

## PROBLEMS FOR SOLUTION

P 50. (Corrected) Let  $A(t)$  be an  $n \times n$  matrix which is continuous on an interval  $I: a < t < b$  of the real  $t$ -axis. Show that on a subinterval of  $I$  there exists a complex continuously differentiable and non-singular matrix  $T(t)$  such that the substitution  $x = T(t)y$  transforms the linear and homogeneous system of  $n$  differential equations  $\frac{dx}{dt} = A(t)x$  into a similar system  $\frac{dy}{dt} = B(t)y$  with  $B(t)$  continuous and skew-symmetric.

H. Helfenstein, University of Ottawa

P 55. Let  $P$  be a regular polygon and  $S$  a concentric sphere. Prove that the sum of the squares of the distances from a variable point of  $S$  to the vertices of  $P$  is a constant.

L. Moser, University of Alberta

P 56. If  $x \neq 0$  prove that

$$y + y^2 = x + x^2 + x^3$$

has no solutions in integers.

W. J. Blundon,  
Memorial University of Newfoundland

P 57. Let  $m, n$  be relatively prime positive integers:  $(m, n) = 1$ . Write

$$f(x) = \frac{(1-x^{mn})(1-x)}{(1-x^m)(1-x^n)},$$

and show

(i)  $f(x)$  is a polynomial of degree  $(m-1)(n-1)$  whose non-zero coefficients are alternately  $+1$  and  $-1$ ,

(ii) the number of non-zero coefficients is

$$Mm + Nn - 2MN$$

where  $M, N$  are integers defined by  $Mm - Nn = 1$ ,  $0 < M < n$ .

J. D. Dixon  
California Institute of Technology

P 58. (Conjecture) A graph of  $\binom{k}{2} + t$  edges with  $0 \leq t < k$  has at most  $\binom{k}{3} + \binom{t}{2}$  triangles.

J. W. Moon and L. Moser,  
University of Alberta

## SOLUTIONS

P 43. (Corrected) Let  $G$  be a group generated by  $P$  and  $Q$ , and let  $H$  be the cyclic subgroup generated by  $T$ . If  $P$  and  $Q$  satisfy only the relations  $P^2QP = Q^2$  and  $Q^2PQ^{-4} = P^k$  for some  $k$ , then the index of  $H$  in  $G$  is 1 or 7.

N. S. Mendelsohn, University of Manitoba

Solution by F. A. Sherk, University of Toronto.  
Enumerating cosets of  $H$  by the Todd-Coxeter method (Coxeter and Moser, Generators and Relations for Discrete Groups, Ergebn. Math. 14 (1957) Chapter 2), we obtain the tables