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Attention is called to the fact that the JOURNAL invites submission of (1) original technical papers in the field of symbolic logic, (2) expository papers in this field, (3) philosophical papers which bear upon this field or make use of its methods, and (4) studies in the history of logic in which modern technical developments are taken into account.

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ERRATA

VOLUME 20

Page 197, line 18. For « H. S. CALDWELL », read « S. H. CALDWELL ».
Page 321, column 2, line 10. For « H. S. », read « S. H. ».

VOLUME 22

Page 348, line 17. Delete the negation sign and for $= 0$, read $= 1$.

VOLUME 23

Page 134, line 5. For e , read \dot{e} .
Page 314, line 6 from the bottom. For R_e^a , read $R_{\dot{e}}^a$.

VOLUME 24

Page ii, line 5. For « Maart », read « March ».
Page 190, line 17. For « ŁUSZCZEWESKA », read « ŁUSZCZEWSKA ».
Page 287, the unnumbered footnote. For 1959, read 1958.
Page 347, column, next-to-last line. For « Semantics », read « semantics ».
Page 353. The first line at the top of column 2 should be indented.

VOLUME 25

Page ii, line 5. For $\delta\delta$, read 9.
Page 158, line 7 from the bottom. For \sim , read \sim .
Page 179, line 23. For XIII, read XXIII.
Page 182, line 14. For \sim , read \sim .
Page 250, line 9. For « "Función" », read « "Función" ».
Page 265, line 26. For « f. », read « ff. ».
Page 265, last line. For « f. », read « ff. ».
Page 266, line 17. For « f. », read « ff. ».
Page 269, line 1. Add a hyphen at the end of the line.
Page 284. Insert space between lines 7 and 6 from the bottom.
Page 297, line 4. For « consequences », read « conséquences ».
Page 330, line 6 from the bottom. For the first P_2 read P_0 .
Page 334, line 2. Delete parentheses, twice.
Page 354, line 24. For « systeme », read « système ».
Page 358, line 10 from the bottom. For], read [.
Page 360, line 3. For $(x/p)(y/q)$, read $\begin{pmatrix} x \\ p \end{pmatrix} \begin{pmatrix} y \\ q \end{pmatrix}$.
Page 361, line 22. For XXV 000(0), read XXV 356(1).
Page 361, line 27. For $a < b$, read $a <_{\Delta} b$.
Page 362, line 24. For « HILLARY », read « HILARY ».

ERRATA

- Page 370, last line. For « *for the synthesis* », read « *in synthesis* ».
Page 376, line 31 from the bottom. For « *pure* », read « "*pure*" ».
Page 377, line 19. For « ZIEMBINSKI », read « ZIEMBIŃSKI ».
Page 380, line 9. For XXV 000, read XXV 299(1).
Page 380, line 7 from the bottom. For « PAWŁOWSKI », read « PAWŁOWSKI ».
Page 381, line 3. For « Bochenski », read « Bocheński ».
Page 381. Insert space between lines 6 and 7.
Page 381, line 10. For XXV 271, read XXV 269.
Page 383, line 15. For « Ferruccio Rossi-Landi », read « FERRUCCIO ROSSI-LANDI ».

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- Page 16, line 11 and line 16. For †, read |.