GDP, we need to test for the assumption of unitary income elasticity and, when evidence in its favor is found, impose it and estimate long-run money-demand equations, where the natural logarithm of the money-income ratio depends on the natural logarithm of the nominal interest rate (log-log) or the nominal interest rate (semilog). We analyze the confidence sets of the estimated TV income elasticity parameter in

TABLE 2. TV cointegration analysis of money demand

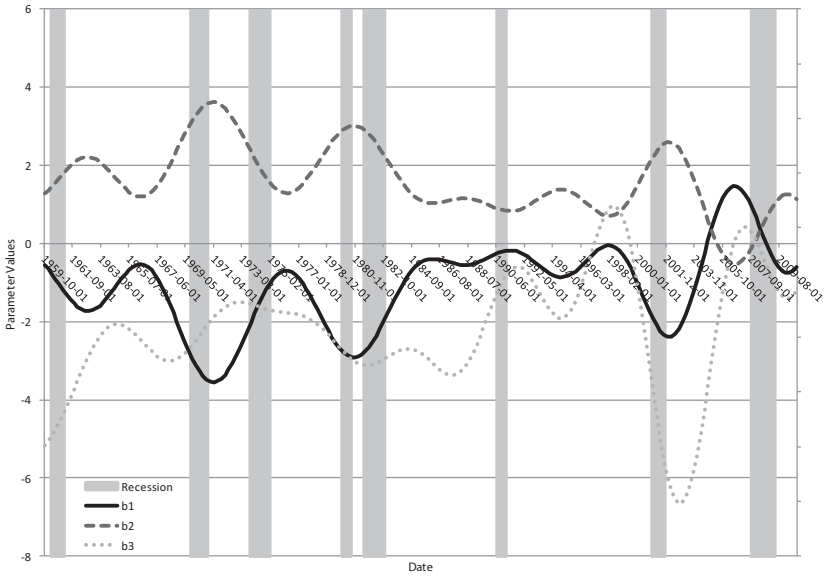
Money variable	Interest rate variable	Lag-length information criterion	p^*	m^*	TVC (LR)	WB	SB
$k = 3$							
ln(M/P)	r	SBC	2	15	(0.000)	(0.000)	(0.000)
		HQ	4	22	(0.000)	na	na
	ln(r)	SBC	2	19	(0.000)	(0.000)	(0.000)
		HQ	5	23	(0.000)	na	na
$k = 2$							
ln(m)	r	SBC	4	1	(0.006)	(0.030)	(0.033)
		HQ	4	22	(0.000)	na	na
	ln(r)	SBC	2	24	(0.000)	(0.000)	(0.000)
		HQ	7	29	(0.000)	na	na

Notes: Numbers in parentheses are p -values for null hypothesis of standard TI cointegration (Johansen) against the alternative hypothesis of TV cointegration; TVC is the original (chi-squared) statistic [Bierens and Martins (2010)]; WB is the Wild Bootstrap TVC statistic; and SB is the Sieve Bootstrap TVC statistic (Martins, in press). k is the number of variables in the cointegration system. That is, when k equals 3, the additional variable in the cointegration equations is the natural logarithm of real GDP (Y/P). p^* is the lag order chosen according to the SBC or HQ criteria. m^* is the chosen number of Chebishev polynomials, given p^* . “na” means that the estimation of the reduced rank regression is not possible.

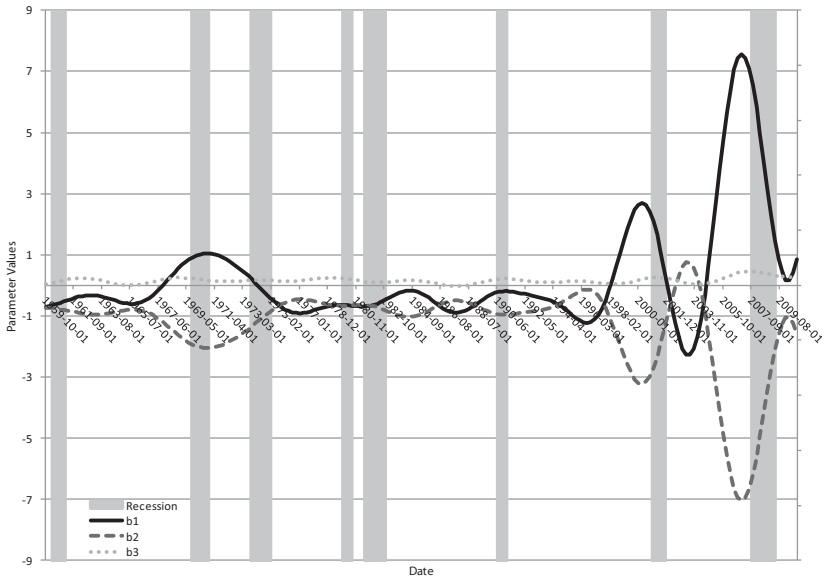
the cointegrated equations that involves real money balances, real income, and the interest rate, and choose the functional form (log–log or semilog) for which the estimate falls within the confidence set of an income elasticity of unitary.

In Table 2, we present the results for testing the standard TI cointegration of Johansen (1988, 1991) versus the TV cointegration of Bierens and Martins (2010). In all cases, we reject the null hypothesis of TI cointegration in the favor of TV cointegration. This table reports the results with and without imposing the constraint that the income elasticity of real money demand equals 1.

Although we initially estimate the model without imposing the restriction that the income elasticity of money demand equals 1, the calculation of the welfare cost of inflation requires a unitary income elasticity for all t . Figure 1 reports the TV coefficients for the long-run relationship with $k = 3$, where b_1 , b_2 , and b_3 are the coefficients of the natural logarithms of real money, real GDP, and the interest rate (levels, in Figure 1a), respectively.¹¹ The coefficient of the interest rate variable follows its own path but appears much more stable for the log–log specification of the model. We note that for both the log–log and semilog specifications, the movement in the coefficients of the natural logarithm of real money and real GDP mirrors each other such that the ratio tends to remain relatively constant and, possibly, for almost the entire sample, equal to 1 in the absolute value, as also suggested in Figure 2 (plots the income elasticity of real money demand relative to 1). Furthermore, we test whether, in fact, the real income elasticity of money

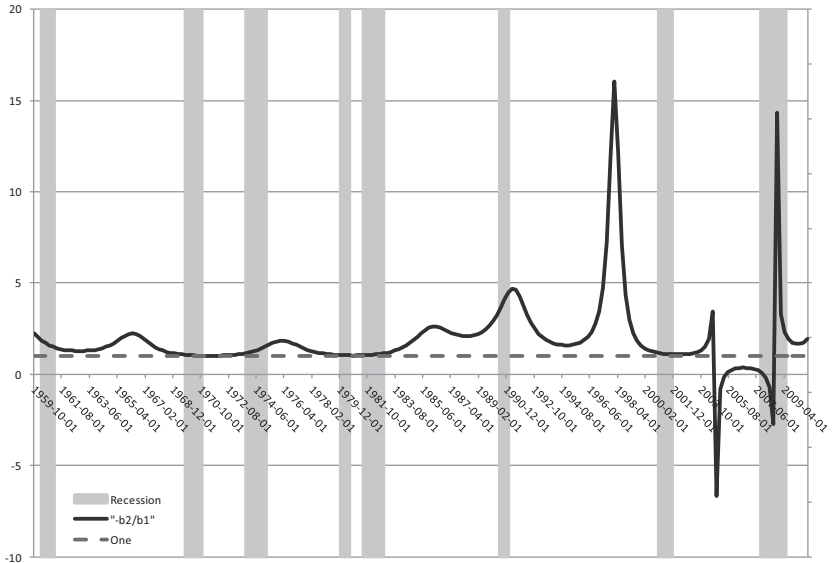


(a)

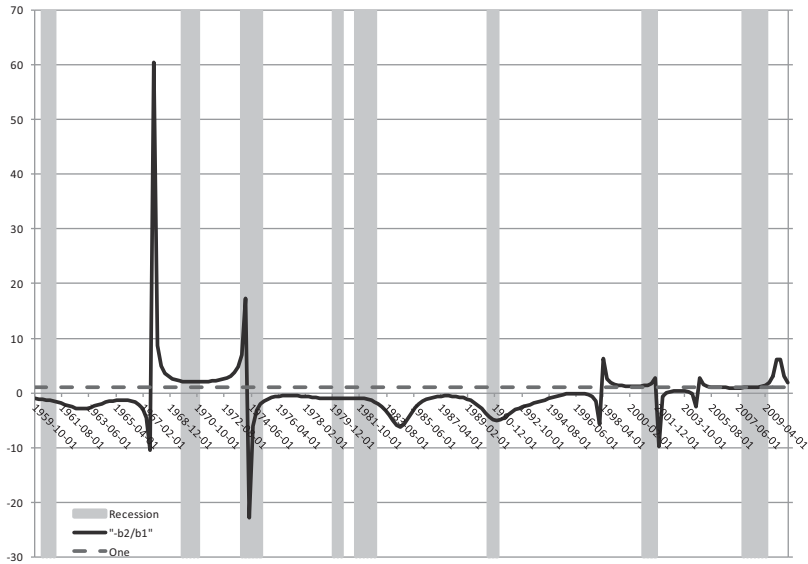


(b)

FIGURE 1. TV cointegration coefficients. (a) Semilog specification. (b) Log-log specification.



(a)



(b)

FIGURE 2. TV income elasticities. (a) Semilog specification. (b) Log-log specification.

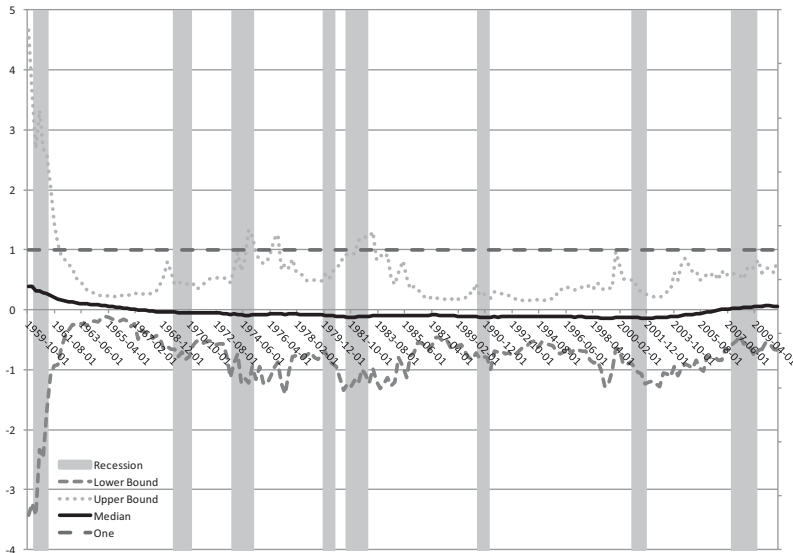
demand equals 1 throughout by means of the bootstrap distribution of the estimated coefficient as explained in Martins (in press). Figure 3 plots the upper and lower 90% confidence bands for $-b_2/b_1$ relative to one as well as the median points, all based on the wild bootstrap procedure. We conclude that only the log–log specification exhibits an income elasticity that does not differ significantly from one during the whole sample.¹²

Ireland (2009) provides graphs that show the actual values of the nominal interest rate and the money-to-income ratio as well as the semilog and log–log money-demand specifications (see Figure 2, p. 1043). He also identifies actual values from 1900 to 1979 and from 1980 to 2006, the end of his sample period. The latter, more-recent data did not associate with large increases in money demand as the interest rate went to low levels, around 1% in his sample period. As such, Ireland (2009) suggested "... the semilog specification ... may now provide a more accurate description of money demand. ... the new data points appear to trace out a demand curve that is far less interest-elastic ... (than) the earlier data ... " (p. 1043). Our TV cointegration relationship sees parameters changing over time. Thus, in Figure 4, we also plot the actual and fitted values for the money-to-income ratio ($MIRS/Y$). The estimated TV cointegration model in log–log form fits the actual data closely, which clearly did not occur in Ireland (2009) where he found spurious regression.

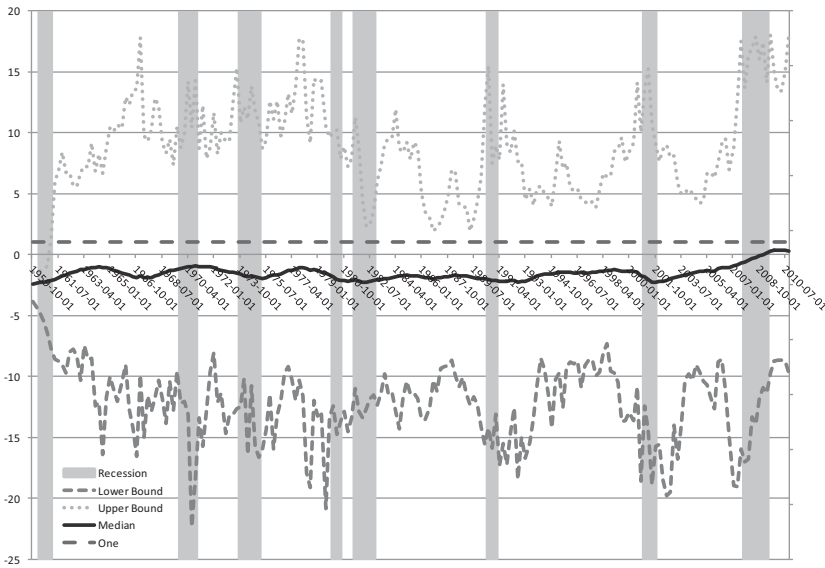
Furthermore, Ireland suggested that the interest elasticity of money demand changed in the post-1980 period. We plot the TV elasticity in Figure 5. We see that the elasticity varies between 0.013 and 0.250 and although the elasticity varies over the sample period, we find an average elasticity of 0.123. Moreover, the average elasticity over the same sample period considered by Ireland (2009) equals 0.113, whereas he finds an elasticity of 0.0873. Thus, our TV cointegration does not differ dramatically from his. Moreover, we do not find a big change in the interest elasticity of money demand between pre-1980, where it equals 0.129, and post-1979, where it equals 0.119.¹³

We do observe a large decrease in the elasticity from 1986 extending through 1998. A couple of events did transpire around 1980 that could contribute to this decline. First, the US Congress enacted a series of deregulatory legislation, beginning with the Depository Institution Deregulation and Monetary Control Act of 1980 and culminating with the Riegle–Neal Interstate Banking and Branching Efficiency Act of 1994 and the Gramm–Leach–Bliley Act Financial Services Modernization Act of 1999. Second, beginning in 1982 or 1984, economists refer to the US economy as experiencing the Great Moderation. Whether due to good (monetary) policy, good luck, or something else, the US economy saw a diminution in the volatility of many macroeconomic variables.¹⁴ In sum, the freeing of regulation and the reduction in macroeconomic volatility may have contributed to the large reduction in the interest elasticity of money demand, which moves the money market toward the classical paradigm.

Since we use the log–log specification, we calculate the welfare cost of inflation from equation (6) for three different values of inflation—0%, 2%, and 10%. We



(a)



(b)

FIGURE 3. Income elasticities: Upper and lower bounds. (a) Semilog specification. (b) Log-log specification.

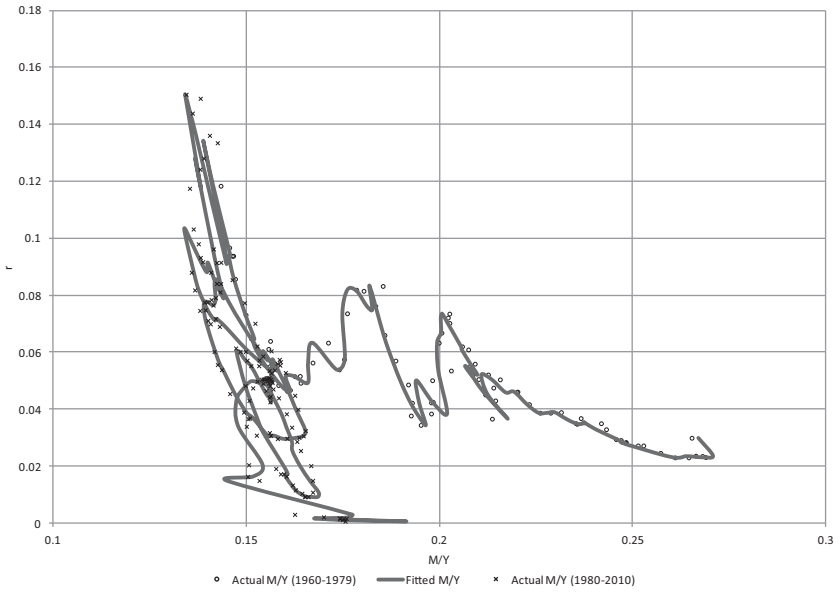


FIGURE 4. Fitted and actual money/income versus the nominal interest rate.

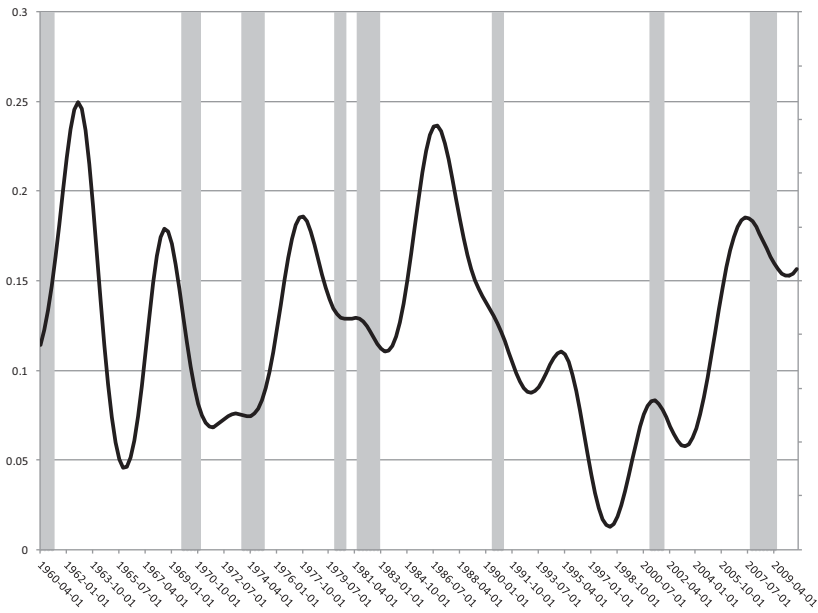


FIGURE 5. TV interest elasticity of money demand.

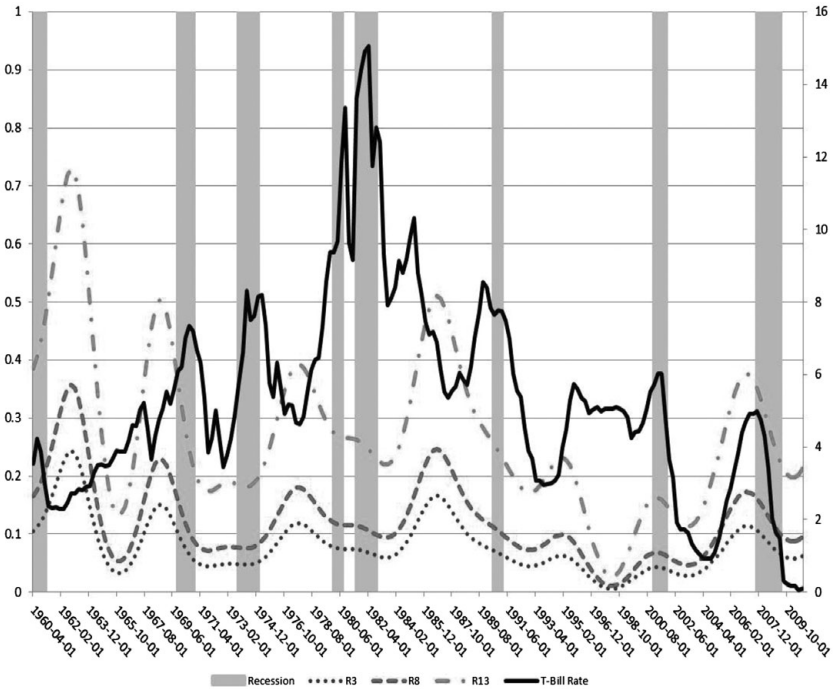


FIGURE 6. TV welfare cost of inflation, 0%, 2%, and 10% inflation.

plot the three different measures of welfare cost in Figure 6 measured as a percent, along with the interest rate also measured as a percent. Finally, the chart also includes the National Bureau of Economic Research recession dates in gray bars.

Examining the average welfare costs, recessions experience, on average, lower welfare costs than expansions, which, as depicted in Figure 5, reflects the higher average interest elasticity during the expansions. More specifically, expansions average 12%, 10%, and 7% higher welfare costs than recessions for the 0%, 2%, and 10% inflation rates, respectively. The maximum and minimum values of the welfare cost across the three values of inflation occur in 1962:Q4 and 1998:Q2, respectively. In addition, the Treasury-bill rate averages 48% higher (i.e., 7.21% versus 4.87%) during recessions relative to expansions.

Table 3 reports the empirical distribution of welfare costs for 0%, 2%, and 10% inflation rates.¹⁵ The distributions tend to concentrate at the lower end of the welfare cost distribution. The mean and median welfare costs rise as we move from 0% to 2% to 10% inflation. Ireland (2009) reports welfare costs as a percent of income for the static OLS model of 0.0131, 0.0356, and 0.219 for the 0%, 2%, and 10% inflation rates, respectively. Our welfare cost results exceed Ireland's, equaling 0.08, 0.123, and 0.277 as a percent of income, respectively.

TABLE 3. Descriptive statistics: Welfare cost (1959:Q4–2010:Q4)

Inflation rate (%)	Mean	Median	Maximum	Minimum	Standard deviation	Jarque–Bera
0	0.080	0.067	0.243 [1962:Q4]	0.006 [1998:Q2]	0.047	69.005 (0.00)
2	0.123	0.106	0.357 [1962:Q4]	0.010 [1998:Q2]	0.069	56.371 (0.00)
10	0.277	0.2444	0.731 [1962:Q4]	0.026 [1998:Q2]	0.142	36.999 (0.00)

Notes: Numbers in brackets correspond to the specific quarter for which maximum and minimum welfare costs are attained. Numbers in parentheses indicates the *p*-value of the Jarque–Bera test.

5. CONCLUSION

This paper revisits the estimation of the welfare costs of inflation, using TV cointegration to estimate the long-run money demand in the log–log and semilog specifications of Meltzer (1963) and Cagan (1956). In preliminary tests, we find strong evidence against the standard TI specification of Johansen (1988, 1991) and in favor of the VEC model of Bierens and Martins (2010) where the cointegration vector is TV according to a flexible Fourier function of time, the Chebyshev time polynomials, thus providing a much better fit of the actual data. This means that Fischer’s (1981), Serletis and Yavari’s (2004), and Ireland’s (2009) estimates of the welfare cost of inflation for the US economy probably, in fact, measure the average of welfare cost of an actual changing welfare cost over time.

We conclude that the semilog specification does not exhibit unit income elasticity. Instead, the log–log model does present a unitary elasticity for the whole sample, and our estimate of the welfare cost of inflation for a 10% inflation rate lies in the range of 0.025–0.75% of GDP. In sum, our findings fall well within the ranges of existing studies of the welfare cost of inflation. The interest elasticity of money demand shows substantial variability over our sample period.

The log–log model proves more consistent with economic theory than the semilog model. That is, the semilog specification yields a functional form that exhibits an interest elasticity that varies as a function of the interest rate. Moreover, when the interest rate equals zero, the elasticity is finite. The log–log specification assumes a constant interest rate elasticity, but in our method, this elasticity changes over time as its estimate is TV. Finally, the log–log specification proves consistent with the zero interest rate bound, since the demand for money becomes asymptotic to the horizontal axis as the interest rate approaches zero.

We do observe a large decrease in the interest elasticity of money demand from 1986 extending through 1998. The US Congress enacted a series of deregulatory legislation, beginning in the early 1980s through the late 1990s. Also, beginning in the early 1980s, the US economy experienced the Great Moderation. These two factors may explain some of the movements in the elasticity during this time

frame. In addition, we observe that the interest elasticity generally declines during recessions.

Two natural extensions of the analysis of TV welfare costs of inflation include the alternative specifications of general-equilibrium models [Cooley and Hansen (1989)] and partial-equilibrium models [Feldstein (1997, 1999)] as well as studying the implications of assuming an interest rate that equals zero in the limit.

NOTES

1. If some portion of the monetary aggregate pays a positive interest rate, then the opportunity cost of holding money differs from that assumed by Bailey (1956), Lucas (2000), and Ireland (2009). The opportunity cost and the welfare cost in this case relies on the adjusted interest rate that takes out the interest rate paid on that portion of the monetary aggregate that receives interest payment. Cysne (2003) and Cysne and Turchick (2010) note that this leads to the Divisia Index methodology.

2. Miller (1986) offered an early explanation that relied on financial innovation and deregulation, using data through 1983. More recently, Lucas and Nicolini (2013) also argued that regulatory changes can explain the post-1973 problems with money demand.

3. For a detailed review of the international literature on the welfare costs of inflation, refer to Gupta and Uwilingiye (2010).

4. Cysne (2009) also shows that under certain conditions, Bailey's methodology fits into a general-equilibrium methodology as well.

5. For example, Dibooglu and Kenc (2009) use a stochastic general-equilibrium balanced growth model to re-examine the welfare cost of inflation. Their model incorporates recursive utility, portfolio balance effects, monetary volatility, and monetary policy uncertainty. They find that that a monetary policy can exhibit substantial welfare effects, where portfolio adjustments seem to explain a major part of the welfare adjustments. Dotsey and Ireland (1996) use a general equilibrium monetary model, wherein the inflation rate distorts a series of marginal decisions. They find that the traditional, partial equilibrium approach can seriously underestimate the welfare cost of inflation. Gupta and Majumdar (2014) provide the exception. They estimate a nonparametric long-run money demand function and find welfare costs comparable to general equilibrium estimates, since the data coverage by the nonparametric function far exceeds the coverage in a linear money demand specification.

6. As noted in the Introduction, Ireland (2009) begins his sample in 1980, since he sees possible structural change in the quarterly sample between 1979 and 1980. He suspects that the semilog specification will perform better in the post-1979 period rather than the log-log specification that Lucas (2000) uses. Ireland confirms that the semilog specification dominates the log-log specification in his quarterly sample.

7. Lucas (2000) uses the Sidrauski and a shopping-time model in his welfare calculations, and not Bailey's area under the inverse demand formula. In both cases, Lucas's calculations lead to numerical results close to Bailey's, but differing because of the general-equilibrium perspectives.

8. Other approaches to modifying the original linear specification of cointegration include sudden deterministic structural breaks and Markov-switching approaches. Regarding TV error-correction models, Hansen (2003) generalizes reduced-rank methods to cointegration under sudden regime shifts with a known number of break points, whereas Andrade et al. (2005) develop tests on the cointegration rank and on the cointegration space under known and unknown break points. The Markov-switching approach of Hall et al. (1997) and the smooth transition model of Saikkonen and Choi (2004) provide interesting approaches to modeling shifts in cointegrating vectors.

9. The literature that examines nonlinear long-run relationships is not new and it includes, for example, Blake and Fomby (1997), de Jong (2001), Granger and Yoon (2002), Harris et al. (2002), and Juhl and Xiao (2005).

10. We also performed the analysis using M1 and not correcting for sweep programs. We find better performance for the measure of M1 that adjusts for sweep programs.

11. Comparing these coefficients to equations (1) and (2), α and β both equal $(-b_2/b_1)$ and η and ξ both equal b_3/b_1 .

12. Figure 3 reports the bootstrapped confidence bands. The median line gives the midpoint (median) of all the estimates for the bootstrapped estimations. The maximum likelihood estimate point estimates from the original data set are given in Figure 2.

13. Mogliani and Urga (2015) find for their cointegration model with structural breaks that before 1945, the interest elasticity equals 0.13, between 1945 and 1976, it equals 0.43, and after 1976, it equals 0.12.

14. We do find a positive correlation between the interest elasticity and the growth rate of the M1 money stock.

15. Similar figures and tables on the 0% and 2% inflation rates are available from the authors.

REFERENCES

- Adão, B. and A. C. Silva (2013) Government financing with taxes or inflation. SSRN: <http://ssrn.com/abstract=2395815>.
- Aiyagari, S. R., R. A. Braun, and Z. Eckstein (1998) Transaction services, inflation, and welfare. *Journal of Political Economy* 106, 1274–1301.
- Andrade, P., C. Bruneau, and S. Gregoir (2005) Testing for the cointegration rank when some cointegrating directions are changing. *Journal of Econometrics* 124, 269–310.
- Bae, Y. and R. M. de Jong (2007) Money demand function estimation by nonlinear cointegration. *Journal of Applied Econometrics* 22(4), 767–793.
- Bailey, M. (1956) The welfare cost of inflationary finance. *Journal of Political Economy* 64, 93–110.
- Barigozzi, M. and A. M. Conti (2014) On the stability of Euro Area money demand and its implications for monetary policy. SSRN: <http://ssrn.com/abstract=1599669>.
- Bierens, H. J. and L. F. Martins (2010) Time-varying cointegration. *Econometric Theory* 26, 1453–1490.
- Blake, N. S. and T. B. Fomby (1997) Threshold cointegration. *International Economic Review* 38, 627–645.
- Boel, P. and G. Camera (2011) The welfare cost of inflation in OECD countries. *Macroeconomic Dynamics* 15(Suppl. 2), 217–251.
- Burstein, A. and C. Hellwig (2008) Welfare costs of inflation in a menu cost model. *American Economic Review* 98, 438–443.
- Cagan, P. (1956) The monetary dynamics of hyperinflation. In M. Friedman (ed.), *Studies in the Quantity Theory of Money*, pp. 25–117. Chicago: University of Chicago Press.
- Calza, A. and A. Zaghini (2009) Nonlinearities in the dynamics of the Euro Area demand for M1. *Macroeconomic Dynamics* 13, 1–19.
- Chow, G. C. (1966) On the long-run and short-run demand for money. *Journal of Political Economy* 74, 111–131.
- Cooley, T. F. and G. Hansen (1989) The inflation tax in a real business cycle. *American Economic Review* 79, 733–744.
- Cooley, T. F. and G. Hansen (1991) The welfare cost of moderate inflations. *Journal of Money, Credit and Banking* 23, 483–503.
- Craig, B. and G. Rocheteau (2008) Inflation and welfare: A search approach. *Journal of Money, Credit and Banking* 40, 89–119.
- Cynamon, B. Z., D. H. Dutkowsky, and B. E. Jones (2006) Redefining the monetary aggregates: A clean sweep. *Eastern Economic Journal* 32(4), 661–672.
- Cysne, R. P. (2003) Divisaindex, inflation and welfare. *Journal of Money, Credit and Banking* 35, 221–239.
- Cysne, R. P. (2009) Bailey's measure of welfare costs of inflation as a general equilibrium measure. *Journal of Money, Credit and Banking* 41, 451–459.

- Cysne, R. P. and D. Turchick (2010) Welfare costs of inflation when interest-bearing deposits are disregarded: A calculation of the bias. *Journal of Economic Dynamics and Control* 34, 1015–1030.
- de Jong, R.M. (2001) Nonlinear estimation using estimated cointegrating relations. *Journal of Econometrics* 101, 109–122.
- Dibooglu, S. and T. Kenc (2009) Welfare cost of inflation in a stochastic balanced growth model. *Economic Modelling* 26, 650–658.
- Dickey, D. and W. Fuller (1981) Likelihood ratio statistics for autoregressive time series with a unit root. *Econometrica* 49, 1057–1072.
- Dotsey, M. and P. N. Ireland (1996) The welfare cost of inflation in general equilibrium. *Journal of Monetary Economics* 37, 29–47.
- Duprey, J. N. (1980) The search for a stable money demand equation. *Federal Reserve Bank of Minneapolis Quarterly Review* 4(3), 5–14.
- Elliott, G., T. J. Rothenberg, and J. H. Stock (1996) Efficient tests for an autoregressive unit root. *Econometrica* 64, 813–836.
- Engle, R. F. and C. W. J. Granger (1987) Cointegration and error correction: Representations, estimation and testing. *Econometrica* 55, 251–276.
- Escribano, A. (2004) Nonlinear error correction: The case of money demand in the United Kingdom (1878–2000). *Macroeconomic Dynamics* 8, 76–116.
- Evans, L. and T. Kenc (2003) Welfare cost of monetary and fiscal policy shocks. *Macroeconomic Dynamics* 7, 212–238.
- Feldstein, M. (1997) The costs and benefits of going from low inflation to price stability. In C. D. Romer and D. H. Romer (eds.), *Reducing Inflation: Motivation and Strategy*, pp. 123–156. Chicago: The University of Chicago Press.
- Feldstein, M. (1999) Capital income taxes and the benefit of price stability'. In M. Feldstein (ed.), *The Costs and Benefits of Price Stability*, pp. 9–46. Chicago and London: The University of Chicago Press.
- Fischer, S. (1981) Towards an understanding of the costs of inflation: II. *Carnegie-Rochester Conference Series on Public Policy* 15, 5–41.
- Friedman, M. (1969) *The Optimum Quantity of Money and Other Essays*. Chicago: Aldine Publishing Company.
- Garcia, G. and S. Pak (1979) Some clues in the case of the missing money. *American Economic Review* 69(2), 330–334.
- Gillman, M. (1993) The welfare cost of inflation in a cash-in-advance economy with costly credit. *Journal of Monetary Economics* 31, 97–115.
- Gillman, M. (1995) Comparing partial and general equilibrium estimates of the welfare cost of inflation. *Contemporary Economic Policy* 13, 60–71.
- Goldfeld, S. M. (1976) The case of the missing money. *Brookings Papers on Economic Activity* 3, 683–739.
- Gomme, P. (1993) Money and growth revisited: Measuring the costs of inflation in an endogenous growth model. *Journal of Monetary Economics* 32, 51–77.
- Granger, C. W. J. (2008) Non-linear models: Where do we go next—time varying parameter models? *Studies in Nonlinear Dynamics and Econometrics* 12, 1–11.
- Granger, C. W. J. and G. Yoon (2002) Hidden Cointegration. Working paper no. 2002-02, University of California, San Diego.
- Gupta, R. and A. Majumdar (2014) Reconsidering the welfare cost of inflation in the US: A non-parametric estimation of the nonlinear long-run money demand equation using projection pursuit regressions. *Empirical Economics* 46, 1221–1240.
- Gupta, R. and J. Uwilingiye (2010) Evaluating the welfare cost of inflation in a monetary endogenous growth general equilibrium model: The case of South Africa. *International Business and Economics Research Journal* 9, 101–112.
- Hafer, R. W. and D. W. Jansen (1991) The demand for money in the United States: Evidence from cointegration tests. *Journal of Money, Credit and Banking* 23, 155–168.

- Hall, S. G., Z. Psaradakis, and M. Sola (1997) Cointegration and changes in regime: The Japanese consumption function. *Journal of Applied Econometrics* 12, 151–168.
- Hansen, P. R. (2003) Structural changes in the cointegrated vector autoregressive model. *Journal of Econometrics* 114, 261–295.
- Harris, D., B. McCabe, and S. Leybourne (2002) Stochastic cointegration: Estimation and inference. *Journal of Econometrics* 111, 363–384.
- Henriksen, E. and F. Kydland (2010) Endogenous money, inflation and welfare. *Review of Economic Dynamics* 13, 470–486.
- Ireland, P. N. (2009) On the welfare cost of inflation and the recent behavior of money demand. *American Economic Review* 99, 1040–1052.
- Jawadi, F. and R. M. Sousa (2013) Money demand in the euro area, the US and the UK: Assessing the role of nonlinearity. *Economic Modelling* 32(C), 507–515.
- Johansen, S. (1988) Statistical analysis of cointegration vectors. *Journal of Economic Dynamics and Control* 12, 231–254.
- Johansen, S. (1991) Estimation and hypothesis testing of cointegration vectors in Gaussian vector autoregressive models. *Econometrica* 59, 1551–1580.
- Judd, J. P. and J. L. Scadding (1982) The search for a stable money demand function. *Journal of Economic Literature* 20, 993–1023.
- Juhl, T. and Z. Xiao (2005) Testing for cointegration using partially linear models. *Journal of Econometrics* 124, 363–394.
- Khan, M. S. (1974) The stability of the demand for money function in the United States, 1901–65. *Journal of Political Economy* 82, 1205–1220.
- Kumar, S. (2014) The varying interest elasticity and the cost of inflation in India. *Applied Economics Letters* 21, 497–500.
- Lagos, R. and R. Wright (2005) A unified framework for monetary theory and policy analysis. *Journal of Political Economy* 113, 463–484.
- Lim, C., F. Columba, A. Costa, P. Kongsamut, A. Otani, M. Saiyid, T. Wezel, and X. Wu (2011) Macroprudential Policy: What Instruments and How to Use Them? Lessons from Country Experiences. IMF working paper no. 11/238.
- Lucas, R. E. Jr. (1981) Discussion of: Stanley Fischer, ‘towards an understanding of the costs of inflation: II.’ *Carnegie-Rochester Conference Series on Public Policy* 15, 43–52.
- Lucas, R. E. Jr. (1994) The Welfare Costs of Inflation. CEPR working paper no. 394.
- Lucas, R. E. Jr. (2000) Inflation and Welfare. *Econometrica* 68, 247–274.
- Lucas, R. Jr. and J. Nicolini (2013) On the Stability of Money Demand. 2013 Meeting Papers 353, Society for Economic Dynamics.
- Lütkepohl, H. (1993) The sources of the U.S. money demand instability. *Empirical Economics* 18(4), 729–743.
- Martins, L. F. (in press) Bootstrap tests for time varying cointegration. *Econometric Reviews*.
- Meltzer, A. H. (1963) The demand for money: The evidence from the time series. *Journal of Political Economy* 71, 219–246.
- Miller, S. M. (1986) Financial innovation, depository institution deregulation, and the demand for money. *Journal of Macroeconomics* 8, 279–296.
- Miller, S. M. (1990) Disequilibrium macroeconomics, money as a buffer stock, and the estimation of money demand. *Journal of Macroeconomics* 12, 563–586.
- Miller, S. M. (1991) Monetary dynamics: An application of cointegration and error-correction modeling. *Journal of Money, Credit and Banking* 23, 139–154.
- Mogliani, M. and G. Urga (2015) On the instability of long-run money demand and the welfare cost of inflation in the U.S. Mimeo, Faculty of Finance, Cass Business School.
- Nakashima, K. (2009) An extremely-low-interest-rate policy and the shape of the Japanese money demand function. *Macroeconomic Dynamics* 13, 553–579.
- Nakashima, K. and M. Saito (2012) On the comparison of alternative specifications for money demand: The case of extremely low interest rate regimes in Japan. *Journal of the Japanese and International Economies* 26, 454–471.

- Ng, S. and P. Perron (2001) Lag length selection and the construction of unit root tests with good size and power. *Econometrica* 69, 1519–1554.
- Pakko, M. R. (1998) Shoe-leather costs of inflation and policy credibility. *Federal Reserve Bank of St. Louis Review* 80, 37–50.
- Park, J. Y. and S. B. Hahn (1999) Cointegrating regressions with time varying coefficients. *Econometric Theory* 15, 664–703.
- Phillips, P. and P. Perron (1988) Testing for a unit root in time series regression. *Biometrika* 75, 335–346.
- Rao, B. B. and S. Kumar (2011) Is the US demand for money unstable? *Applied Financial Economics* 21, 1263–1272.
- Saikkonen, P. and I. Choi (2004) Cointegrating smooth transition regressions. *Econometric Theory* 20, 301–340.
- Serletis, A. and A. Shahmoradi (2005) Semi-nonparametric estimates of the demand for money in the United States. *Macroeconomic Dynamics* 9, 542–559.
- Serletis, A. and A. Shahmoradi (2007a) A note on imposing local curvature in generalized Leontief models. *Macroeconomic Dynamics* 11, 290–294.
- Serletis, A. and A. Shahmoradi (2007b) Flexible functional forms, curvature conditions, and the demand for assets. *Macroeconomic Dynamics* 11, 455–486.
- Serletis, A. and K. Yavari (2004) The welfare cost of inflation in Canada and the United States. *Economics Letters* 84, 199–204.
- Silva, A. C. (2012) Rebalancing frequency and the welfare cost of inflation. *American Economic Journal: Macroeconomics* 4, 153–183.
- Tsafatsion, L. and J. M. Veitch (1990) U.S. money demand instability: A flexible least squares approach. *Journal of Economic Dynamics and Control* 14, 151–173.
- Vinod, H. R. (1998) Nonparametric estimation of non-linear money demand cointegration equation by projection pursuit methods. In S. Weisberg (ed.), *Computing Science and Statistics*, vol. 30, pp. 174–183. Fairfax, Virginia: Interface Foundation.
- Wang, Y. (2011) The stability of long-run money demand in the United States: A new approach. *Economics Letters* 111, 60–63.
- Wolters, J. and H. Lütkepohl (1998) A money demand system for German M3. *Empirical Economics* 23, 371–386.
- Wu, Y. and J. Zhang (1998) Endogenous growth and the welfare costs of inflation: A reconsideration. *Journal of Economic Dynamics and Control* 22, 465–482.
- Zuo, H. and S. Y. Park (2011) Money demand in China and time-varying cointegration. *China Economic Review* 22, 330–343.